UNIVERSITÀ
DEGLI STUDI DI MILANO-BICOCCA

COURSE SYLLABUS

Numerical Analysis

2021-3-E3501Q058

Aims

In line with the educational objectives of the Bachelor Degree in Mathematics, the course aims at providing the basic knowledge, with a deep theoretical support, about the topics of the course (mainly optimization problems, and also discretization of ordinary differential equations). It will also build the skills needed to understand, analyse and compare the different methods, in addition to implementing them in the computer.

Contents

The main part of the course is about optimization problems in R^n, whose resolution is a fundamental step in many applied math problems. We will consider the following topics: search for zeros of functions, then minima of functions, finally constrained minima. The last part of the course will instead consider the discretization of ordinary differential equations.

The course will provide a rigorous theoretical support of the methods considered, together with a computational lab part in MATLAB.

Detailed program

All the topics developed in class will have also a coding part in the computer Lab (MATLAB language). Some labs

will consider PDE problems that, after discretization/approximation by some numerical scheme, become optimization problems in R^N. We will consider the following topics. Iterative methods for fixed points, local and global convergence properties. Search of zeros of vector valued functions, quasi-Newton methods, examples, local convergence, modifications for global convergence. Search of minima of functions (in open sets), line search methods, examples, convergence properties. Search of constrained minima, Kuhn-Tucker and lagrangian theory, projected gradient, Uzawa method, convergence properties. Ordinary differential equations, one step methods, convergence theory, absolute stability, RK methods.

Prerequisites

The standard knowledge of a third year math student is sufficient

Teaching form

Standard blackboard classes, plus practice classes in the computer Lab.

During the Covid-19 emergency period the classes will be delivered remotely, making use of video recording. Some special events and clarifications/tutorials will be delivered by direct online meetings.

Textbook and teaching resource

• C.T. Kelley, “Iterative methods for linear and nonlinear equations”, SIAM

• J. Nocedal, S.J. Wright, “Numerical Optimization”, Springer

• P.G. Ciarlet, “Introduction to numerical linear algebra and optimizations”, Cambridge Texts in Applied Math

• Uploaded pdf text on the Ordinary Diff. Eq. part

Semester

Second semester.

Assessment method

The exam is an oral examination, and is divided into two parts. In the first part, the student presents a matlab laboratory project (to be developed individually), chosen by the teacher among a set of three previously selected by the student (these are 3 among the projects developed in the Lab during the course). The second part is an evaluation of the critical and operational knowledge of the definitions, results and proofs presented during the course. The relative weight of the project and the theoretical examination are roughly 30% and 70%, respectively. In the project discussion the teacher will evaluate the exactness of the results and the comprehension of the practical/computational aspects of the adopted numerical method. During the theoretical part of the exam, the teacher will mainly evaluate the comprehension of the topic and the mathematical rigour in presenting the numerical methods and the associated proofs.

During the Covid-19 emergency period the exams will be handled remotely, by making use of the WebEx platform

and the E-learning page of the course (where also a public link for external audience will be provided).

Office hours

Flexible, arranged directly via email.