



UNIVERSITÀ  
DEGLI STUDI DI MILANO-BICOCCA

## SYLLABUS DEL CORSO

### Calcolo Numerico

2021-2-E3501Q064

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#### Aims

The aim of this course is to present the basic topics of Numerical Analysis, both from the theoretical and algorithmical point of view, that every Mathematician should know.

The learning outcomes are:

Knowledge:

- Knowledge and understanding of the fundamental techniques of Numerical Analysis, including theorems and proofs;
- Knowledge and understanding of the scientific problems related to numerical analysis.

Skills:

- \_\_\_\_\_
- \_\_\_\_\_
- \_\_\_\_\_
- Being able to present in a clear and precise way the theoretical results shown in the course and their practical applications.

#### Contents

The main topics are:

- Floating Point Arithmetic
- Numerical Linear Algebra: linear systems, eigenvalues computation
- Root-finding algorithms
- Polynomial Interpolation
- Least squares method and QR decomposition
- Quadrature Formulas

## Detailed program

- **Floating Point Arithmetic:** Representation of real numbers, Representable numbers, Approximation of real numbers on a computer, Floating point arithmetic, Rounding to even, Computation of elementary functions;
- **Gaussian elimination and the decomposition  $PA=LU$ :** Linear systems, Gaussian elimination, Decomposition  $PA=LU$ ;
- **Topics in linear algebra:** Scalar products and norms, Norms in  $\mathbb{R}^n$ , Matrix norms;
- **Stability of the Gaussian elimination:** Perturbation of a linear system, Application to the Gaussian elimination;
- **Cholesky decomposition:** Symmetric and positive definite matrices, Cholesky decomposition, Application to the solution of a linear system;
- **Iterative methods for linear systems:** Motivations, Iterative methods for systems of linear equations, Stopping criteria;
- **Eigenvalues:** Gershgorin circles, Perturbation analysis of eigenvalues, Power method;
- **Root-finding:** Bisection method, Newton methods and variations, Experimental measurement of the order of convergence, Brent method, MATLAB implementation;
- **Polynomial interpolation:** Weierstrass theorem, Interpolation, Analysis of interpolation algorithms, Conditioning, Interpolation of functions;
- **Splines;**
- **Least squares and QR factorization:** Overdetermined linear systems, Geometrical interpretation, QR decomposition, Linear regression, Using QR factorization to solve linear systems;
- **Quadrature formulas:** Interpolatory quadrature formulas, Trapezoidal rule, Simpson rule, Newton-Cotes formulas, Adaptive quadrature formulas.

## Prerequisites

First year courses *Analisi 1* and *Algebra Lineare e Geometria*.

## Teaching form

Lessons (8 CFU, 64 hours), exercise classes (4 CFU, 48 hours).

The course is taught in italian.

Due to the COVID-19 pandemic, lessons will be recorded and, if possibile, live-streamed. Exercise classes will be live-streamed and recorded.

## **Textbook and teaching resource**

Teacher's notes and recordings of the lectures are available on the web site of the course.

## **Semester**

1<sup>st</sup> semester.

## **Assessment method**

Practice test on the computer followed by oral examination. Final mark out of 30.

In the first part of the examination the student will be assigned a problem in numerical analysis to be solved on the computer using the MATLAB codes developed during the course.

The second part is a standard oral examination which requires the exposition of statements and proofs of the theorems, definitions, examples/counterexamples and computational techniques. The practice test will also be discussed.

In order to take the oral examination, the students need to pass the practice test with a mark of at least 18 out of 30. The final mark will take into account both tests.

The practice test and the oral examination must be taken in the same session (January-February, June-July, September).

Due to the COVID-19 pandemic, the whole examination will be conducted online.

## **Office hours**

On appointment (online via Webex).

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