

# UNIVERSITÀ DEGLI STUDI DI MILANO-BICOCCA

## SYLLABUS DEL CORSO

# Argomenti di Geometria e Topologia

2122-1-F4001Q083

#### **Aims**

The aim of the course is to take some classic topics in algebraic topology of simplicial complexes, introducing homology theory, cohomology theory and some aspects of homotopy theory, with some recent applications.

(Further verbose details in the Italian version.)

#### **Contents**

Simplicial complexes, homology and cohomology of polyhedra, triangulable manifolds, homotopy groups, applications to data analysis and dynamical systems.

## **Detailed program**

Fundamental concepts: topological spaces, connectedness, compactness, function spaces, general ideas on Categories, push-out diagrams. Euclidean and abstract simplicial complexes. Introduction to homological algebra. Homology with coefficients. Category of polyhedra. Cohomology of polyhedra. Cohomology ring, cap product. Triangulable manifolds. Surfaces and classification. Poincaré Duality. Fundamental group of polyhedra. Fundamental group and homology. Homotopy groups. Obstruction theory. Applications to: computational homology, persistent homology, data analysis and dynamical systems.

## **Prerequisites**

Basic topics covered in bachelor courses of geometry and algebra

## **Teaching form**

Lectures: 8 ECTS credits.

## Textbook and teaching resource

Ferrario, Piccinini, "Simplicial structures in topology". CMS Books in Mathematics, Springer, New York, 2011. xvi+243 pp. ISBN: 978-1-4419-7235-4

## Semester

1S

#### **Assessment method**

Oral examination on the topics covered in the course, with in-depth analyis and re-elaboration of them with a personal perspective. The date and the content of the seminar, which is part of the exam, have to be first discussed with the teacher.

## Office hours

By appointment, or Mondays 15:30.