



UNIVERSITÀ
DEGLI STUDI DI MILANO-BICOCCA

SYLLABUS DEL CORSO

Analisi Reale ed Equazioni Differenziali

2122-1-F4001Q076

Aims

According to the Mathematics Degree educational objectives, the course aim is the introduction to linear partial differential equations with hints to nonlinear ones. The skills needed to understand and analyse the most important techniques in the theory and the ability to solve exercises and problems will be provided.

Contents

Spectral theory for compact and selfadjoint operators. Elliptic equations: regularity, maximum principles, eigenvalues and eigenfunctions of the Laplacian. Transport equation and characteristics. Bochner's integral. Partial differential equations of parabolic type: fundamental solution of the heat equation, Galerkin's method, energy estimates and maximum principle.

Detailed program

Second order elliptic equations: regularity of weak solutions, weak and strong maximum principles.

Spectral theory: adjoint, selfadjoint, compact operators, spectrum. Spectrum of compact operators. Fredholm alternative. Spectral decomposition of selfadjoint compact operators. Eigenvalues and eigenfunctions of the Laplacian.

Transport equation: The method of characteristics.

Prerequisites

Main results in functional analysis, bounded linear operators in Banach spaces, weak topologies, spaces of continuous and Hölder continuous functions, L^p spaces, their duals and properties, Sobolev spaces and immersion theorems.

Teaching form

Lectures in classroom where definitions, results and relevant examples are illustrated (sometimes with relation to extra-mathematical applications as well).

Course delivered in Italian with the possibility of being delivered in English if foreign students request it.

Textbook and teaching resource

- A. Bressan. Hyperbolic systems of conservation laws: the one-dimensional Cauchy problem. Vol. 20. Oxford University Press on Demand, 2000.
- _____
- H. Brezis. Functional analysis, Sobolev spaces and partial differential equations. Springer Science and Business Media, 2010.
- L. C. Evans, Partial Differential Equations, AMS Graduate Studies in Mathematics, Vol.19. Second Edition, Providence 2010.
- D. Gilbarg, N. S. Trudinger, Elliptic partial differential equations of second order, Reprint of the 1998 edition. Classics in Mathematics. Springer-Verlag, Berlin, 2001.

Course webpage: <https://elearning.unimib.it/course/view.php?id=37745>

Semester

Second semester.

Assessment method

The exam consists of a written examination and an oral discussion.

The written examination consists in a short essay. The student is asked to develop two topics out of three proposed in two hours. The exposition must be precise, detailed, exhaustive and consistent with the chosen topics and must contain some of the most significant proofs. The ability to present a selection of significant proofs and, above all, the critical and operational knowledge of the definitions and results presented during the course, also by the illustration of examples and counter-examples are evaluated.

The oral discussion is held a few days after the written examination and consists in a short discussion and correction of the short essay. It verifies the mastery of the chosen topics. No other topics or proofs are asked outside of the two chosen topics.

Final grade out of thirty.

Office hours

By appointment.
