



UNIVERSITÀ  
DEGLI STUDI DI MILANO-BICOCCA

## COURSE SYLLABUS

### Large-Scale Graph Algorithms

2223-2-F1801Q162

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#### Aims

The course will present some efficient algorithms concerning fundamental problems in graph theory. Moreover, we will discuss some computational complexity aspects and the related algorithm design techniques, as well as techniques for implementing efficient (and heuristic) algorithms on large -scale graphs.

#### *Knowledge and understanding*

Student will learn how to represent standard graphs and large-dimension graphs, and they will learn some fundamental graph algorithms and heuristics techniques to tackle computational problems on small and large graphs.

#### *Applying knowledge and understanding*

At the end of the course, students will be able to model a real-world problem in terms of a graph problem, and to design specific algorithms to efficiently solve the problem.

#### Contents

Graph theory fundamentals. Computational problems on graphs. Computational complexity. Heuristic approaches on large-scale graphs.

#### Detailed program

- Graph: basic notions. Representation of graphs: adjacency lists, adjacency matrices. Efficient and succinct data structures for graph representation.

## *Graph problems*

1. Connected components, bi- and tri- connected components
2. Graph matching
3. Minimal cover, maximum clique, maximum independent set
4. Eulerian path, Hamiltonian path, and Travelling Salesman Problem (TSP)
5. Graph coloring
6. Graph isomorphism
7. Graph compression

## *Heuristic techniques and computational complexity*

1. Parametric complexity. Graph cover algorithms
2. SAT solvers
3. Kernighan-Lin algorithm
4. Simulated Annealing
5. Approximation complexity
6. Particle Swarm Optimization
7. Streaming Algorithms
8. Fine-grained complexity
9. Ant Colony

## **Prerequisites**

Theory of computation

## **Teaching form**

Lectures

## **Textbook and teaching resource**

The text we will be using is [Graph Algorithms](#), a collection of readings compiled from Wikipedia.

Lecture materials will not be distributed to the class; instead, you are encouraged to attend the lecture yourself and take your own notes.

## **Semester**

First semester

## Assessment method

The exam consists of an oral exam, with open-ended questions over all topics of the course.

The main criteria to evaluate the exam are correctness and completeness of the answers. Secondary criteria are the correct use of formal aspects and the ability to discuss how the answer is related to different course topics.

## Office hours

Office hours are online.

You can book a meeting at:

- <https://www.unimib.it/gianluca-della-vedova>
- [claudio.zandron@unimib.it](mailto:claudio.zandron@unimib.it)

## Sustainable Development Goals

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