UNIVERSITÀ
DEGLI STUDI DI MILANO-BICOCCA

COURSE SYLLABUS

Classical Mechanics

2324-2-E3001Q003

Aims

The content of the Course presents the basic ideas of Classical mechanics, from the Galileo-Newton formulation to those of Lagrange, Hamilton and Jacobi. The necessary mathematical tools for a proper comprehenson of these fundamental theories will be introduced and discussed.

The student, at the end of the course

1) will be able to provide mathematical models of physical phenomena of some complexity by means of the Lagrangian formalism, and understand their qualitative behaviour.

2) will be able to analyze them by using techniques of Analytical Mechanics and the theory of Dynamical Systems.

3) will be able to describe the motivations, the solution techniques and the mathematical apparatus lying beyond points 1) and 2) above.

Contents

Newtonian Mechanics (a reminder).

Second order differential equations. Qualitative analysis.

Lagrangian Mechanics.

Hamiltonian mechanics.

Detailed program

1) Space-time and events. Newton's principia and the dynamics of point masses.

2) Dynamical systems as mathematical models for physical phenomena. Basic aspects of the theory of second order Ordinary Differential Equations. Phase diagrams of conservative Newtonian systems in one dimension. The Lotka-Volterra system and Volterra’s laws. Compartmental models in epidemiology: the SIR model.

Bifurcation diagrams. Linearization of a dynamical system around an equilibrium point. Stability and the theorems of Lyapunov (statement).

3) Dynamics of systems of point masses.

4) Constraints, degrees of freedom, and free coordinates. The D'Alembert principle and Lagrangian Mechanics.

5) The Lagrangian and the Euler-Lagrange equations. Variational principles. Central motions and the Kepler problem. Lagrangian formulation of the Lorentz force. Theory of small oscillations. Further applications. Noether’s theorem. Basic notions of the theory of rigid bodies. Applications: rigid bodies in the plane. The Lagrange top.

6) Hamiltonian Mechanics: Hamilton equations and their variatiional formulation. Canonical transformations. Canonical contact (point) transformations. Poisson brackets and constants of the motion. Infinitesimal canonical transformations and Noether’s theorem in Hamiltonian Mechanics.

7) Liouville theorem on the conservation of volume in phase space. The Hamilton-Jacobi equation. Complete integrals. Introduction to the notion of separation of variables

Prerequisites

The content of the courses of Calculus I, Linear Algebra and Geometry, Physics I.

Teaching form

- Lectures (5 CFU)

- Classes (3 CFU)

Videorecordings of lectures and classes will be available online.

Textbook and teaching resource

References:

L.D. Landau, E.M. Lifshits, “Course of Theoretical Physics, Vol. I: Mechanics” (Pergamon)

H Goldstein, C. Poole, J. Safko, “Classical Mechanics”.

Lecture Notes available on the e-learning page.

Notes of (some of) the lectures, available on the e-learning page.

Semester

First semester

Assessment method

Written and oral examination. The written examination consists in the solution of significant problems in Dynamical Systems, Lagrangian Mechanics and Hamiltonian Mechanics.

Two partial written examinations concerning parts of the program will be held. The first one will be be at the beginning of November, the second one at mid-December. The written part of the examination must be completed in one of the final examination sessions within the July one. After that, students will be asked to solve the full set of problems. Should a student be absent at one of the ongoing partial examination, or in case of fail, he/she will be allowed to solve the corresponding problem in the occasion of his/her first final examination session (still within July).
The first partial written examination will propose a problem in the qualitative theory of dynamical systems in the plane. The second one will concern Lagrangian Mechanics. The written part of the eamination will be completed, in the sessions after the end of the lectures, by a problem in Hamiltonian Mechanics.

The oral examination consists in the discussion of the written part, as well as the discussion of fundamental topics of the course. Questions will be chosen (by the instructor) from a list to be given to the students at the end of the lectures.

The aim of the written examination is basically to assess the achievemnt of points 1) and 2) of the "Aims" Section. Its weight in terms of the final score, is 2/3.

The oral part mainly deals with point 3) of the "Aims" section.

Office hours

Meetings with individual students or small groups thereof are to be agreed via e-mail or the e-learning page.

Sustainable Development Goals

QUALITY EDUCATION