



UNIVERSITÀ  
DEGLI STUDI DI MILANO-BICOCCA

## SYLLABUS DEL CORSO

### Teoria e Fenomenologia delle Interazioni Fondamentali

2324-1-F1701Q128

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#### Aims

- Study of the theoretical aspects at the core of the Standard Model of Particle Physics (electroweak and strong sectors).
- Learning of techniques to compute cross-sections and decay widths.
- Deepening the knowledge of the phenomenology of fundamental interactions.

#### Contents

Introduction to the Standard Model of the electroweak and strong interactions: the  $SU(3) \times SU(2) \times U(1)$  model. Electroweak symmetry breaking, the Higgs boson, and the phenomenology of the strong and electroweak interactions.

#### Detailed program

##### Review of various topics:

- representations of the Lorentz group (in particular spinors and their transformation properties)
- Abelian gauge theories.
- Non-abelian gauge theories.
- kinematics and phase space (in 4 and in  $d$  dimensions)
- rules to compute cross sections and decay widths
- optical theorem

##### Lagrangian of the Standard Model:

- SU(N) algebra. Comments on SU(2) and SU(3).
- The electroweak sector of the Standard Model:
  - Experimental evidences
  - Spontaneous Symmetry Breaking, Higgs potential, masses of the W and Z vector bosons
  - Yukawa potential and masses of quarks and charged leptons; Cabibbo-Kobayashi-Maskawa (CKM) matrix, CP violation, unitary triangle
  - EW vertexes
  - various comments (Landau-Yang theorem, propagator of a massive vector boson and Breit-Wigner distribution,...)
- The strong sector (Quantum Chromodynamics - QCD)
  - Experimental evidences (quark model, naive parton model, need of colour: R-ratio, Delta++,...)
  - Lagrangian and vertexes of the strong sector
  - color algebra
  - Sum over polarizations ( $q\bar{q} \rightarrow \gamma\gamma$  vs  $q\bar{q} \rightarrow g g$ ), gauge choice
  - various comments (confinement,...)

### **Computation of cross sections and decay widths:**

- Z, W, H decay widths
- $e^+ e^- \rightarrow \mu^+ \mu^-$ : forward-backward asymmetry
- unitarity bounds: examples of unitarity violation in Fermi theory and in longitudinal vector boson scattering
- from LEP to Higgs phenomenology at the LHC

### **Review of the renormalization procedure:**

- The renormalization of the electromagnetic and of the strong coupling constant
- The renormalization scale and the  $\beta$ -function in QED and QCD
- The asymptotic freedom in QCD
- The renormalization group equations (+)

### **Electron-positron annihilation into hadrons at Next-to-Leading Order (NLO):**

- Preliminary analysis of potential divergences
- Computation of the Born term, and of the real and virtual contributions in dimensional regularization (+)
- Phase space
- Total cross section and cancellation of divergences (KLN theorem)

### **Final-state soft and collinear singularities:**

- Eikonal approximation and soft factorization
- Final state collinear factorization (FSR)
- Stermann-Weinberg jets as an example of an infrared-safe observable
- General properties of infrared-safe observables, brief discussion on event shapes

### **Hadrons in the initial state:**

- Deep-Inelastic Scattering (DIS) and structure functions, Bjorken scaling and the "naive" parton model
- Factorization theorem and partonic distribution functions (PDF)
- Initial-state soft and collinear singularities (ISR)
- Altarelli-Parisi splitting functions
- "Improved" parton model, factorization scale
- The Dokshitzer-Gribov-Lipatov-Altarelli-Parisi (DGLAP) evolution equations: interpretation and phenomenological consequences.

(+) = some of these topics might be skipped or discussed only briefly, depending on the time available and on the

students' interest.

Depending on the students' interest, some supplementar topics (not required for the exam) might be discussed, as for example:

- Neutrino masses, Pontecorvo-Maki-Nakagawa-Sakata (PMNS) matrix, Dirac and Majorana fermions
- Kinematics and phenomenology at hadron colliders
- Physics Beyond the Standard Model (BSM)

## Prerequisites

Basics knowledge of Quantum Field Theory.

Familiarity with basic techniques to compute amplitudes and cross sections for simple processes in QED (Dirac matrices, sum over polarizations and traces,...)

## Teaching form

Frontal lectures.

## Textbook and teaching resource

Notes and lectures can be found at the web page: <https://virgilio.mib.infn.it/~re>

### EW part: main references:

- C. Becchi and G. Ridolfi: *An Introduction to Relativistic Processes and the Standard Model of Electroweak Interactions*
- lecture notes / reviews (available on elearning and/or on the webpage of the lecturer)

### QCD part: main references:

- lectures by P. Nason, by M. Mangano and others (available on elearning and/or on the webpage of the lecturer)
- lecture notes from previous years course (available on elearning and/or on the webpage of the lecturer)

### Very useful textbooks:

- Peskin, Schroeder: *An Introduction To Quantum Field Theory*
- Schwartz: *Quantum Field Theory and the Standard Model*
- Ellis, Stirling, Webber: *QCD and collider Physics*
- Cheng, Li: *Gauge theory of elementary particle physics*
- Dissertori, Knowles, Schmelling: *Quantum Chromodynamics. High Energy Experiments and Theory*

### Other references:

- T. Muta: *Foundations of Quantum Chromodynamics*

- R. D. Field: *Applications of Perturbative QCD*

Exam sheets from previous years can be found here: <https://virgilio.mib.infn.it/~re>

## Semester

Second term.

## Assessment method

The exam consists of a written test, followed by an oral one. Normally the oral test takes place few days after the written one.

- Written test: exercises similar to those of previous years and of complexity similar to the cases discussed during lectures. In practice, the requirements are
  - being able to compute a cross section (or decay rate) in all its parts (going from the Feynman rules to the squared amplitude, compute the phase space, express the kinematics using relativistic invariants, e.g. Mandelstam variables)
  - being able to comment on the properties of the result obtained.
- Oral test: questions on the topics discussed during the course (possibly with a very quick discussion of the written test when needed).

During the academic year, there will be at least 5 exam sessions, typically in January, February, June, July, Spetember.

## Office hours

By appointment.

## Sustainable Development Goals

QUALITY EDUCATION

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