

$$\frac{d\phi}{dt} = \int_S \frac{\partial \underline{B}}{\partial t} \cdot d\underline{S} + \int_C \underline{B}(t) \cdot (\underline{\mu}_\perp \times d\underline{l})$$

$$\frac{\partial \underline{B}}{\partial t} = -\nabla \times \underline{E} \rightarrow \underline{E} + \underline{\mu}_\perp \times \underline{B} = 0 \text{ (caso ideale)}$$

resistività

$$\underline{E} + \underline{\mu}_\perp \times \underline{B} = \eta \underline{j}$$

$$\underline{E} = -\underline{\mu}_\perp \times \underline{B} + \eta \underline{j}$$

$$\frac{\partial \underline{B}}{\partial t} = -\underline{\nabla} \times \underline{E} = -\underline{\nabla} \times (\eta \underline{j} - \underline{u}_{\perp} \times \underline{B}) \quad (1)$$

$$\begin{aligned} \frac{d\Phi}{dt} &= \int_S \underline{\nabla} \times (-\eta \underline{j} + \underline{u}_{\perp} \times \underline{B}) \cdot d\underline{S} + \int_C \underline{B}(t) \cdot (d\underline{l} \times \underline{u}_{\perp}) \\ &= - \int_S \underline{\nabla} \times (\eta \underline{j}) \cdot d\underline{S} + \int_S \underline{\nabla} \times (\underline{u}_{\perp} \times \underline{B}) \cdot d\underline{S} + \int_C \underline{B}(t) \cdot (d\underline{l} \times \underline{u}_{\perp}) \end{aligned}$$

(2): The Ampere $\underline{\nabla} \times \underline{B} = \mu_0 \underline{j}$; $\underline{j} = \frac{1}{\mu_0} (\underline{\nabla} \times \underline{B})$ $\underline{\nabla} \times (\underline{\nabla} \times \underline{B}) =$
 $= \underline{\nabla} (\underline{\nabla} \cdot \underline{B}) - \nabla^2 \underline{B}$

(2), (1): $\frac{\partial \underline{B}}{\partial t} = -\frac{\eta}{\mu_0} \underline{\nabla} \times (\underline{\nabla} \times \underline{B}) + \underline{\nabla} \times (\underline{u}_{\perp} \times \underline{B}) = \frac{\eta}{\mu_0} \nabla^2 \underline{B} + \underline{\nabla} \times (\underline{u}_{\perp} \times \underline{B})$

SU ppaungo $u_{-1} = 0$

$$\frac{\partial \underline{B}}{\partial t} = \frac{\eta}{\mu_0} \nabla^2 \underline{B} \quad (\text{eq. di diffusione})$$

$$\frac{\underline{B}}{\tau} \approx \frac{\eta \underline{B}}{\mu_0 L^2} ; \quad \tau \approx \frac{\mu_0 L^2}{\eta}$$

Se $\eta \rightarrow 0$

$\tau \rightarrow +\infty$

$L \approx 1 \text{ m}$

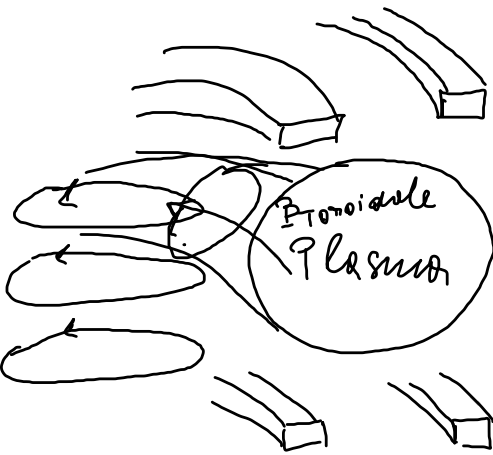
$$\sigma_{\text{Copper}} \approx 6 \cdot 10^7 \Omega^{-1} \text{ m}^{-1}$$

$$\eta = \frac{1}{\sigma_{\text{Copper}}} = 1.7 \cdot 10^{-8} \Omega \cdot \text{m}$$

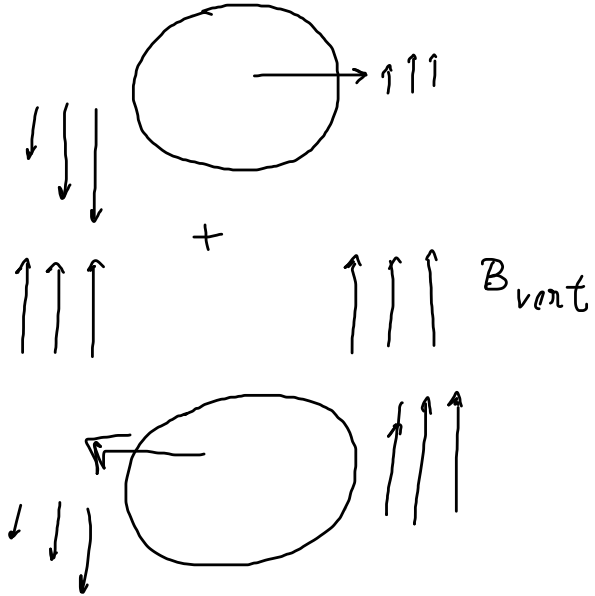
$$\tau \approx \frac{4 \cdot \pi \cdot 10^{-7}}{1.7 \cdot 10^{-8}} \approx 74 \text{ s} \approx \text{minuti}$$

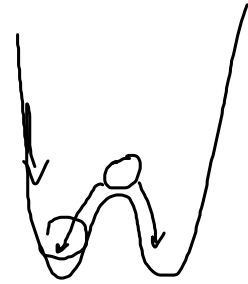
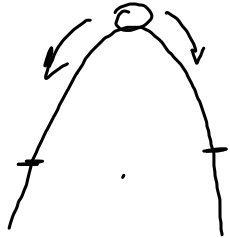
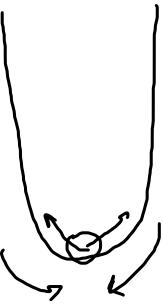
$$\frac{\tau_{\text{MHD}}}{\tau_{\text{Copper}}} \sim \frac{L}{\sqrt{\mu_0 \epsilon_0} T} \sim \mu\text{s}$$

$T \sim \text{keV}$



B_{vert}





Inst. ideali

rispettano la legge
di gelo

$$1) W^{fin} < W^{iniz.}$$

$W^{c.in}$

è accessibile

$$\tau \sim \mu s$$

rispett. la legge di gelo

$$2) W^{fin} < W^{iniz.}$$

violano la legge di gelo

non ideali

$$\tau \sim s$$

Inst. $\left\{ \begin{array}{l} \text{interne} : \text{near distributione locale} \\ \text{esterne} : \text{moto compl. del plasma} \end{array} \right.$
 (dette ^{es} di seg)



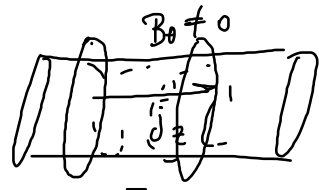
Inst. dovute alla corrente \parallel pressione
 = = pressione

limitano la corrente \parallel può scorrere

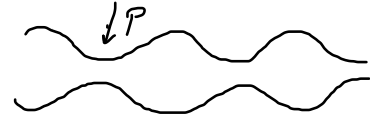
$$\nabla p = \mathbf{j} \times \mathbf{B}$$

↑
⊥

modo kink

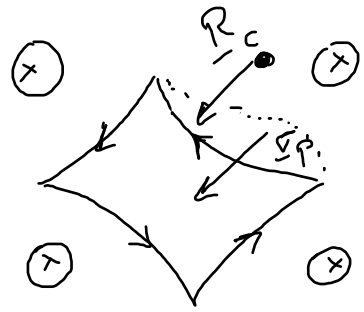


$\uparrow B_z \Rightarrow$ saen pinch

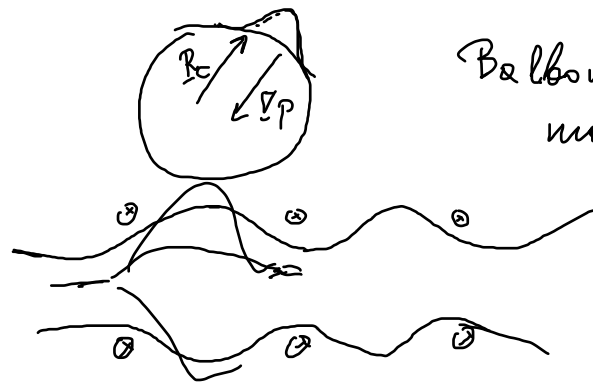


Regioni a curvatura favorevole e sfavorevole

Se $R_{-c} \parallel \nabla p$: curvatura è favorevole
 Se $R_{-c} \text{ anti} \parallel \nabla p$: = = sfavorevole



2 pinchi



Ballooning modes

$$f(x) \in \mathcal{L}_2 \left(-\frac{a}{2}, \frac{a}{2} \right) \quad \left[-\frac{a}{2}, \frac{a}{2} \right]$$

$$f(x) = \frac{a_0}{2} + \sum_{m=1}^{+\infty} \left[a_m \cos\left(\frac{2\pi m x}{a}\right) + b_m \sin\left(\frac{2\pi m x}{a}\right) \right] \quad m=1, 2, 3, \dots$$

$$a_m = \frac{2}{a} \int_{-\frac{a}{2}}^{\frac{a}{2}} f(x) \cos\left(\frac{2\pi m x}{a}\right) dx$$

$$b_m = \frac{2}{a} \int_{-\frac{a}{2}}^{\frac{a}{2}} f(x) \sin\left(\frac{2\pi m x}{a}\right) dx$$

$$k_m = \frac{2\pi m}{a}$$

$$\lambda = \frac{2\pi}{k_m} = \frac{a}{m}$$

$$k_m - k_{m-1} = \frac{2\pi}{a}$$

