



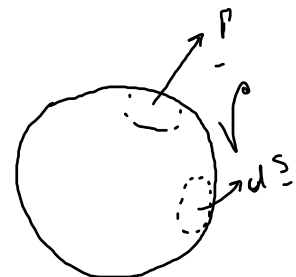
$$\Delta x \quad \Delta t$$

$$\langle x \rangle = 0$$

$$\langle x^2 \rangle \neq 0$$

$$\langle x^2 \rangle = N (\Delta x)^2 = t \frac{(\Delta x)^2}{\Delta t}$$

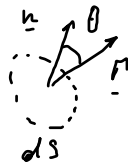
$$N = \frac{t}{\Delta t} \quad \sigma = \sqrt{\langle x^2 \rangle} \propto \sqrt{t}$$



$\vec{\Gamma}$ : flusso netto di particelle che entrano/escono dal volume  $V$

$$[\vec{\Gamma}]: \frac{\text{particelle}}{m^2 \cdot s}$$

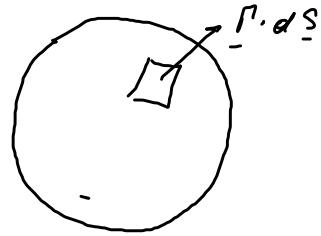
$$\vec{\Gamma} \cdot d\vec{S} = \Gamma dS \cos \theta$$



Se  $\vec{\Gamma} \cdot d\vec{S} > 0$ : particelle escono da  $dS$   
 Se  $\vec{\Gamma} \cdot d\vec{S} < 0$ : = entrano in  $dS$

Fisica 2:  $\vec{j} \cdot d\vec{S} = j \cdot dS$

$$\frac{dN}{dt} = - \int_{\text{Sup}} \vec{\Gamma} \cdot d\vec{S}$$



$\vec{\Gamma} \cdot d\vec{S} < 0$  se part. entrano  $\Rightarrow \frac{dN}{dt} > 0 \Rightarrow$  segno  $\ominus$

$$\int_{\text{Sup}} \vec{\Gamma} \cdot d\vec{S} = \int_V (\nabla \cdot \vec{\Gamma}) dV$$

$$N = \int_V n dV$$

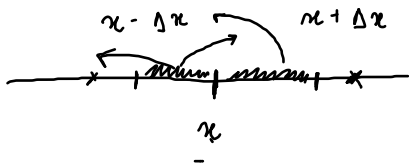
↑ densità di particelle  
(part/m<sup>3</sup>)

$$\frac{d}{dt} \int_V n dV = - \int_V (\nabla \cdot \vec{\Gamma}) dV$$

$$\int_V \frac{\partial n}{\partial t} dV = - \int_V (\nabla \cdot \vec{\Gamma}) dV$$

$$\int_V \left( \frac{\partial n}{\partial t} + \nabla \cdot \Gamma \right) dV = 0 \Rightarrow \nabla \text{ arbitrario } \frac{\partial n}{\partial t} + \nabla \cdot \Gamma = 0$$

Modello 1D per  $\Gamma$



Quante particelle attraversano  $n$ ?  
 $\frac{m^2 \cdot S}{\Gamma_+(n,t)}$

$$\Gamma(x,t) = \left[ \begin{array}{l} \text{part. che a } t-\Delta t \text{ si trovano in} \\ \left( \frac{m^2}{n}, x-\Delta x \right) \end{array} \right] \rightarrow \left[ \begin{array}{l} \text{part. che a } t-\Delta t \text{ si trovano} \\ \text{in } \left( \frac{m^2}{n}, x+\Delta x \right) \end{array} \right]$$

$$\begin{aligned} \Gamma(n,t) &= \Gamma_+(n,t) - \Gamma_-(n,t) = \int_{x-\Delta x}^{x+\Delta x} n(x') dx' - \int_x n(x') dx' \\ &= \frac{1}{2\Delta t} \int_{x-\Delta x}^{x+\Delta x} n(x') dx' - \frac{1}{2} \frac{1}{\Delta t} \int_x n(x') dx' \end{aligned}$$

$$\begin{aligned} n dV &= \# \text{ particelle } dV = S \cdot dx \\ \# \frac{\text{part.}}{m^2} &= \frac{n dV}{S} = n dx \end{aligned}$$

$$\Gamma_1(x) = \frac{1}{2\Delta t} \int_{x-\Delta x}^x n(x') dx' =$$

$$f(x) \approx f(x_0) + \left. \frac{df}{dx} \right|_{x=x_0} (x-x_0)$$

$$\therefore n(x') \approx n(x) + \left. \frac{dn}{dx'} \right|_x (x'-x)$$

$$= \frac{1}{2\Delta t} \int_{x-\Delta x}^x \left[ \underbrace{n(x)} + \left. \frac{dn}{dx'} \right|_x \underbrace{(x'-x)} \right] dx' =$$

$$= \frac{1}{2\Delta t} \left[ n(x) \int_{x-\Delta x}^x dx' + \left. \frac{dn}{dx'} \right|_{x'=x} \int_{x-\Delta x}^x (x'-x) dx' \right]$$

$$= \frac{1}{2\Delta t} \left[ n(x) [x-x+\Delta x] + \left. \frac{dn}{dx'} \right|_{x'=x} \frac{1}{2} (x'-x)^2 \right]_{x-\Delta x}^x =$$

$$= \frac{1}{2\Delta t} \left[ n(x) \Delta x - \frac{1}{2} (\Delta x)^2 \left. \frac{dn}{dx'} \right|_{x'=x} \right]$$

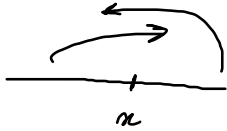
$$\begin{aligned}
 \Gamma_{-}(x) &= \frac{1}{2\Delta t} \left[ n(x) \int_x^{x+\Delta x} dx' + \frac{dn}{dx} \bigg|_{x'=x} \int_x^{x+\Delta x} (x'-x) dx' \right] \\
 &= \frac{1}{2\Delta t} \left[ n(x) \Delta x + \frac{dn}{dx} \bigg|_{x'=x} \frac{1}{2} (x'-x)^2 \bigg|_x^{x+\Delta x} \right] \\
 &= \frac{1}{2\Delta t} \left[ n(x) \Delta x + \frac{dn}{dx} \bigg|_{x'=x} \frac{(\Delta x)^2}{2} \right]
 \end{aligned}$$

$$\Gamma_{+}(x) = \frac{1}{2\Delta t} \left[ n(x) \Delta x - \frac{dn}{dx} \bigg|_{x'=x} \frac{(\Delta x)^2}{2} \right]$$

$$\Gamma = \Gamma_{+} - \Gamma_{-} = -\frac{1}{2\Delta t} \frac{dn}{dx} (\Delta x)^2 = -D \frac{dn}{dx}$$

$D = \text{coefficiente di diffusione}$   
 $= \frac{(\Delta x)^2}{2\Delta t}$

$$\frac{\partial n}{\partial t} + \underbrace{\frac{d}{dx} \Gamma}_{\nabla \cdot \Gamma} = 0$$



$$\frac{\partial n}{\partial t} = - \frac{d\Gamma}{dx} = + \frac{d}{dx} \left( D \frac{dn}{dx} \right)$$

$$\Gamma = -D \frac{dn}{dx}$$

$$\Gamma = -D \frac{dn}{dx}$$

Flusso netto solo se  $\frac{dn}{dx} \neq 0$

Flusso solo se c'è sbilanciamento tra particelle a  $DX$  e  $5X \Rightarrow \frac{dn}{dx} \neq 0$



n non è una costante

$$\frac{\partial n}{\partial t} = \nabla \cdot (D \nabla n)$$

$$\frac{a}{\tau} \approx \frac{D}{a^2} a ; \quad \tau \approx \frac{a^2}{D}$$

Se  $D \neq 0$ , allora  $\tau \neq 0$

Se  $D \rightarrow 0$ , allora  $\tau \rightarrow +\infty$

$\tau$ : tempo configurazione delle particelle

$$\tau_E \approx \frac{r^2}{\chi}$$

$\chi \rightarrow$  coefficiente di diffusione energia  $[\chi] = [D] = \frac{m^2}{s}$

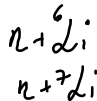
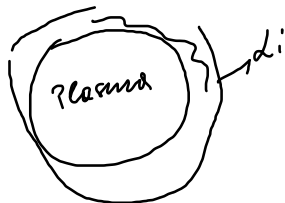
$d + t \rightarrow \alpha + tritium$

$\downarrow$

$E_n \approx 14 \text{ keV}$

$E_\alpha \approx 3.5 \text{ MeV}$   
 $T_e \approx T_i \approx 10-20 \text{ keV}$

$\tau_d > \tau_{SL}$   
 slowing down



$$D \sim \frac{(\Delta x)^2}{\Delta t}$$

Caso  $B=0$

$\omega = (\Delta t)^{-1}$

$\uparrow$   $\omega_{eq}$  collisionale

$\Delta x \sim \lambda_{mfp}$  (libero cammino medio)

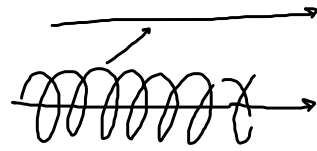
$$\lambda_{mfp} \approx v_{th} \cdot \Delta t \sim v_{th} \nu^{-1}$$

$$D \sim v_{th}^2 \nu^{-2} \cdot \nu \sim v_{th}^2 \nu^{-1} \sim \frac{T}{m \nu}$$

Caso  $B \neq 0$

$$\Delta n \sim \pi_L$$

$$D \sim \frac{(\Delta n)^2}{\Delta t} \sim \pi_L^2 \nu$$



$D \propto \nu$