

New periodic motion:
that of the T.P.

Confined particles

$$\int \underline{v}_{\parallel} ds$$

$$|\underline{\nabla}|B|| \propto \hat{e}_{\perp z}$$

Curvature $\propto \hat{e}_{\perp r}$

$$\underline{v}_{\perp 0} = -\mu \frac{|\underline{\nabla}|B|| \times \underline{B}}{qB^2} \propto \hat{e}_{\perp \theta}$$

$$\underline{v}_{\text{center}} = \frac{-(\hat{b} \cdot \dot{\hat{r}}) \hat{b} m \underline{v}_{\parallel}^2 \times \underline{B}}{qB^2} \propto \hat{e}_{\perp \theta}$$

$$\langle \underline{v} \rangle = \frac{1}{T_{\text{bounce}}} \int_0^{T_h} \underline{v} dt$$

$$\frac{\int m \langle \underline{v} \rangle \cdot d\underline{\pi}_{\text{bounce}}}{\int q \underline{A} \cdot d\underline{\pi}_{\text{bounce}}}$$

$$\frac{\frac{m}{qB} (\frac{v_{\parallel}^2}{2} + v_{\perp}^2) \cdot \pi}{q \phi(B)} \approx \frac{m v_{\perp}^2}{qB \pi \pi^2}$$

$$|\underline{v}_{\text{center}}| \approx \frac{m v_{\perp}^2}{\pi} \frac{B}{qB^2} \approx \frac{m v_{\perp}^2}{qB\pi}$$



$$\underline{J}_3 = \int (m \langle \underline{v} \rangle + q \underline{A}) \cdot d\underline{\pi}_{\text{bounce}}$$

$$\underline{B} = \nabla \times \underline{A}$$

Stokes th.

$$\int \underline{B} \cdot d\underline{S} = \int (\nabla \times \underline{A}) \cdot d\underline{S} = \oint \underline{A} \cdot d\underline{l}$$

$$\langle \underline{v} \rangle = \underline{v}_{\perp/B} + \underline{v}_{\text{center}}$$

$$\underline{v}_{\perp/B} = -\mu \frac{\nabla |B| \times B}{|B|} \quad \underline{v}_{\text{center}} \approx -\frac{m v_{\perp}^2}{\pi} \frac{\hat{n} \times \underline{B}}{qB^2}$$

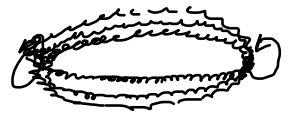
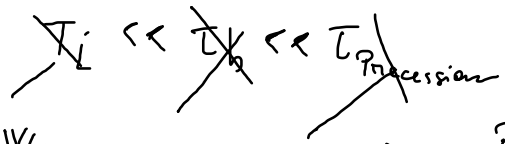
$$|\underline{v}_{\perp/B}| \approx \frac{m v_{\perp}^2}{2B} \frac{B \cdot B}{\pi} \frac{1}{qB^2} \approx \frac{m v_{\perp}^2}{2qB\pi}$$

$$\frac{\int m \langle \underline{v} \rangle \cdot d^3 \pi_{\text{bounce}}}{\int q \underline{A} \cdot d^3 \pi_{\text{bounce}}} \approx \frac{\left(\frac{m v}{q B}\right)^2}{\pi r^2} \approx \left(\frac{r_L}{r}\right)^2 \ll 1$$

size of T.P. orbit

$$y_3 = \int (m \underline{v} \cdot \underline{A} + q \underline{A} \cdot \underline{A}) d^3 \pi_{\text{bounce}} \approx \int q \underline{A} \cdot d^3 \pi_{\text{bounce}} = q \cdot \underbrace{\phi(B)}_{\text{orbit}}$$

- μ : T_L
- y_2 : T_b
- y_3 : $\tau_{\text{precession}}$



Waves

$$m = m_p = 1.67 \cdot 10^{-27} \text{ kg}$$

$$B = 1 \text{ T}$$

$$\omega_L = \frac{q B}{m}$$

$$T_L = \frac{2\pi}{\omega_L} = \frac{2\pi m}{q B}$$

$$T_L \approx \frac{6 \cdot 10^{-27} \cdot 1.67}{1.6 \cdot 10^{-19}} \approx 10^{-7} \text{ s} \approx 0.1 \mu\text{s}$$

Electrons

$$T_L \approx m$$

$$\frac{m_e}{m_p} \approx \frac{1}{2000}$$

$$T_{L,e} \approx 0.1 \text{ ns}$$

T_{bounce}

$$\sim \frac{\text{size system}}$$

kinemal speed

$$\sim \frac{\text{few m}}{10^6 \text{ m/s}} \approx \text{few } \mu\text{s}$$

$$10^6 \text{ m/s}$$

$$T \sim \text{keV}$$

$$m = m_p$$

$$\left. \begin{array}{l} T \sim \text{keV} \\ m = m_p \end{array} \right\} v_{th} \approx 10^6 \text{ m/s}$$

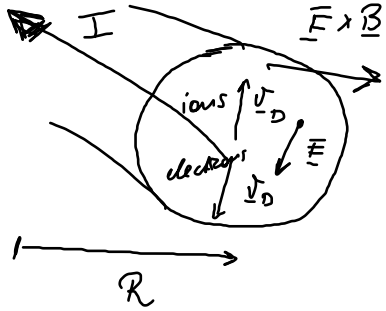
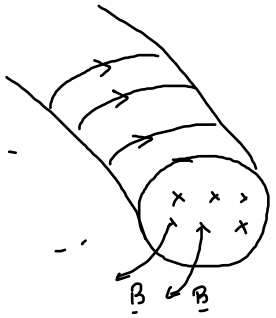
$T_{\text{precession}}$

$$\sim \text{few } T_{\text{bounce}}$$

T_{bounce}

$$\sim$$

same tens of μs



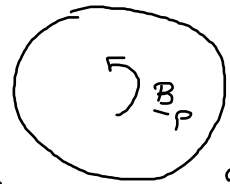
$$B = \frac{B_0 R_0}{R}$$

$$v_D = \frac{F \times B}{B^2}$$

$$B = \frac{k}{R}$$

at center $k = B_0 R_0$

$$\Rightarrow B = \frac{B_0 R_0}{R}$$



Equilibrium :

$$\nabla p = j \times B$$

Ideal

MHD eq. for eq.

pressure \uparrow
current density \uparrow
 $j \parallel B \parallel p_{const}$





$i = \frac{d}{r}$
 Rotational
 transform

$$\frac{i}{2\pi}$$

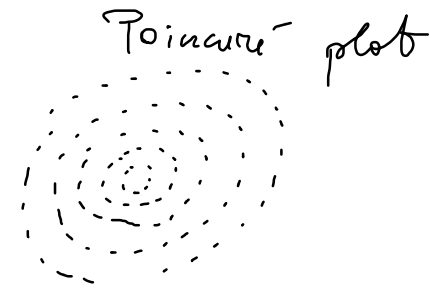
$$\frac{i}{2\pi}$$

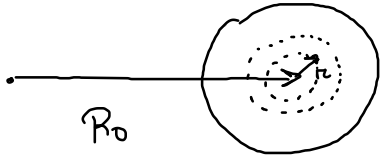
is a rational number
 = (not) = = =



$$\frac{1}{2\pi} = \frac{1}{3}$$

$$\frac{2}{3}$$



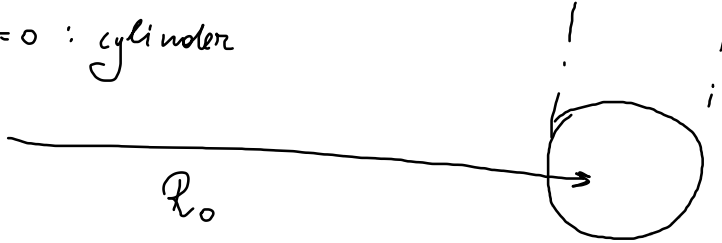


$$\frac{r}{R_0} = \epsilon$$

$\frac{R_0}{r}$ = aspect ratio

Typically $\frac{R_0}{r} \gg 1$; $\epsilon \ll 1$

When $\epsilon = 0$: cylinder

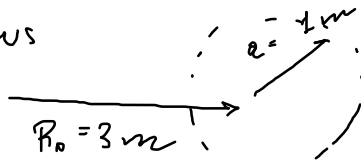


$R_0 \rightarrow +\infty$ cylinder

$$\frac{r}{R_0} \rightarrow 0$$

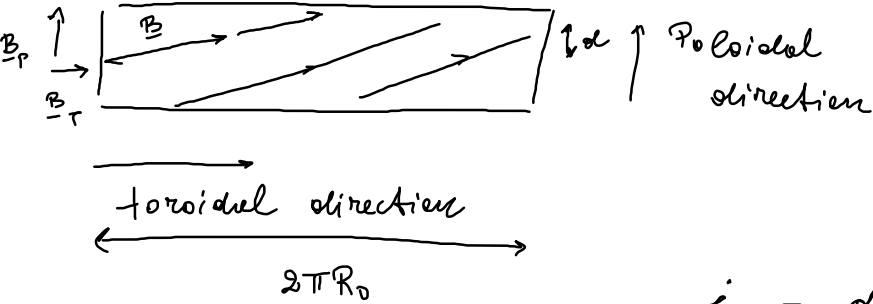
$\epsilon \ll 1$: cylindrical approx

Joint European Torus



$$\frac{a}{R_0} = \frac{1}{3}$$

most outer surface



$$\frac{B_p}{B_T} = \frac{d}{2\pi R_0} \Rightarrow d = 2\pi R_0 \frac{B_p}{B_T}$$

Safety factor

$$q = \frac{2\pi}{i} = \frac{r B_T}{R_0 B_p}$$

$$i = \frac{d}{r} = \frac{2\pi R_0 B_p}{r B_T}$$

Stability considerations

$$\frac{B_T}{B_p} = \frac{R_0}{r} \cdot q \gg 1$$

$$\Rightarrow B_T \gg B_p$$

centre edge

$1 \lesssim q < \text{some units}$
3, 4

$B_T \sim \text{some } T$

$B_p \sim \text{fraction of } T$