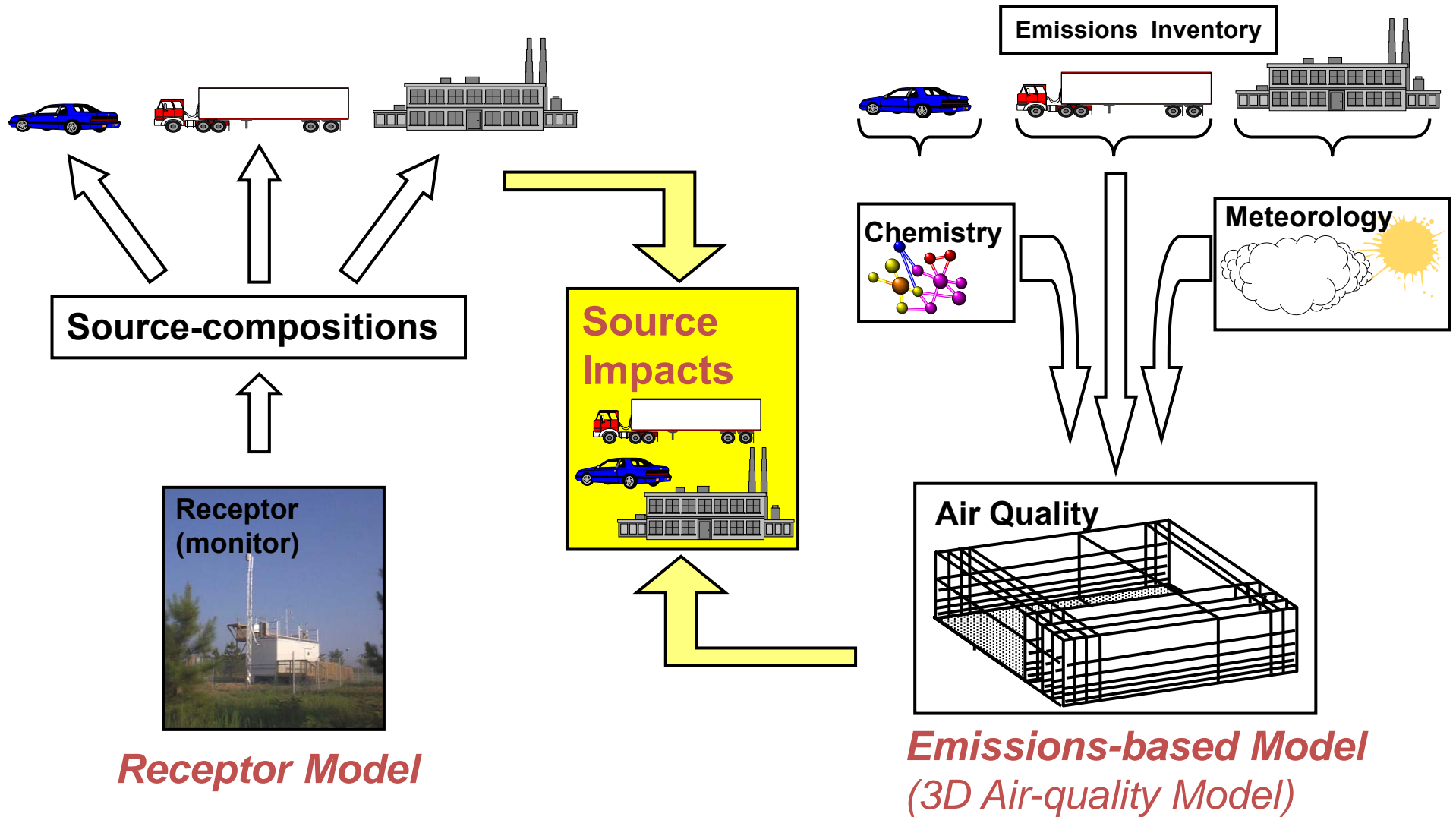


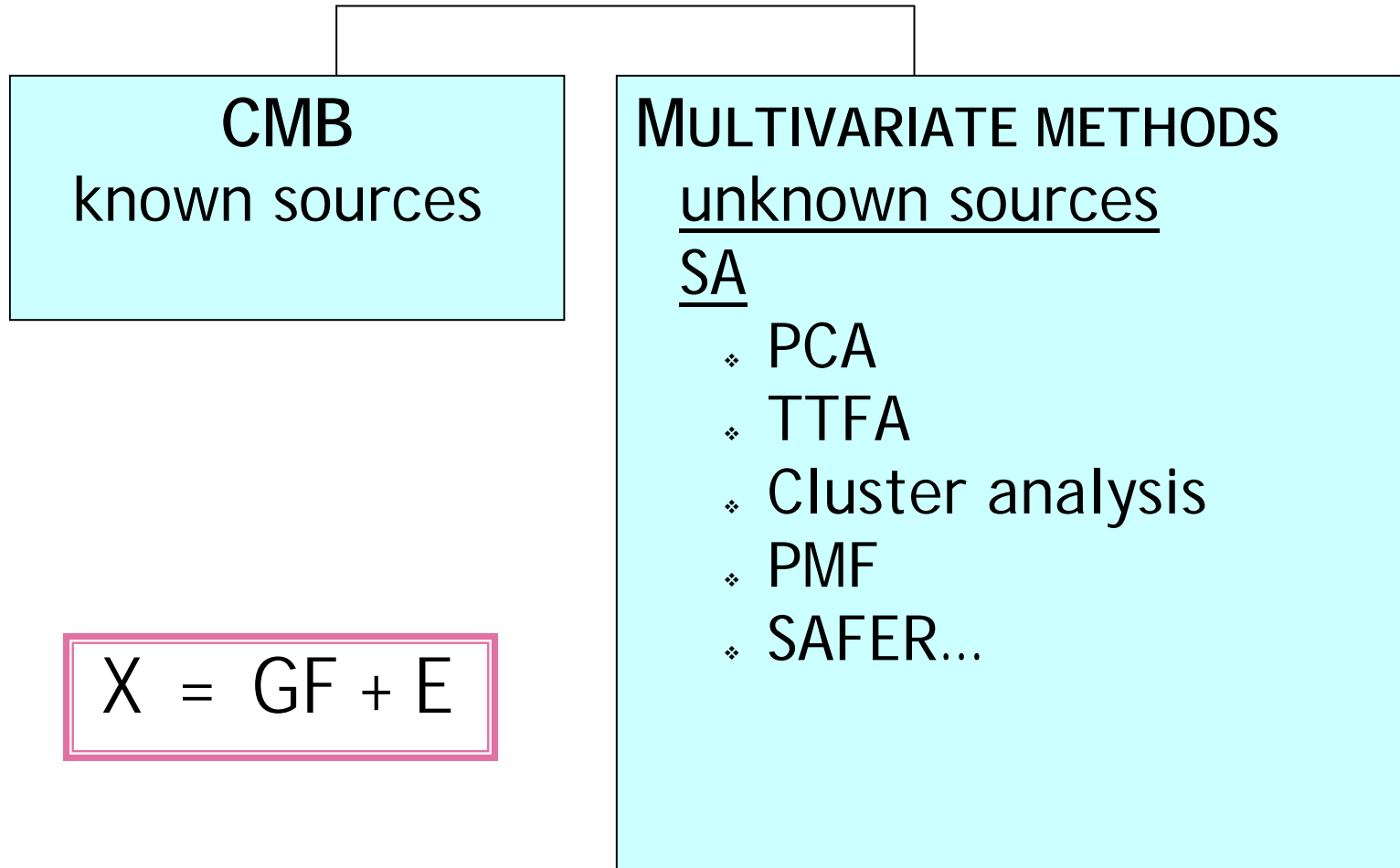
# Receptor vs. Emissions-Based Models



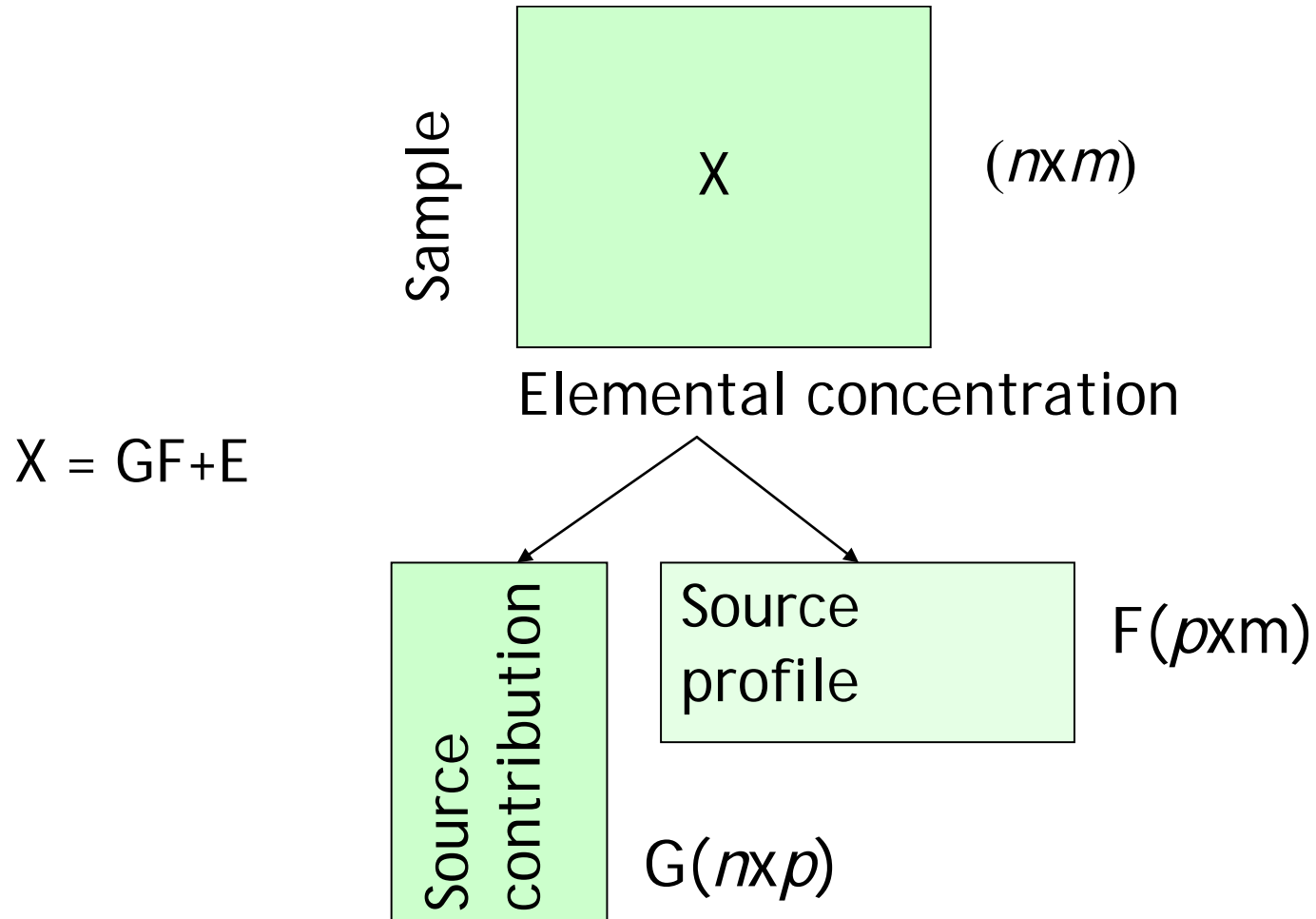
*Source oriented*: date le caratteristiche della sorgente e i dati meteorologici, stima della concentrazione degli inquinanti nei siti recettore

*Receptor oriented*: date le misure delle concentrazioni degli inquinanti nel sito recettore, stima del contributo delle differenti sorgenti e *source apportionment*

# Receptor Models



# Receptor Model



## THERE ARE THREE MAIN GROUPS OF SOURCE APPORTIONMENT TECHNIQUES

(a) Methods based on the evaluation of monitoring data. Basic numerical data treatment is used to identify sources.

Examples are:

- (1) correlation of wind direction with levels of measured components to identify source locations;
- (2) the correlation of gaseous pollutants with PM components to identify source associations;
- (3) subtraction of levels measured at regional background from those obtained at urban background and/or roadside levels to identify the contributions from the regional background, the city background and the monitored street;
- (4) quantification of natural PM contributions (e.g., African dust) by subtracting PM levels at regional background sites from those at urban background locations for specific days.

The main advantage is the simplicity of the methods and the consequent low impact of mathematical artefacts due to data treatment.

(b) Methods based on emission inventories and/or dispersion models to simulate aerosol emission, formation, transport and deposition. These models require detailed emission inventories that are not always available, and they are limited by the accuracy of emission inventories, especially when natural emissions are important. A significant advantage of these methods is that they may be used in scenario studies to evaluate the impact of emission abatement strategies on the anthropogenic contribution to ambient PM concentrations.

(c) Methods based on the statistical evaluation of PM chemical data acquired at receptor sites (receptor models). The fundamental principle of receptor modelling is that mass and species conservation can be assumed and a mass balance analysis can be used to identify and apportion sources of airborne PM in the atmosphere.

# OVERVIEW OF THE WIDE RANGE OF STATISTICAL MODELS AND MODELLING APPROACHES WHICH ARE CURRENTLY AVAILABLE IN THE LITERATURE.

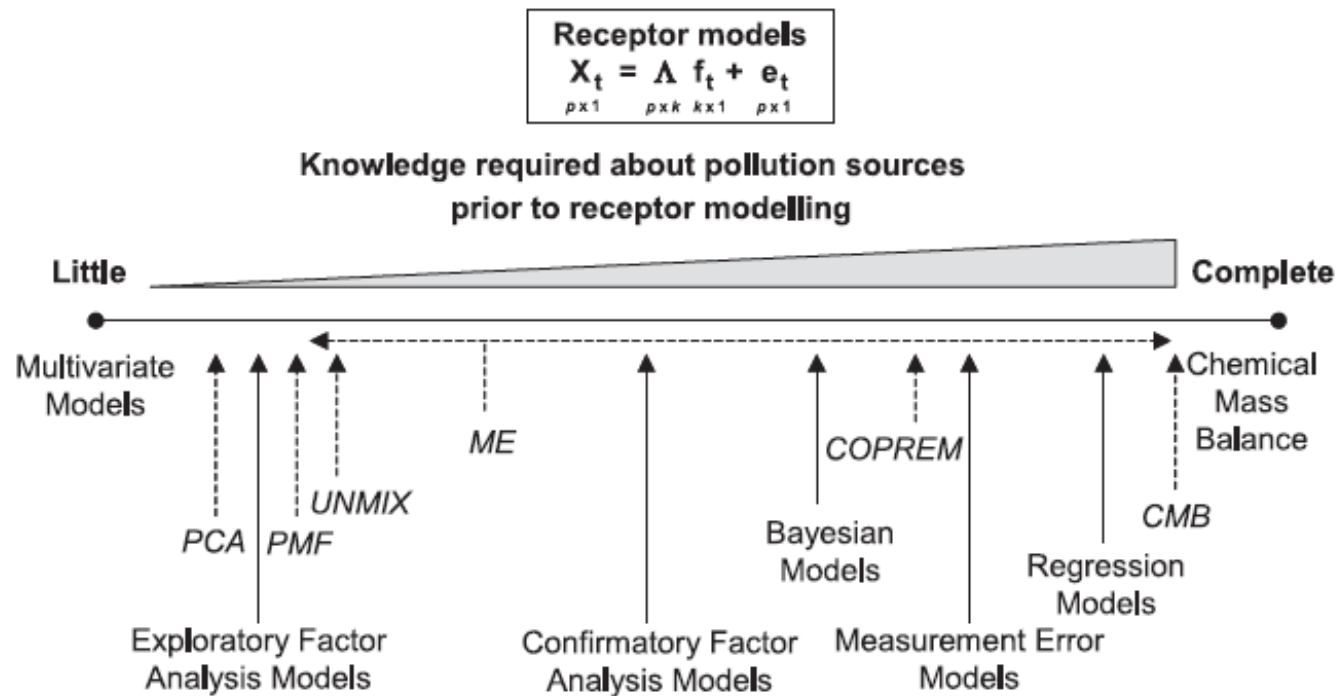
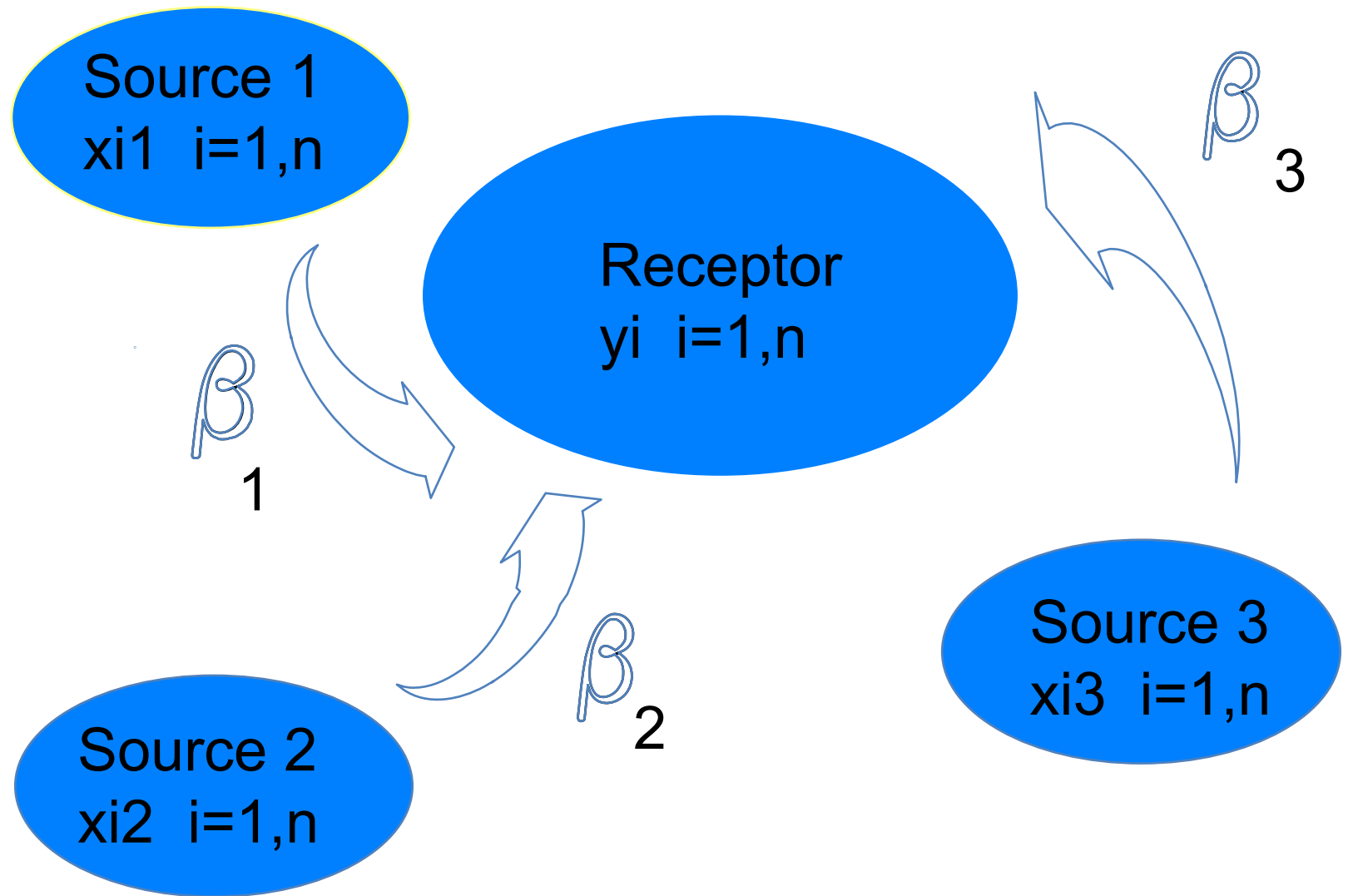


Fig. 1. Approaches for estimating pollution source contributions using receptor models (modified from Schauer et al., 2006). Specific models are shown in italics and with dotted arrows.

# Chemical Mass Balance Receptor Modelling

---





# PARTICULATE MATTER

European standard for the environmental air quality and for a cleaner air in Europe (2008/50/CE)

Standard limits for **PM<sub>10</sub>**:

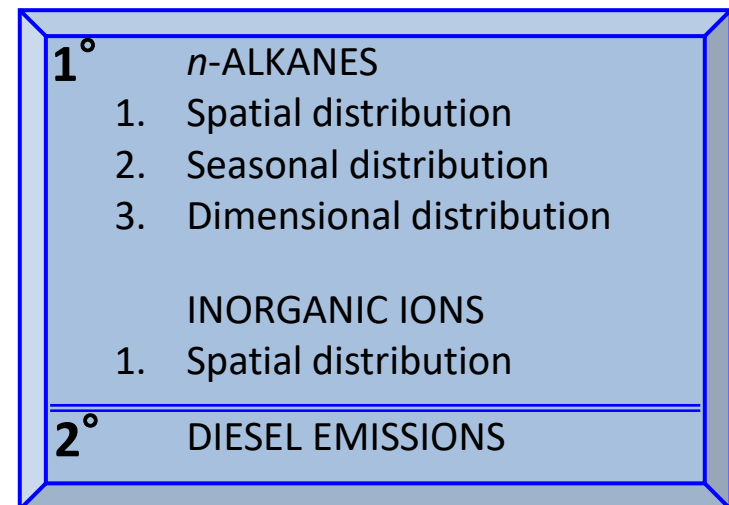
- 40  $\mu\text{g}/\text{m}^3$  as yearly average
- 50  $\mu\text{g}/\text{m}^3$  as daily average (not to be exceeded more than 35 times a year)

PM<sub>10</sub> concentrations to reduce within 2010 (1999/30/EG and 96/62/EG)

1° STEP: actual situation of **PM<sub>10</sub>** in the Lombardy Region

2° STEP: sources of PM<sub>10</sub> in the Lombardy Region

PM SOURCE IDENTIFICATION is a need



# PM SAMPLING

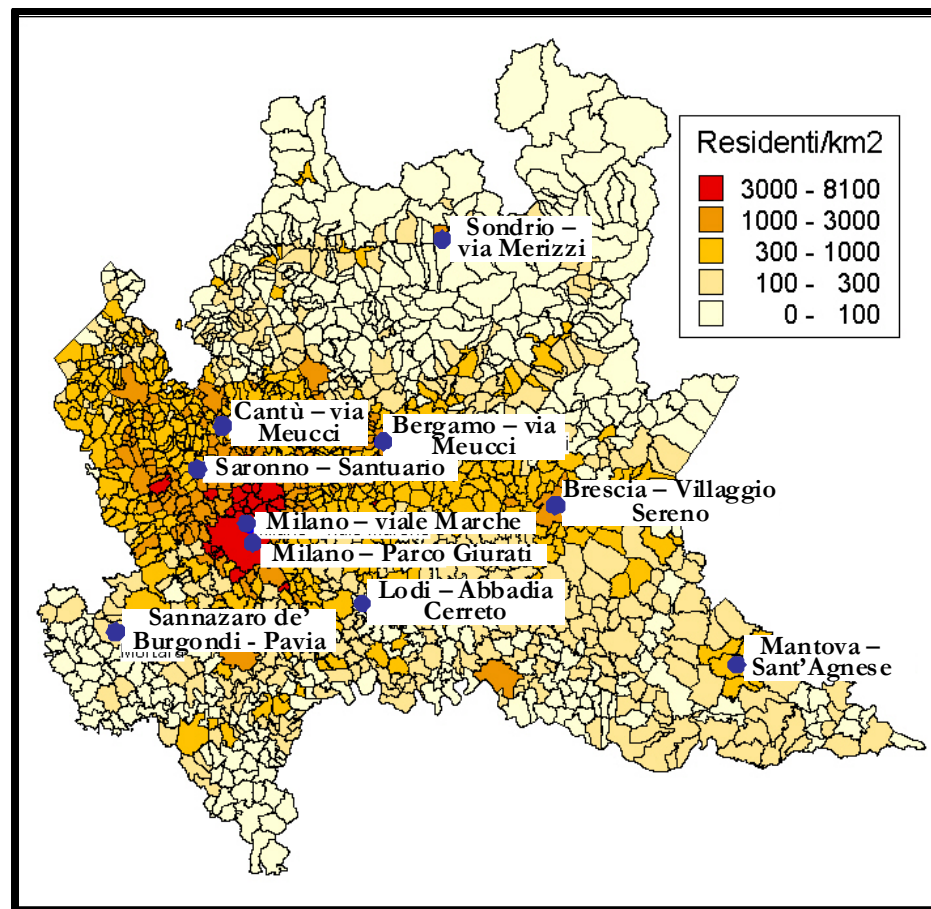
Ten sites of the Lombardy Region, from urban background to regional (pre-alpine) air quality.

- ❑ Low volume sampler, dual channel, Hydra (FAI Instruments); PM<sub>10</sub> inlet cut
- ❑ 24h sampling (0:00 to 24:00)
- ❑ Total volume = 27 - 55 m<sup>3</sup>
- ❑ PTFE filters, diameter of 47 mm

Sampling during **winter (feb-mar) 2007**;  
14 < n < 18 for a single site.

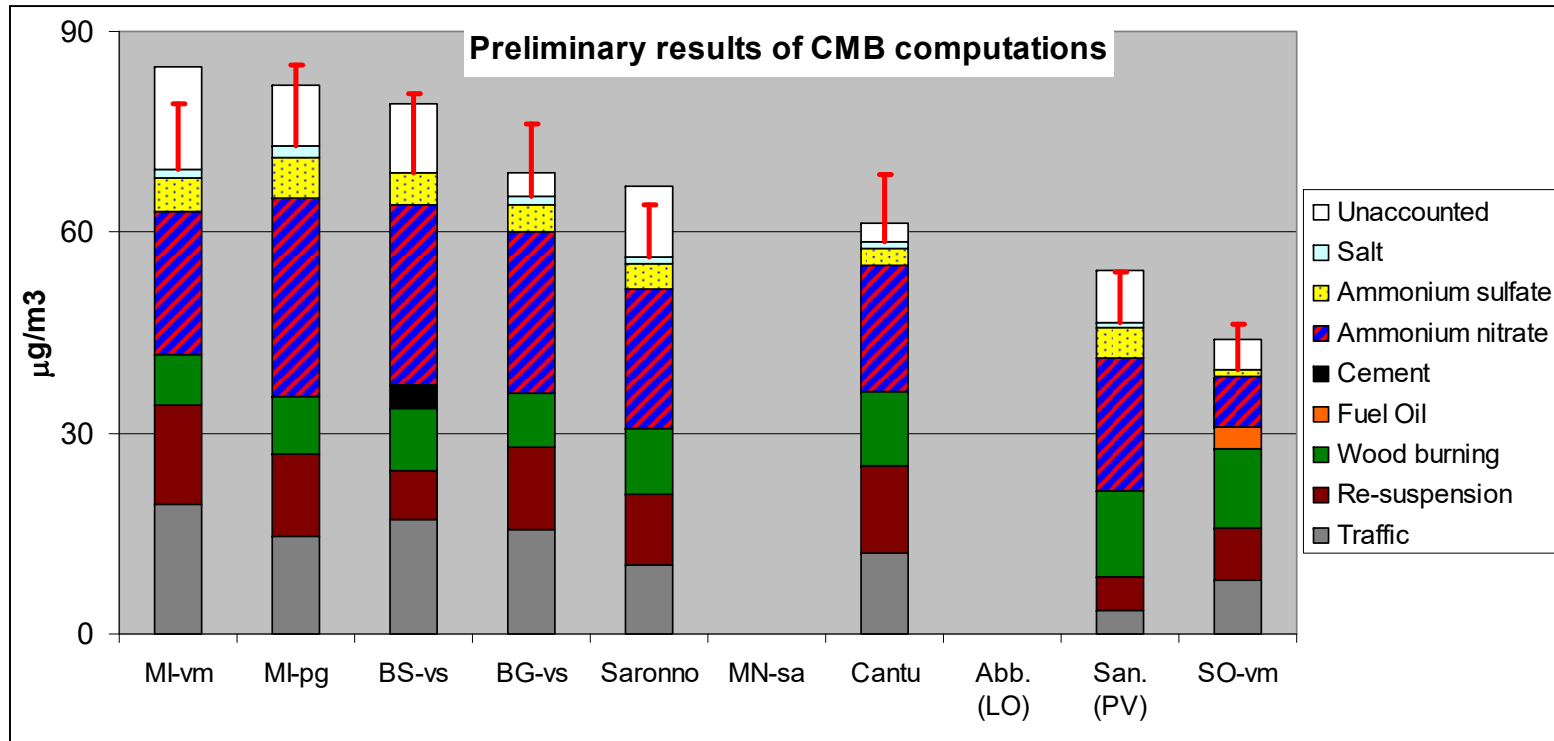
## ANALYSIS:

- inorganic ions
- elemental and inorganic carbon
- levoglucosan
- polycyclic aromatic hydrocarbons
- trace elements
- linear alkanes (not included)



**SOURCE APPORTIONMENT  
(Chemical Mass Balance)**

# PM SOURCE APPORTIONMENT



1. SECONDARY AEROSOL  $[\text{NH}_4\text{NO}_3 + (\text{NH}_4)_2\text{SO}_4] = 30\text{-}45\%$
2. TRAFFIC+RESUSPENSION = 31-41%
3. WOOD BURNING = 10-27%

# Chemical Mass Balance Receptor Modelling

$$y_i = \beta_1 x_{i1} + \beta_2 x_{i2} + \beta_3 x_{i3} + \dots + \varepsilon_i$$

$y_i$  : relative abundance of component  $i$  at the receptor

$x_{i1}$  : relative abundance of component  $i$  at source 1

$\beta_1$  : fractional contribution of source 1

$\varepsilon_i$  : the difference (error) between measured ( $y_i$ ) and

modelled ( $\sum_j \beta_j x_{ij}$ ) relative abundances of component  $i$

# Chemical Mass Balance Receptor Modelling

$$y_i = \beta_1 x_{i1} + \beta_2 x_{i2} + \beta_3 x_{i3} + \dots + \varepsilon_i$$

minimize the sum of the square of the errors :

$$\sum_i \varepsilon_i^2 = \sum_i \left( y_i - \sum_j \beta_j x_{ij} \right)^2$$

by adjusting the fractional contributions  $\beta_j$

Discrepancy in the total mass balance :

$$1 - \sum_j \beta_j$$

# Chemical Mass Balance Receptor Modelling Simple Spreadsheet Implementation

- Electronic spreadsheets like Excel make it easy to implement the model in the above form.
- The “Solver” function in Excel enables the minimization operation.
- Graphical tools in Excel enable qualitative assessment of model fit and the inputs.

Microsoft Excel - cmbssi.xls

File Edit View Insert Format Tools Data Window Help

H18 =

	A	B	C	D	E	F	G	H	I	J	K	
1	<b>Chemical Mass Balance Receptor Modelling: Simple Spreadsheet Implementation</b>											
2												
3		<b>Measured relative abundances</b>						<b>Model</b>	<b>error ^2</b>			
4												
5	<b>Components</b>	<b>Receptor</b>	<b>Source 1</b>	<b>Source 2</b>	<b>Source 3</b>							
6	<b>Comp 1</b>	0.18	0.001	0.043	0.186		0.156	0.001				
7	<b>Comp 2</b>	0.13	0.004	0.955	0.037		0.134	0.000				
8	<b>Comp 3</b>	0.09	0.028	0.002	0.039		0.032	0.003				
9	<b>Comp 4</b>	0.16	0.153	0.000	0.143		0.116	0.002				
10	<b>Comp 5</b>	0.20	0.349	0.000	0.301		0.245	0.002				
11	<b>Comp 6</b>	0.08	0.131	0.000	0.093		0.075	0.000				
12	<b>Comp 7</b>	0.02	0.042	0.000	0.030		0.024	0.000				
13	<b>Comp 8</b>	0.06	0.136	0.000	0.085		0.069	0.000				
14	<b>Comp 9</b>	0.04	0.085	0.000	0.049		0.040	0.000				
15	<b>Comp 10</b>	0.03	0.071	0.000	0.038		0.031	0.000				
16	<b>Total</b>	1.00	1.00	1.00	1.00		0.92	0.008 <b>SSE</b>				
17												
18		<b>coefficients:</b>	0.000	0.109	0.813							
19												

Profile normalization Model implementation

Draw AutoShapes

Ready

Start Eudora Light - [In] Welcome To Pr... CV\_Henri1.doc ... Microsoft Powe... cmbssi.xls ssicmb7.xls EN 11:41 AM

J16 =SUM(J6:J15)

## Chemical Mass Balance Receptor Modelling: Simple Spreadsheet Implementation

Components	Measured relative abundances				Model	error ^2
	Receptor	Source 1	Source 2	Source 3		
Comp 1	0.18	0.001	0.043	0.186	0.156	0.001
Comp 2					0.134	0.000
Comp 3					0.032	0.003
Comp 4					0.116	0.002
Comp 5					0.245	0.002
Comp 6					0.075	0.000
Comp 7					0.024	0.000
Comp 8					0.069	0.000
Comp 9					0.040	0.000
Comp 10	0.03	0.071	0.000	0.038	0.031	0.000
<b>Total</b>	1.00	1.00	1.00	1.00	0.92	0.008
<b>coefficients:</b>		0.000	0.109	0.813		

**Solver Parameters**

Set Target Cell:  Solve

Equal To:  Max  Min  Value of:  Close

By Changing Cells:  Guess

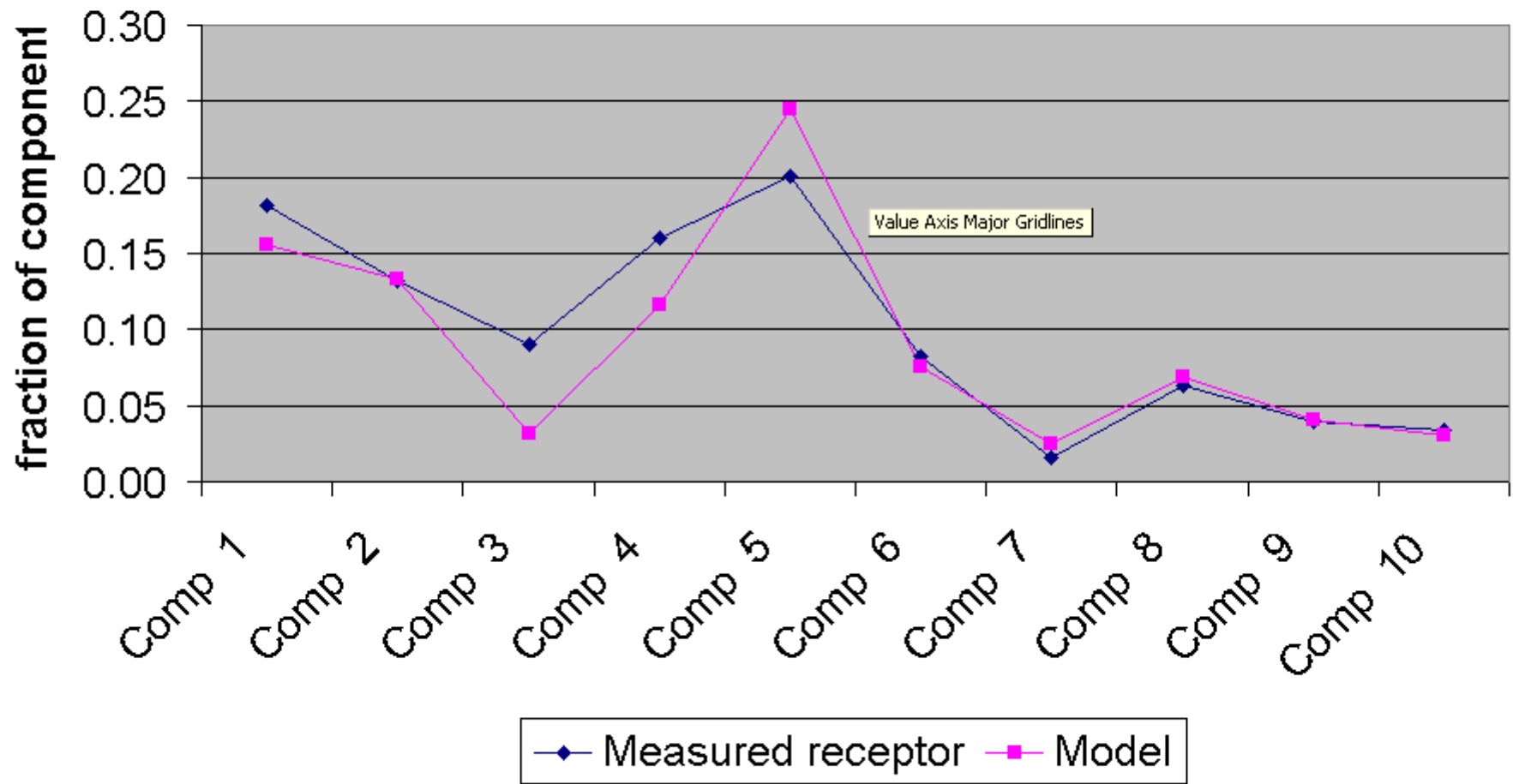
Subject to the Constraints:

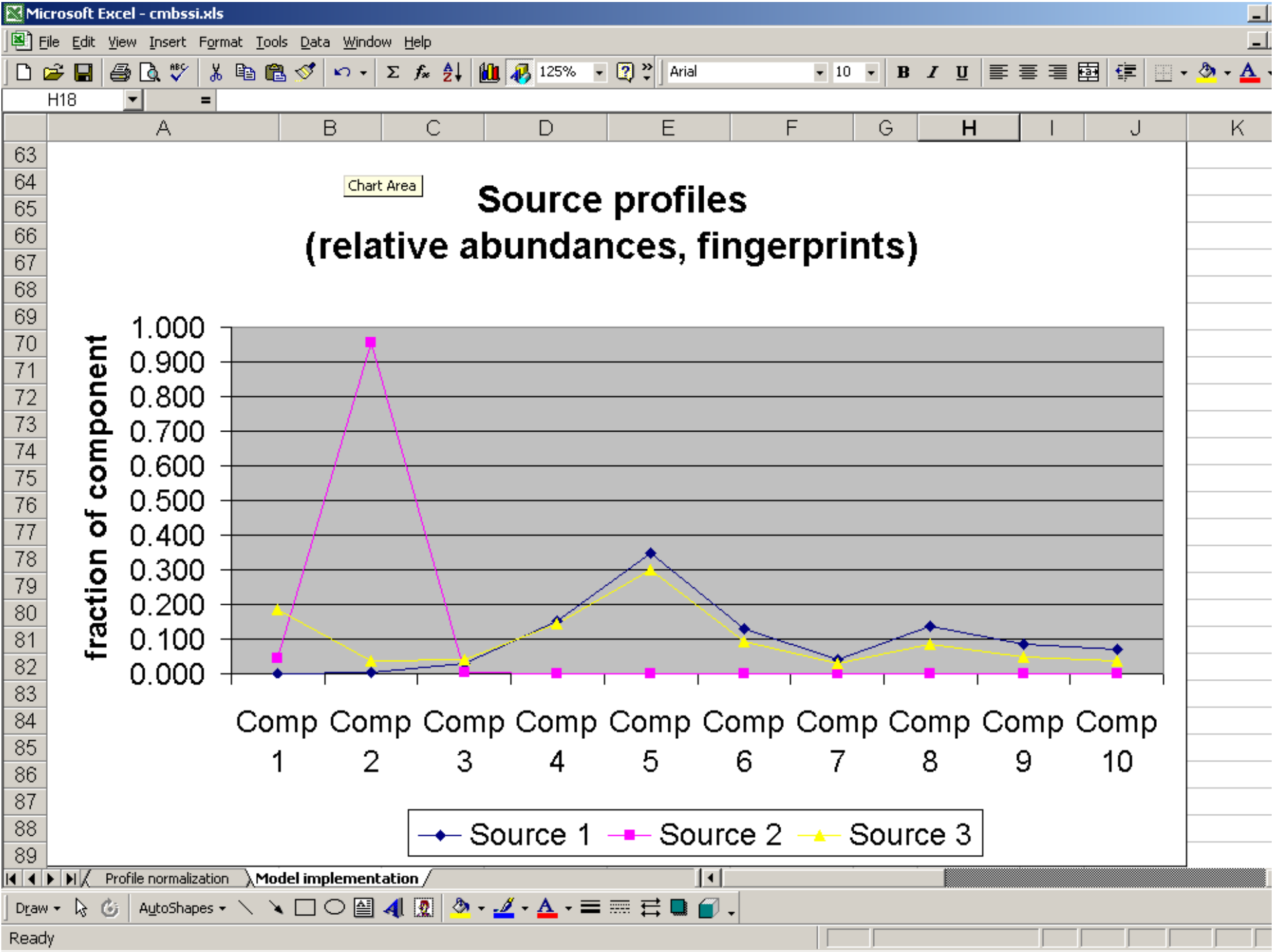
- Add
- Change
- Delete

Options Reset All Help



### Model fit





# Chemical Mass Balance Receptor Modelling U.S. EPA's CMB Model

- There are uncertainties associated with both the receptor and source profiles. The measured quantities are thus:
- The model results then also have uncertainties associated with them:

$$y_i \pm \Delta y_i \quad \text{and} \quad x_j \pm \Delta x_j$$

$$\beta_j \pm \Delta \beta_j$$

# U.S. EPA's CMB Model

## The "effective variance" method

The CMB model uses an effective variance which looks at variances in both the receptor, and source profiles weighted by the source contributions:

$$V_{ei} = \sigma_{Ri}^2 + \sum_j \beta_j^2 \sigma_{Sij}^2$$

$\sigma_{Ri}^2, \sigma_{Sij}^2$  : variances associated with the  $i^{\text{th}}$  component  
in the receptor and source profiles

$V_{ei}$  : diagonal elements of the "effective variance matrix"  
used in the iterative search for  $\beta_j$

## U.S. EPA's CMB8

- The CMB model incorporates the statistics to improve our estimate of the source contributions by weighting the source and receptor profiles according to the uncertainties associated with them.
- It also reports the uncertainties associated with the source contribution estimates and “goodness of fit” parameters.

# Positive Matrix Factorization (PMF)

# Other receptor models

CMB applies the mass balance principles to *known* receptor and source compositions to arrive at the source contribution estimates.

Another type of source apportionment analyzes multiple measurements at the receptor (i.e. many hours of hourly average data) *without prior knowledge of the sources* but attempts to identify “factors” that explain the variation in the composition. The factors are then interpreted as types of sources.

# PMF Characteristics

- ❑ Method: Weighted least-squares
- ❑ Utilize error estimates of the data to optimum data point scaling
- ❑ Non-negativity constraints
- ❑ Does not require comprehensive advance information on source compositions
- ❑ Incorporate the time variation
- ❑ Obtain uncertainties for source composition and source contribution output profiles



# PMF Characteristics

- Input:
  - Ambient concentration data
  - Uncertainty of ambient data
- Output
  - Source compositions (F-factor)
  - Source contributions (G-factor)
  - Scaled residuals ( $e_{ij}/s_{ij}$ )

# Methodology Approach

- Data handling/preparation
- Run PMF
- Interpretation of PMF results
- Source identification and source apportionment
- Optional examination of variations of source contributions and meteorological effects

$$X = GF + E$$

$X$ :  $n \times m$  data matrix measured at the receptor, of  
 $m$  compounds and  $n$  observations

$G$ :  $n \times p$  matrix of the time variation of source contributions,  
 $n$  periods and  $p$  sources

$F$ :  $p \times m$  matrix of source (factor) compositions,  
 $p$  sources,  $m$  compounds

$E$ :  $n \times m$  matrix of residuals

Given  $X$ , PMF attempts to find  $G$  and  $F$  with all positive elements to minimize the elements of  $E$ , i.e., to minimize:

$$Q(E) = \sum_{i=1}^n \sum_{j=1}^m \left( \frac{e_{ij}}{s_{ij}} \right)^2$$

where  $e_{ij}$  are the elements of the  $E$  matrix,

$s_{ij}$  are the error estimates for the elements of the  $X$  matrix

# Data File

Sample No.	Al	As	Br	Ce	Cl
1	1016.86	0.56	-1.29	0.59	675.83
2	853.37	2.61	9.63	0.71	915.45
3	822.65	0.99	8.23	0.31	567.13
4	1574.65	1.68	18.03	1.93	710.76
5	1074.94	0.97	11.23	0.85	693.22
6	2497.35	3.42	38.70	2.03	534.36
7		1.56	8.91	1.16	399.18
8	1057.57	1.02	9.72	1.02	875.76
9	998.97	1.43	40.43	0.93	< 100
10	1719.75	1.85	51.05	1.55	1290.81

# Data Handling

		<u>Data</u>	<u>Unc.</u>
• Missing data	➤	$\bar{X}_{ij}$	$4 \bar{X}_{ij}$
• $< DL$	➤	$1/2 DL$	$DL$
• Negative values	➤	Real data	

# PMF Operation

- PMF2 program
  - Dr. Pentti Paatero, University of Helsinki, Finland
- EPA PMF 1.1 using ME2 program
  - Dr. Shelly Eberly, US EPA, U.S.A.

# PMF Running: Trial and error

- Varying the number of factor
- Varying parameters/optional functions
- Graphical interpretation of obtained results of G and F factors
- Decision make for the number of source factor to be retained

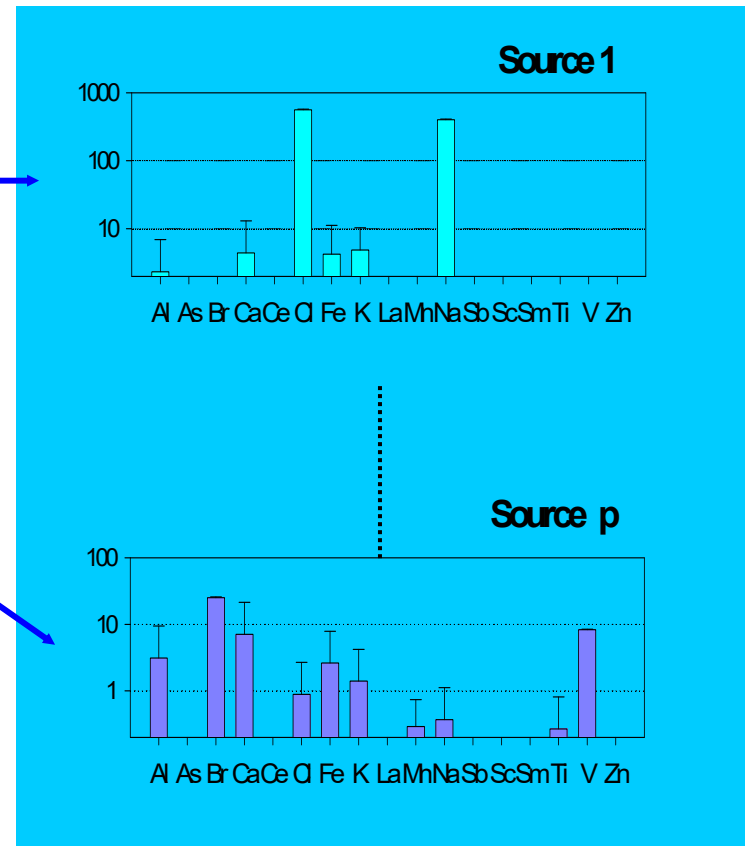
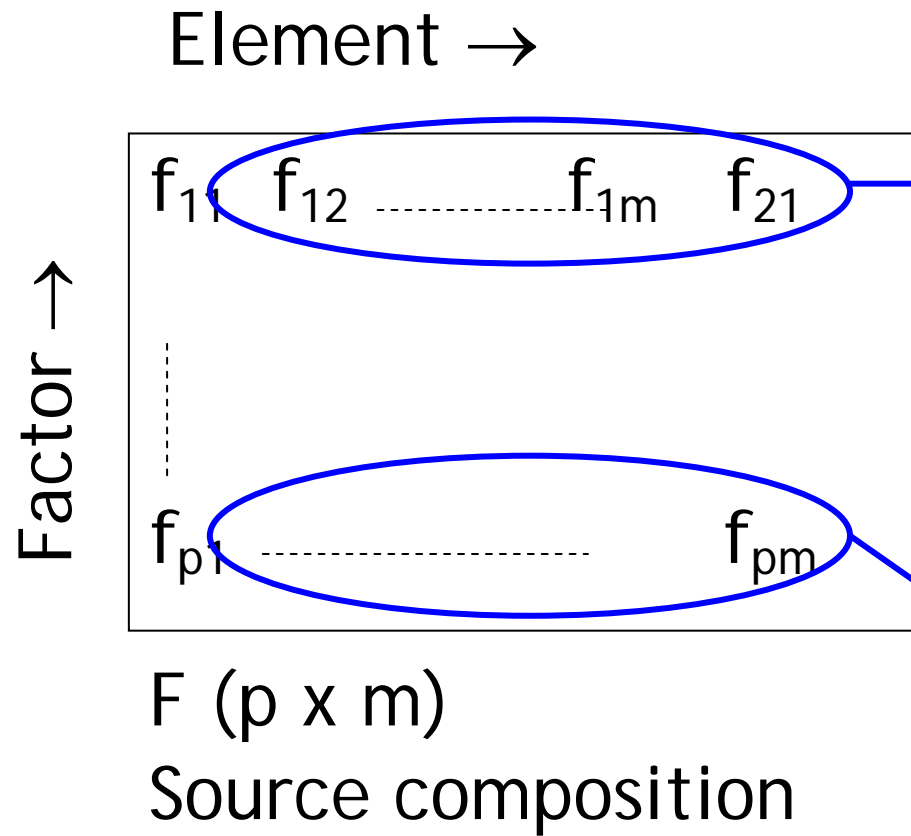


# Determination of the Number of Sources

- Too few factors will combine sources of different nature together
- Too many factors will make a real factor dissociate into two or more non-existing sources
- A good fit of Q value
- The weighted residuals of the model ( $e_{ij}/s_{ij} \sim \pm 2$ )
- The interpretable and most meaningful factors

PMF Results :  
Source Identification/Fingerprint

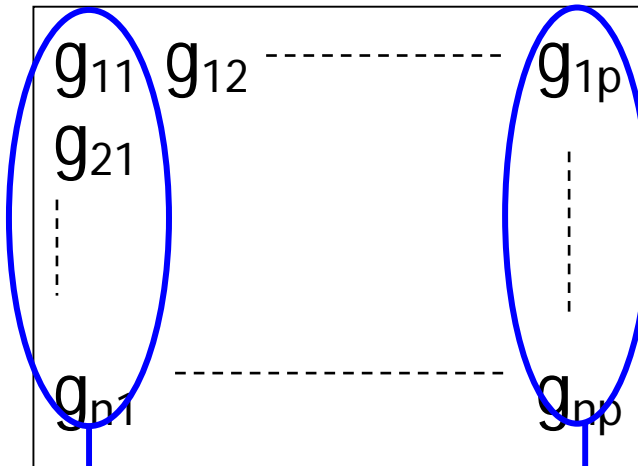
# Source Identification



# Source Contributions to Samples

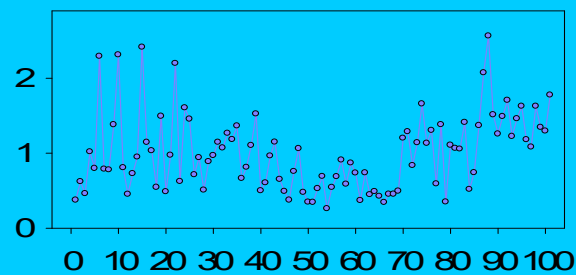
Source factor

Mass  
Contribution



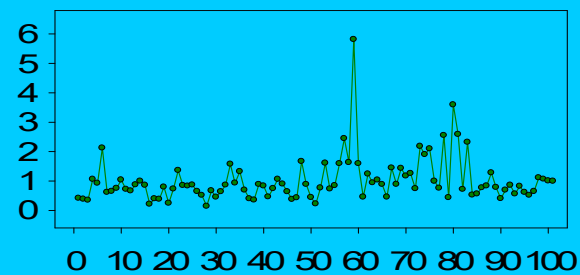
$G (n \times p)$

**Source 1**



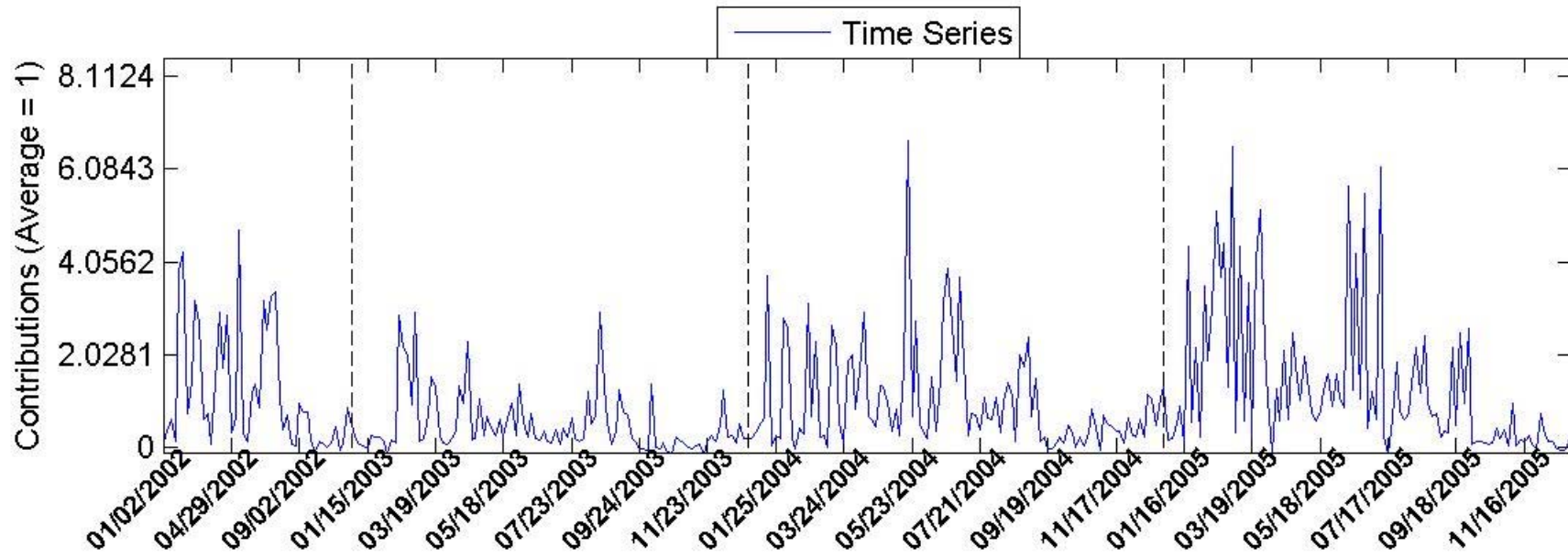
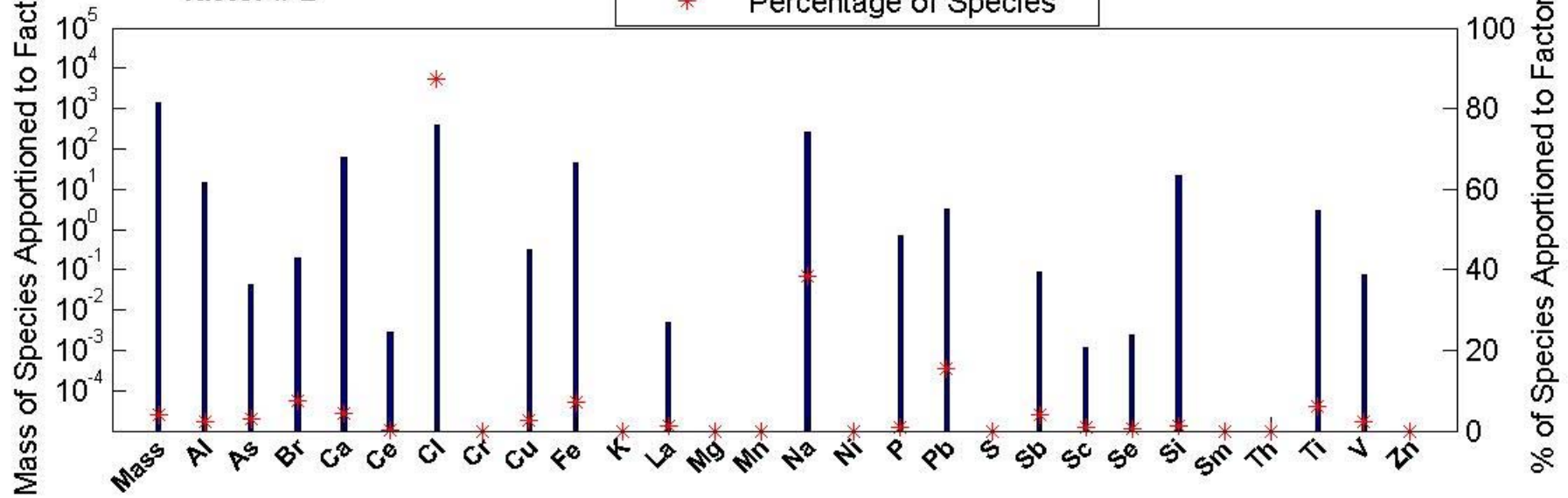
A time series plot

**Source p**



A time series plot

Model Results from random run # 1  
factor # 2



## Airborne Contributions of Certain Marker Species

Source	Elements
Soil	Al, Si, Ca, Sc, Ti, Fe, Mn, K
Cement/Construction	Ca, Mg
Sea-salt	Na, Cl, Mg
Motor vehicles	Br, Pb, Zn, C
Refuse incineration	Sb, Zn, Cd, Ag, Sn, Pb
Wood burning	K, C
Oil combustion	V, Ni, Rare earths
Coal combustion	As, Se, S, C, K
Sulfide smelters	In, Cd, As, Se, S

PMF Results :  
Source Apportionment

# Source Apportionment

- Source contribution factor (G factor) from PMF result
- MLR analysis program
  - Excel
  - StatGraphics
- Graphical interpretation
  - Excel
  - SigmaPlot
  - StatGraphics

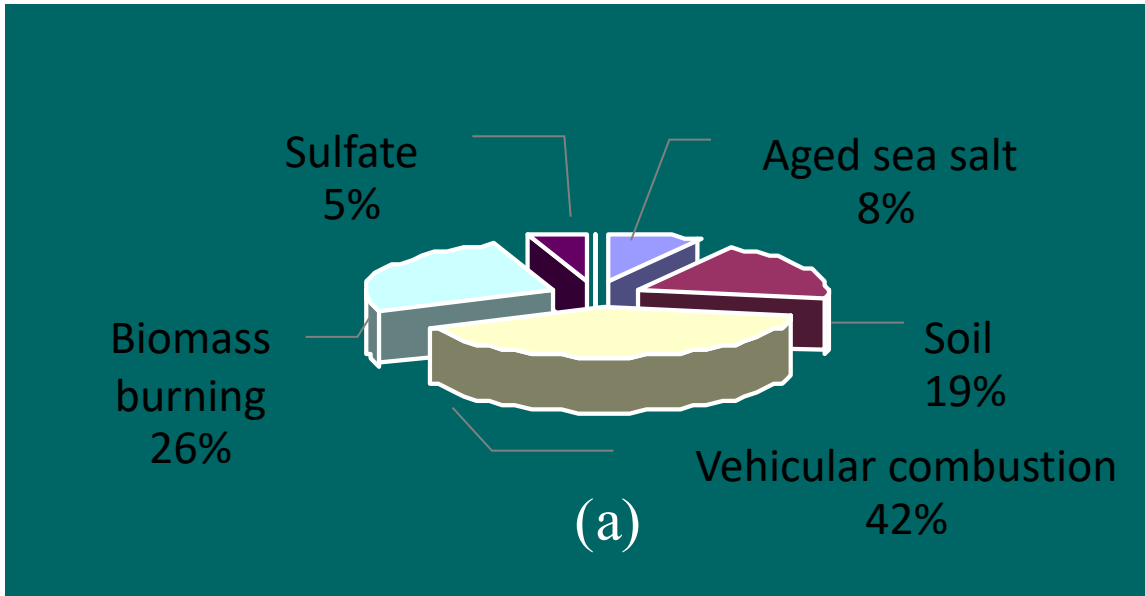


# Multilinear Regression

- Calculates the statistics for a line by using the "least squares" method to calculate a straight line that best fits your data
- The equation for the line is:

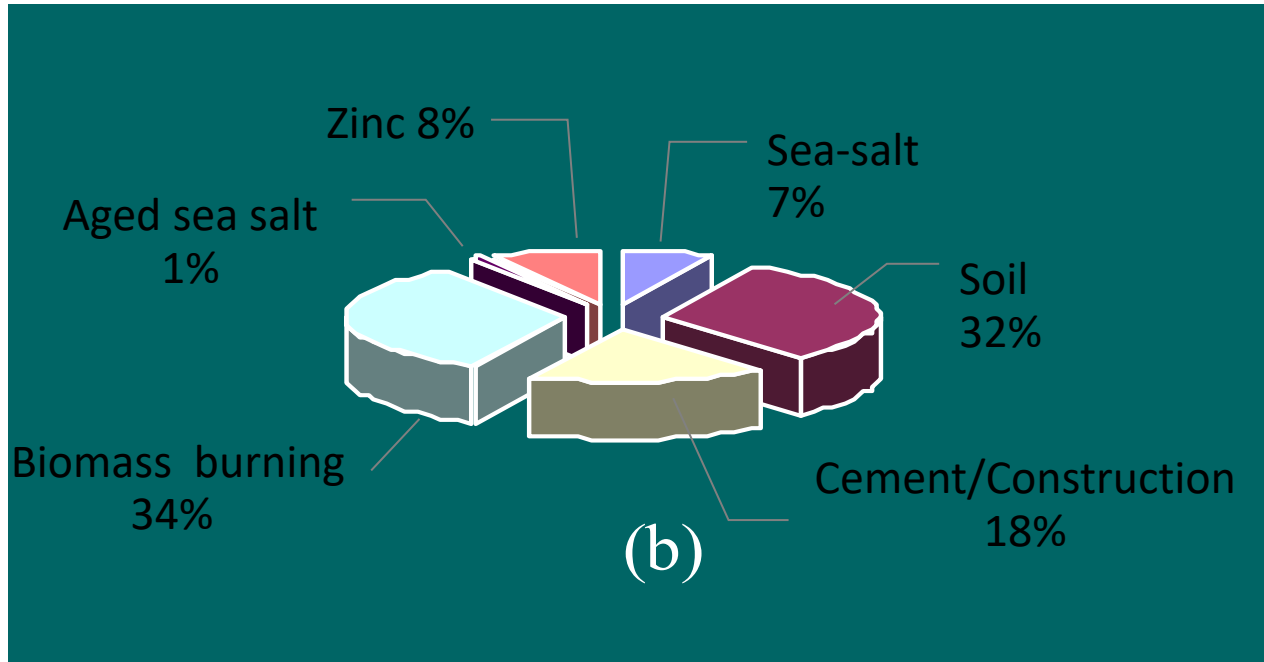
$$y = mx + b$$

$$\underline{\text{PM mass}} = a_1G_1 + a_2G_2 + \dots + a_kG_k$$



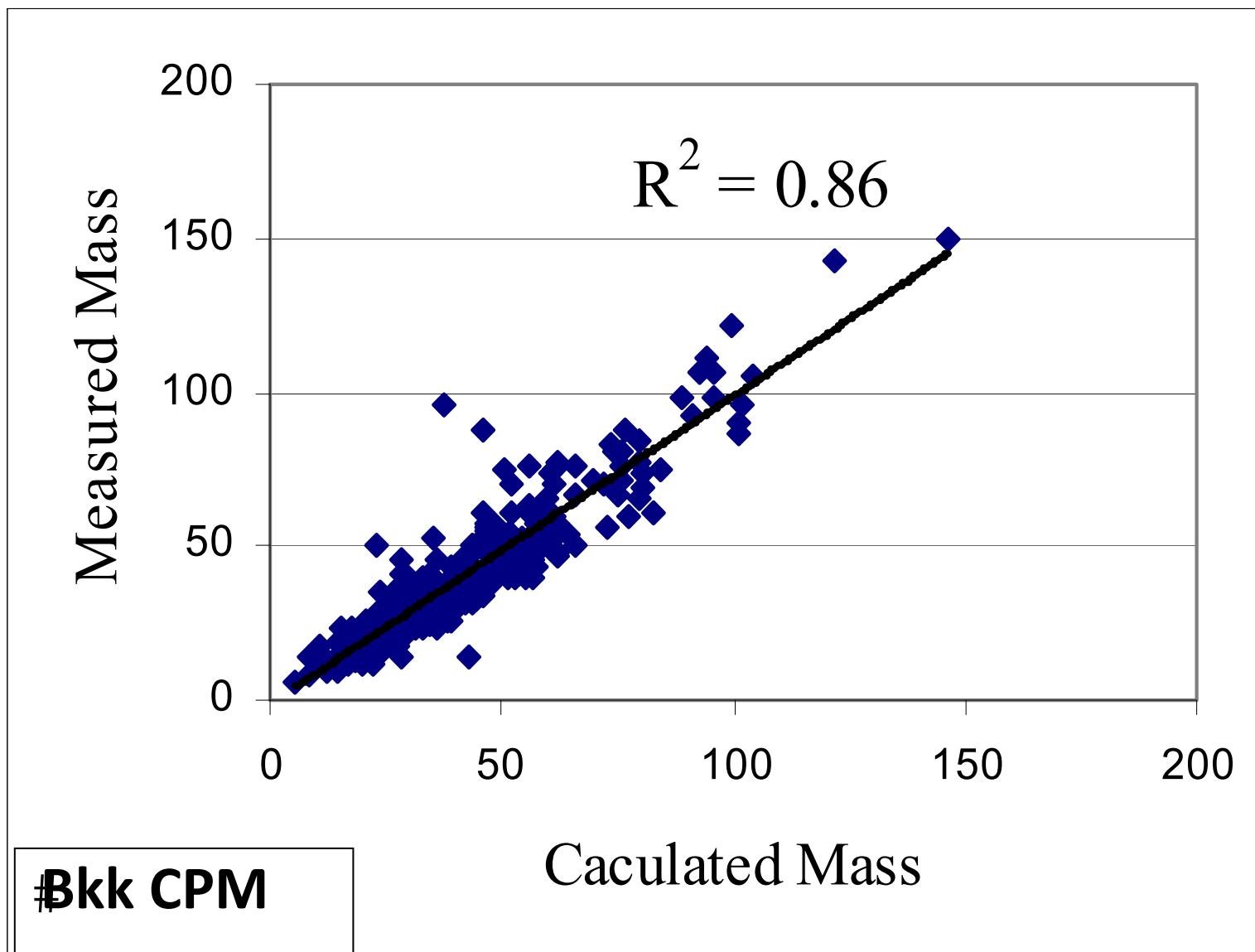
← FPM At Bkk

CPM at Bkk →



# Model fitting

- Measured values & [Model values](#)
- Graphical interpretation
  - Excel



In CMB the required data are the source profiles, or fingerprints, of a list of compounds for all potential sources and the corresponding ambient measurements. CMB modelling can be done individually for each ambient measurement (even a single one!) but getting the source profiles for locally relevant sources requires much effort.

In PMF, many ambient measurements are obtained over a long time period. Statistical analysis of the trends in the individual measured components then leads to the identification of "factors" that explain the variation. These factors can then be identified with potential sources. Actual source profile measurements are not required. Instead, collecting sufficiently long time series data on ambient concentrations becomes the critical issue.

# CMB – PMF Comparison

Even a single receptor observation can be analyzed by CMB, assuming we have characterized the potential sources.

PMF does not require that we characterize the potential sources but it does require sufficient observations to identify the potential sources.