

# Quasi Neutralità – Debye Shielding

Per definizione...

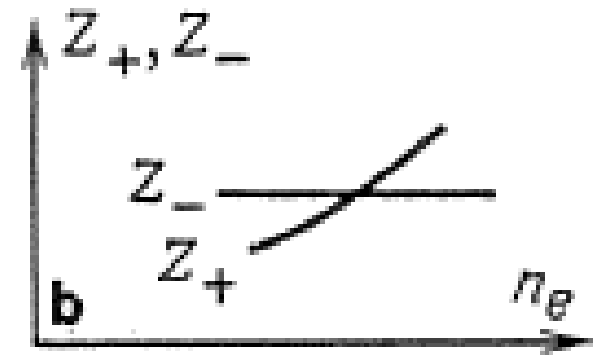
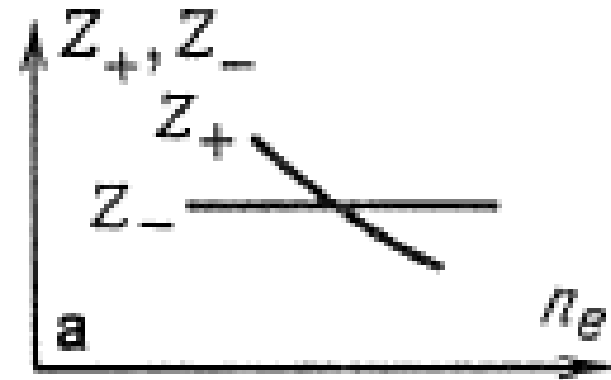
...un plasma è un gas ionizzato globalmente neutro...

Descrizione fluida:  $n_e/n_i/n_g$ ,  $T_e/T_i/T_g$ ,  $E$

$$\frac{dn_e}{dt} = Z_+ - Z_- .$$

$$Z_+ \sim K_{ion}(T_e) n_e n_g$$

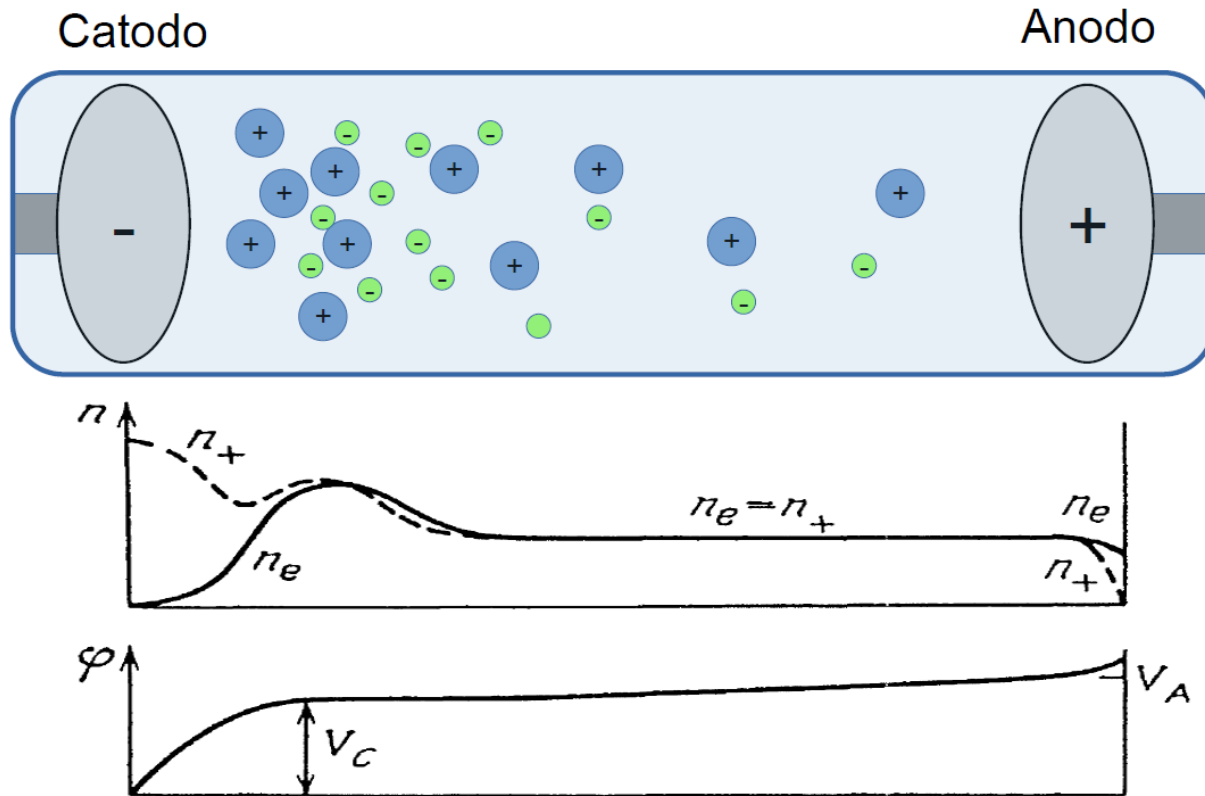
$$Z_- \sim v_{diff} n_e / K_{rec} n_e^2$$



(a) stabile/(b) instabile

# Scariche elettriche nei gas

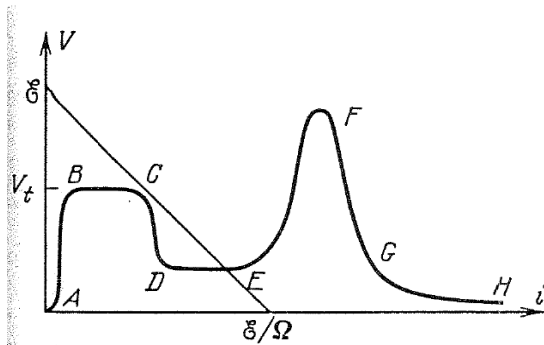
## Glow discharge



# Scariche elettriche nei gas

## Glow discharge

$T_e/n_g \approx \text{cost} \Rightarrow Z_+ \approx ne, Z_- \approx ne/ne^2 \Rightarrow \text{stable}$



$\Omega_{\text{EXT}} \approx \text{cost} \Rightarrow J \nearrow, V = (\xi - \Omega) \searrow, K_{\text{ion}} \searrow$

$Z_+ \sim ne^a (a < 0), Z_- \sim ne^a (a \approx 0)$

Gas heating  $\Rightarrow T_g \nearrow, n_g \searrow, E/N \nearrow, K_{\text{ion}} \nearrow \quad Z_+ \sim ne^a (a > 0)$

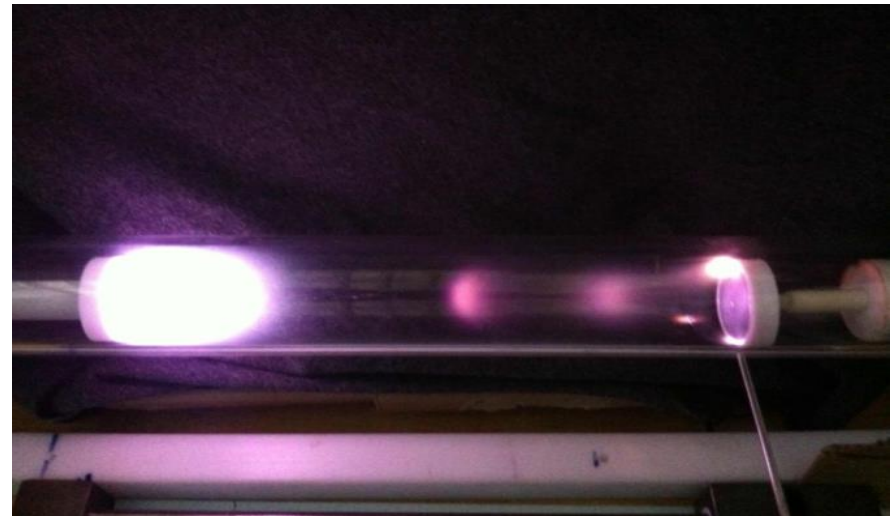
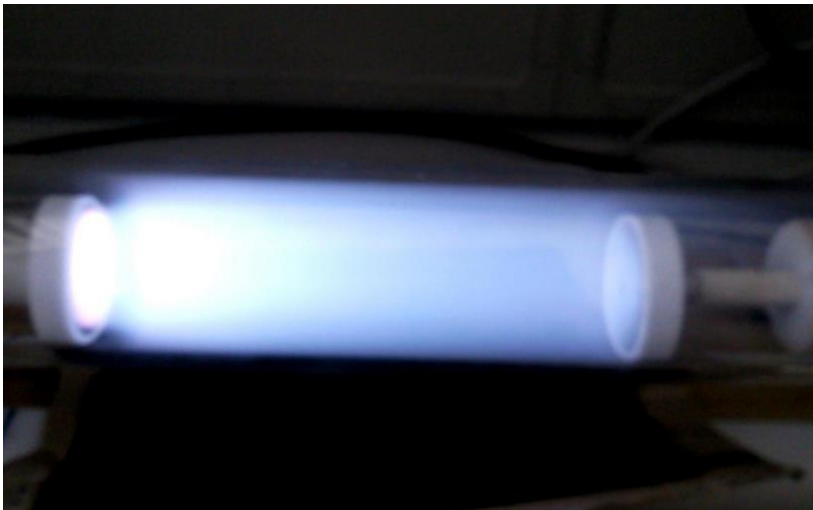
Step-wise ionization  $\Rightarrow n_X \nearrow, K_{\text{ion}} \nearrow \quad Z_+ \sim n \cdot n_X (\approx n^2)$   
(Maxwellization/At-Detachment)

# Scariche elettriche nei gas

## Glow discharge

Homogeneous plasma => inhomogeneous

Striation (longitudinal)  
Contraction (transverse)

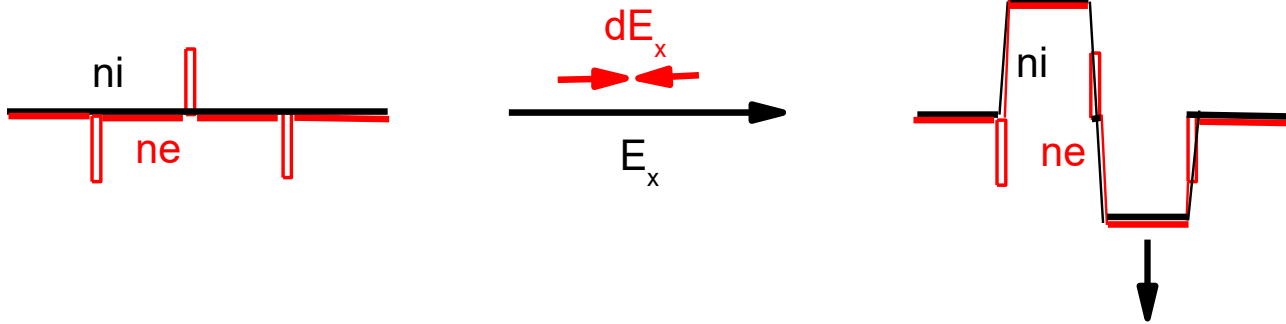
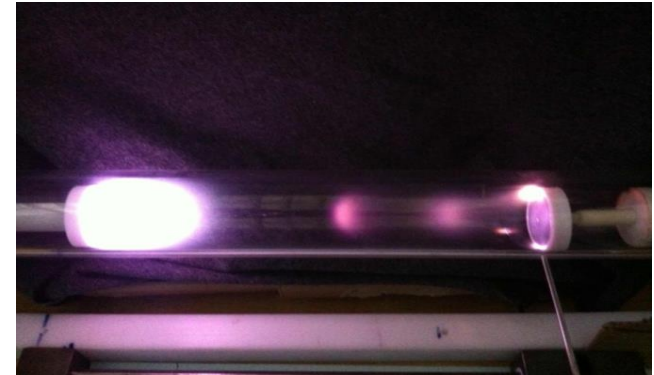


# Scariche elettriche nei gas

## Glow discharge

### Striation

Step-wise ionization =>  
 $n_e \nearrow, n_x \nearrow, K_{ion} \nearrow$



Longitudinal:

$$|E| \sim E_x \pm dE_x$$

Transverse inefficient:

$$|E| \sim \sqrt{E_x^2 + dE_y^2} \sim E_x + \frac{1}{2} \frac{dE_y^2}{E_x}$$

# Scariche elettriche nei gas

## Glow discharge

### Striation

Step-wise ionization  $\Rightarrow n_x \nearrow, K_{ion} \nearrow$

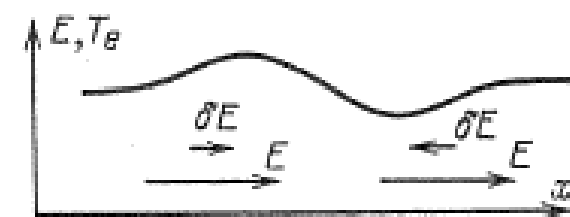
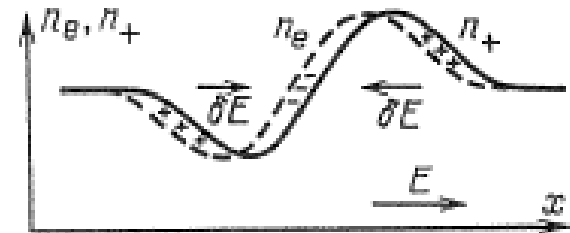
$$dn_e/dt = k_i N n_e + k_i^* N^* n_e - \nu_{da} n_e, \quad k_i = k_i(T_e),$$

$$dn^*/dt = k^* N n_e - k_2 N^* n_e - \nu_d^* N^*, \quad k^* = k^*(T_e).$$

$$N^* \approx N^* [n_e(t)] \approx k^* N n_e / (k_2 n_e + \nu_d^*).$$

$$n_e \propto \exp(\Omega t)$$

$$\Omega = \frac{\nu_d^* k_i^* N^{*2}}{\nu^* n_e} + \frac{\delta \ln T_e}{\delta \ln n_e} (\hat{\nu}_1 \nu_1 + \hat{\nu}^* k_i^* N^*)$$

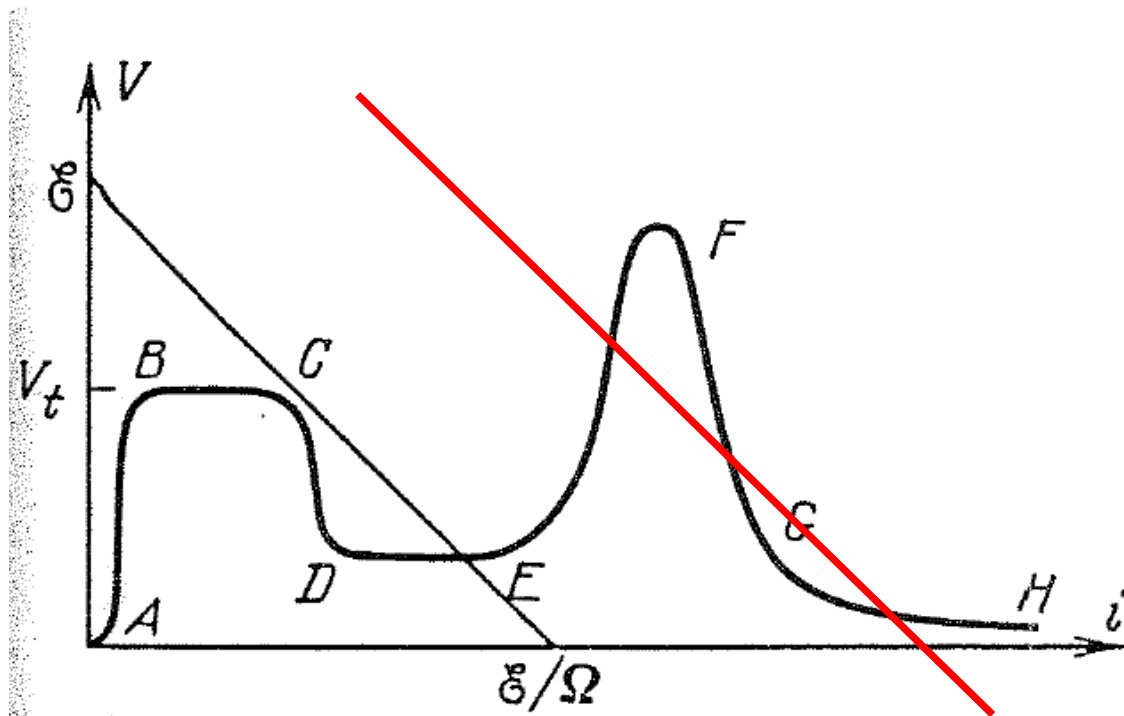


$J \sim \cos t \Rightarrow n_e = a + b \sin(kz)$  Longitudinal profile  $\Rightarrow$  propagates<sub>6</sub>

# Scariche elettriche nei gas

## Glow discharge

Contraction



Positive Column  $\Rightarrow$  Current Filament  
Glow Discharge  $\Rightarrow$  Arc (Voltaic)

# Scariche elettriche nei gas

## Glow discharge

### Contraction due to Thermal Instability

$$\delta n_e \uparrow \rightarrow \delta(jE) \uparrow \rightarrow \delta T \uparrow \rightarrow \delta N \downarrow \rightarrow \delta(E/N) \uparrow \rightarrow \delta T_e \uparrow \rightarrow \delta n_e \uparrow .$$

$$\Omega = \nu_T^0 \frac{\delta \ln n_e}{\delta \ln T} - \nu_{TF}, \quad \nu_T^0 = \frac{\sigma E^2}{N c_{p1} T} = \frac{\gamma - 1}{\gamma} \frac{\sigma E^2}{p} \quad jE > N c_{p1} T \nu_{TF} / \hat{u}_1 ;$$

Transverse:  $Z_- \sim \frac{D}{R^2} ne + K_{rec} ne^2 \quad R_{eff} \sim \sqrt{D/K_{rec} ne}$

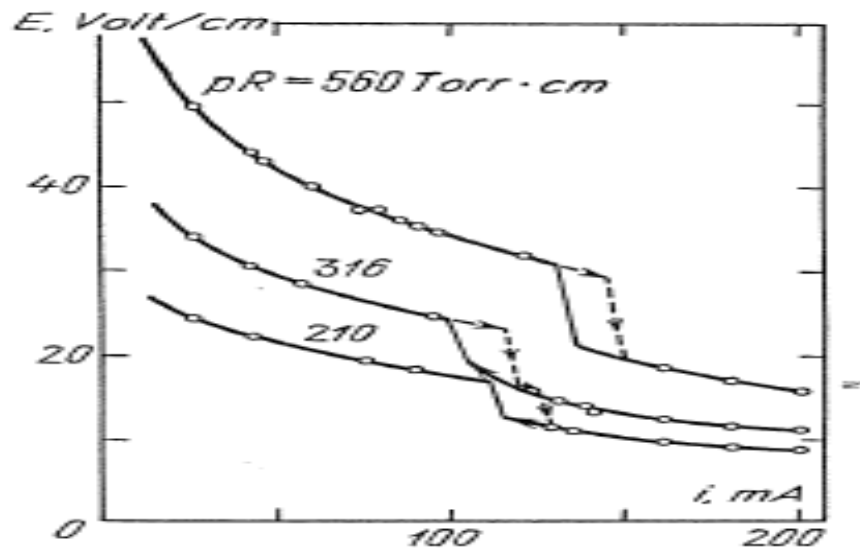
Longitudinal inefficient:  $I \approx \text{cost} \Rightarrow ne(x) \approx \text{cost}$



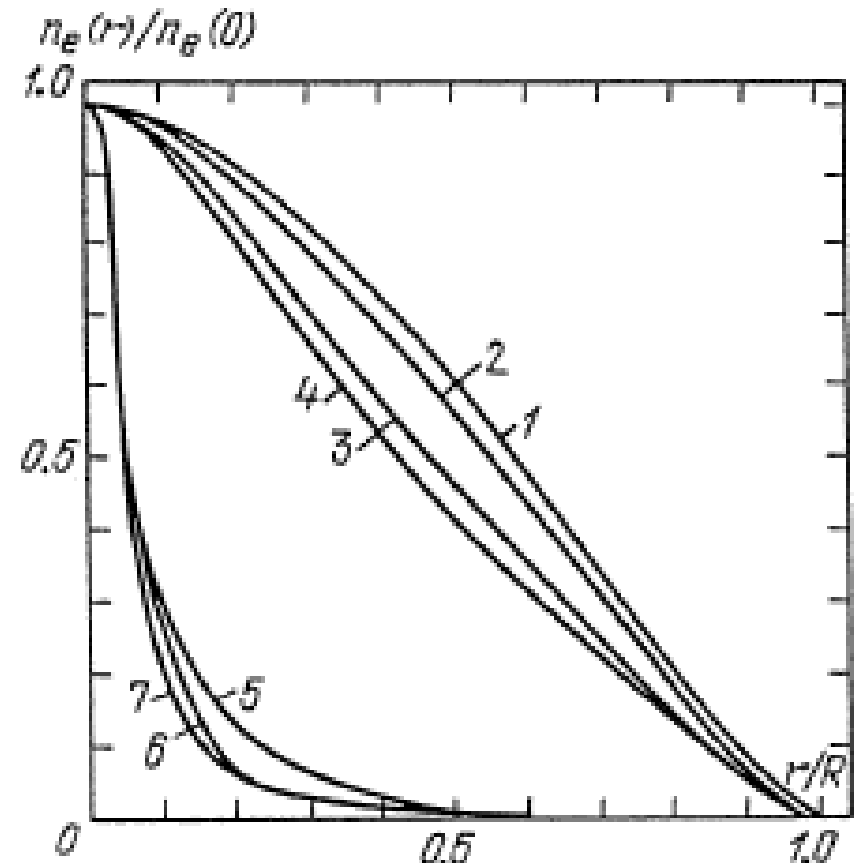
# Scariche elettriche nei gas

## Glow discharge

### Contraction due to Thermal Instability



$i, \text{ mA}$	$T_e(0), \text{ eV}$	$T(0), \text{ K}$	$n_e(0), 10^{11} \text{ cm}^{-3}$
13.5	3.0	440	0.12
43	3.3	650	0.39
75	3.6	840	0.93
96	3.7	930	1.2
120	3.0	1200	54
160	2.6	1300	72
200	2.5	1400	93



# Moto di una carica in un plasma magnetizzato

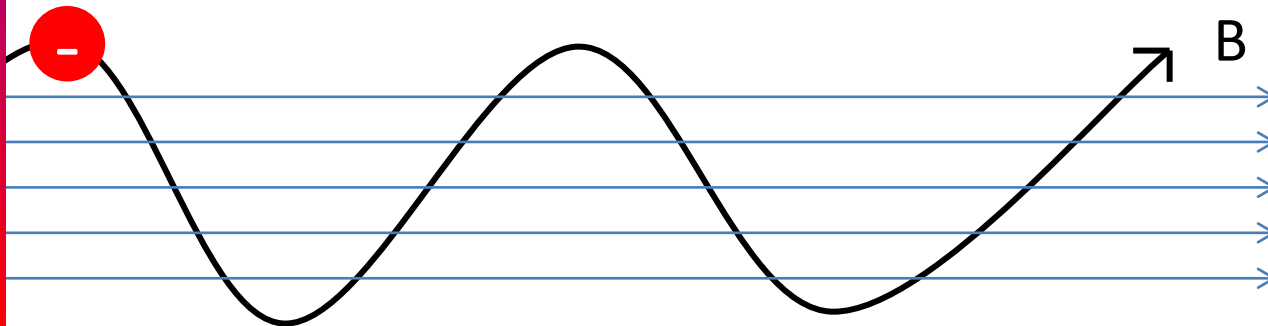
In un campo magnetico uniforme in una direzione:

$$\begin{cases} m \frac{dv_{\parallel}}{dt} = q(v_{\parallel} \wedge B_{\parallel}) = 0 \\ m \frac{dv_{1\perp}}{dt} = qv_{2\perp}B \\ m \frac{dv_{2\perp}}{dt} = -qv_{1\perp}B \end{cases}$$

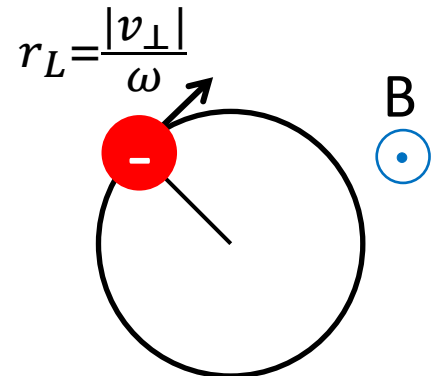
Frequenza di ciclotrone (o di girazione):

$$\omega_c = \frac{qB}{m}$$

$$\begin{aligned} v_{\parallel} &= \text{const} \\ v_{1\perp} &= v_{\perp} \cos(\omega_c t) \\ v_{2\perp} &= v_{\perp} \sin(\omega_c t) \end{aligned}$$

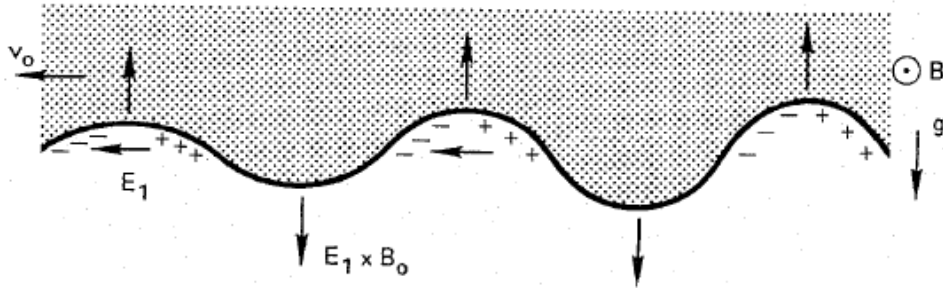


Raggio di larmor

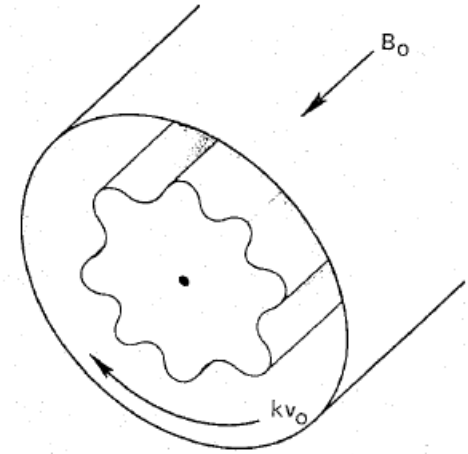


# Instabilità di un plasma magnetizzato

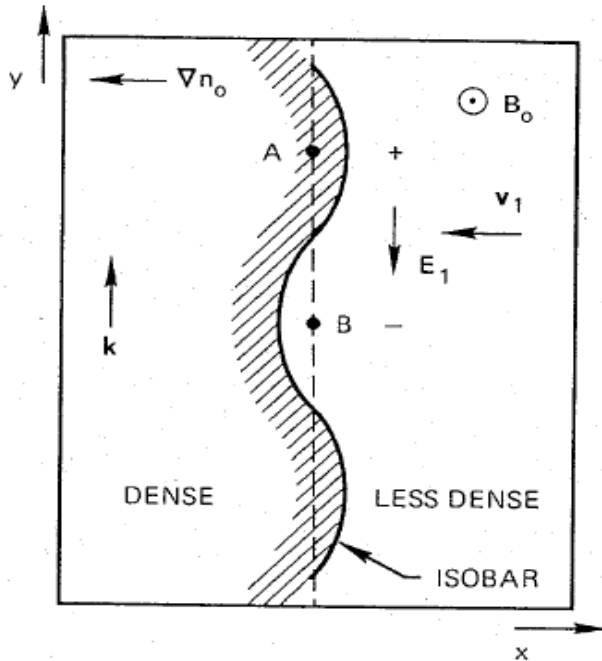
Rayleigh-Taylor (gravitational)



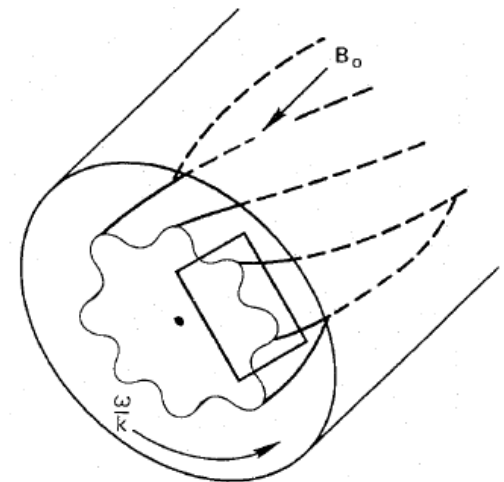
Flute structure



Drift wave instability

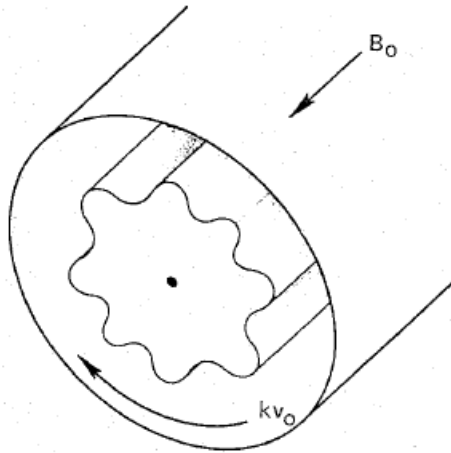


Drift structure



# Instabilità di un plasma magnetizzato

## Flute structure

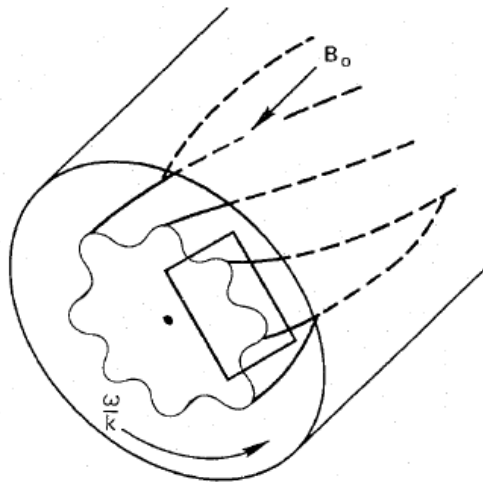


$$k_{\parallel} = 0$$

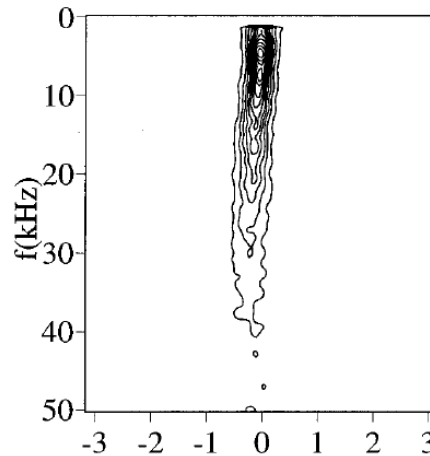
$$\frac{\tilde{n}}{\langle n \rangle} \ll \frac{e\tilde{\Phi}}{\langle kT_e \rangle},$$

$$\Phi(\bar{n}, \bar{E}) \approx 0$$

## Drift structure



$$k_{\parallel} \neq 0$$



$$\frac{\tilde{n}}{\langle n \rangle} \approx \frac{e\tilde{\Phi}}{\langle kT_e \rangle},$$

$$\Phi(\bar{n}, \bar{E}) \approx \pi / 2$$

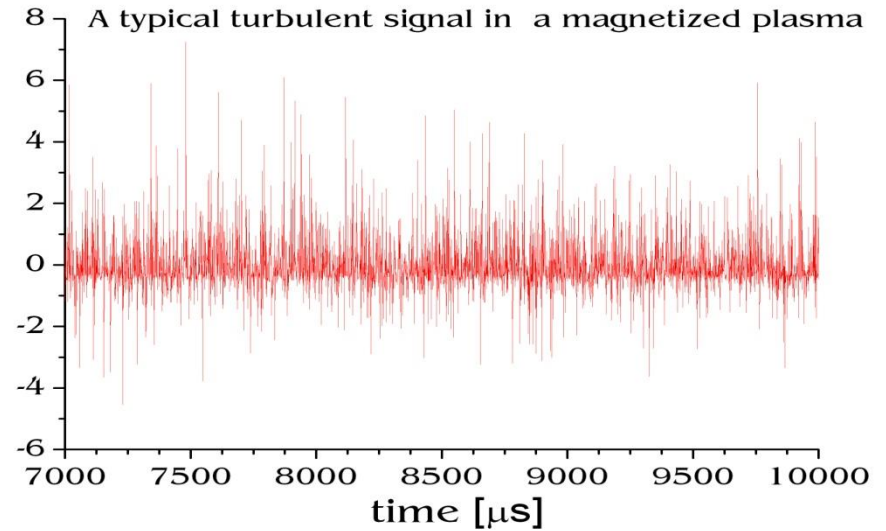
(b)  $k_{\parallel}$  (cm-1)

# Turbolenza

Hydrodynamics:

- Non-linear differential equations
- Scale difference between energy dissipation and energy input.

=> MHD turbulence



**Fluctuations:** 
$$\mathbf{X} = \langle \mathbf{X} \rangle + \overline{\mathbf{X}}$$

Deterministic:  $X_n : \sigma_X \longrightarrow 0, n \longrightarrow \infty$

Turbulence:  $\sigma \rightarrow \alpha \neq 0$

# Turbolenza

## Approccio analitico alle fluttuazioni

FFT, power spectrum, Beall analysis

$$S(k, \omega) = \frac{1}{M} \sum_{i=1}^M I_{0, \Delta k} [k - k^i(\omega)] S^i(\omega),$$

$$k^i(\omega) = \frac{1}{\Delta x} \arg[\Phi_2^i(\omega) \Phi_1^{i*}(\omega)],$$

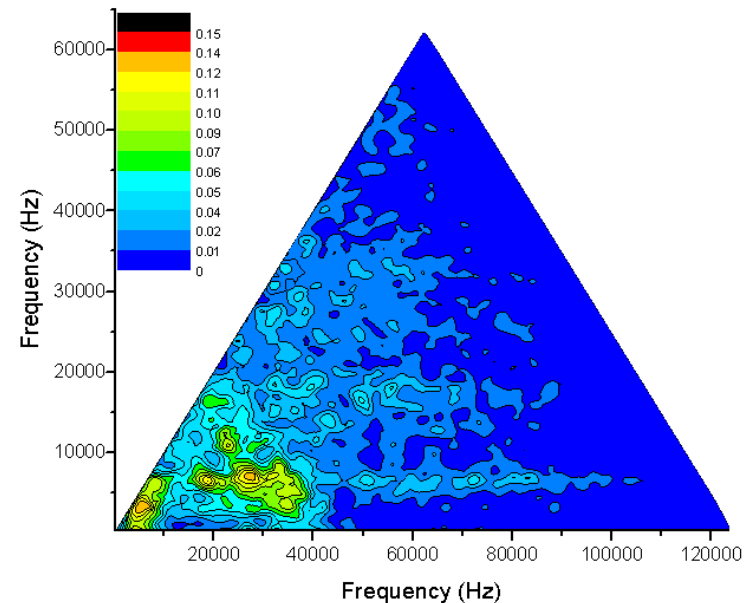
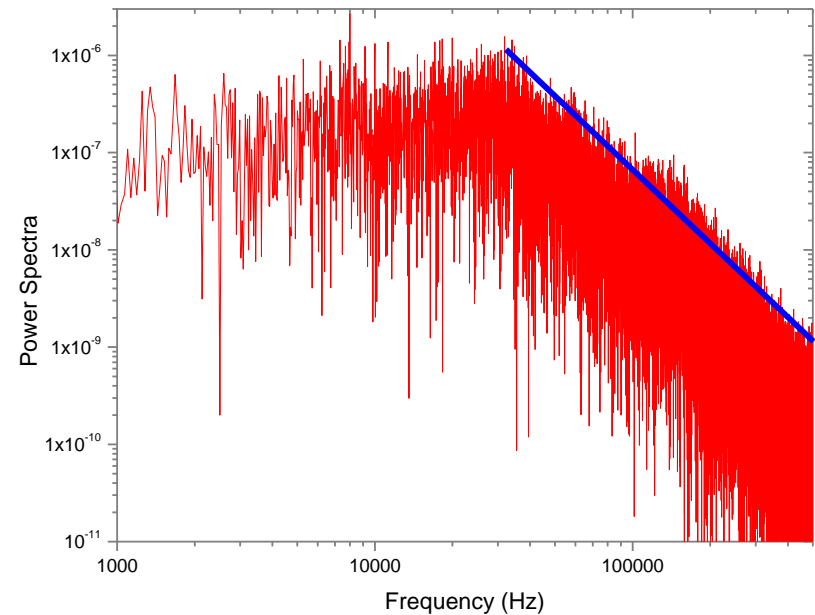
$$S^i(\omega) = \frac{1}{2} [|\Phi_1^i(\omega)|^2 + |\Phi_2^i(\omega)|^2],$$

Wave-wave interactions, bicoherence

$$B = b^2(\omega_1, \omega_2, \omega_1 + \omega_2) = \frac{|\langle f(\omega_1) f(\omega_2) f(\omega_1 + \omega_2)^* \rangle|^2}{\langle |f(\omega_1) f(\omega_2)|^2 \rangle \langle |f(\omega_1 + \omega_2)|^2 \rangle}$$

Cascade and inverse cascade

$$\partial P_k / \partial t \approx \gamma_k P_k + \sum_{\substack{k_1, k_2 \\ k = k_1 + k_2}} T_k(k_1, k_2),$$



# Turbolenza

## Approccio statistico alle fluttuazioni

$$\{f(t_n)\}, t_n = nT \Rightarrow \{f_n\}$$

$$\text{frequency} \Rightarrow \text{PDF}(f)$$

$$m_k = \int f^k \text{PDF}(f) df$$

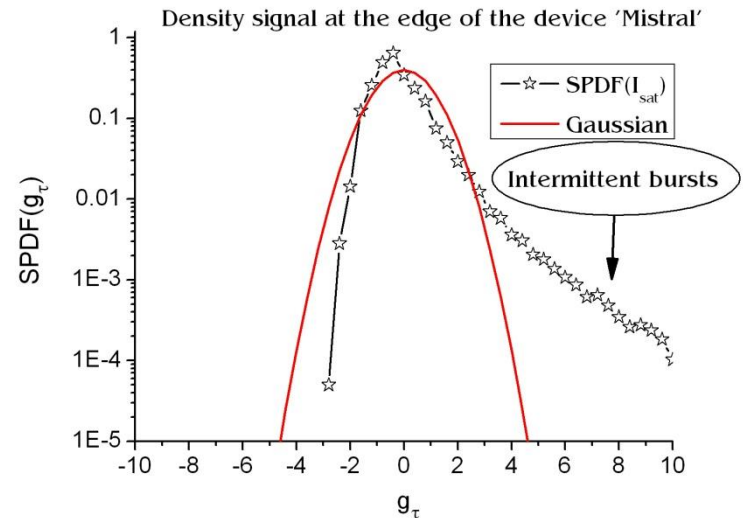
PDF, Non Gaussianity

$$a(T) = \int f(t) f(t+T) dt$$

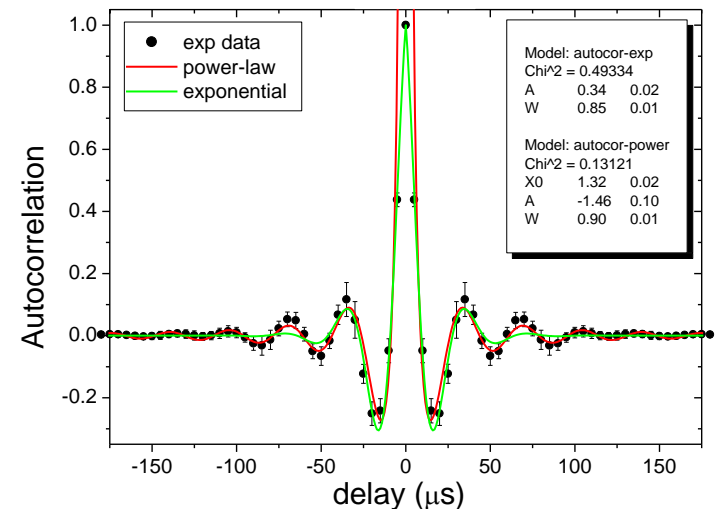
$$\text{PDF} \left[ |f(t) - f(t+T)|^k \right]$$

$$\text{PDF}(T_{\text{wait}}), T_{\text{wait}} :$$

$$f(t) > a, f(t+T) > a, f(t+T-1) < a$$



Time correlations, Memory,  
Structure Functions (intermittenza)



# Turbolenza

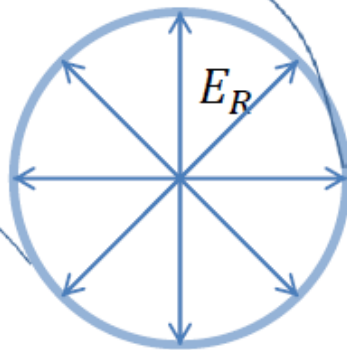
**Strutture spazio-temporali (coerenti) delle fluttuazioni**

**Trasporto convettivo delle fluttuazioni**

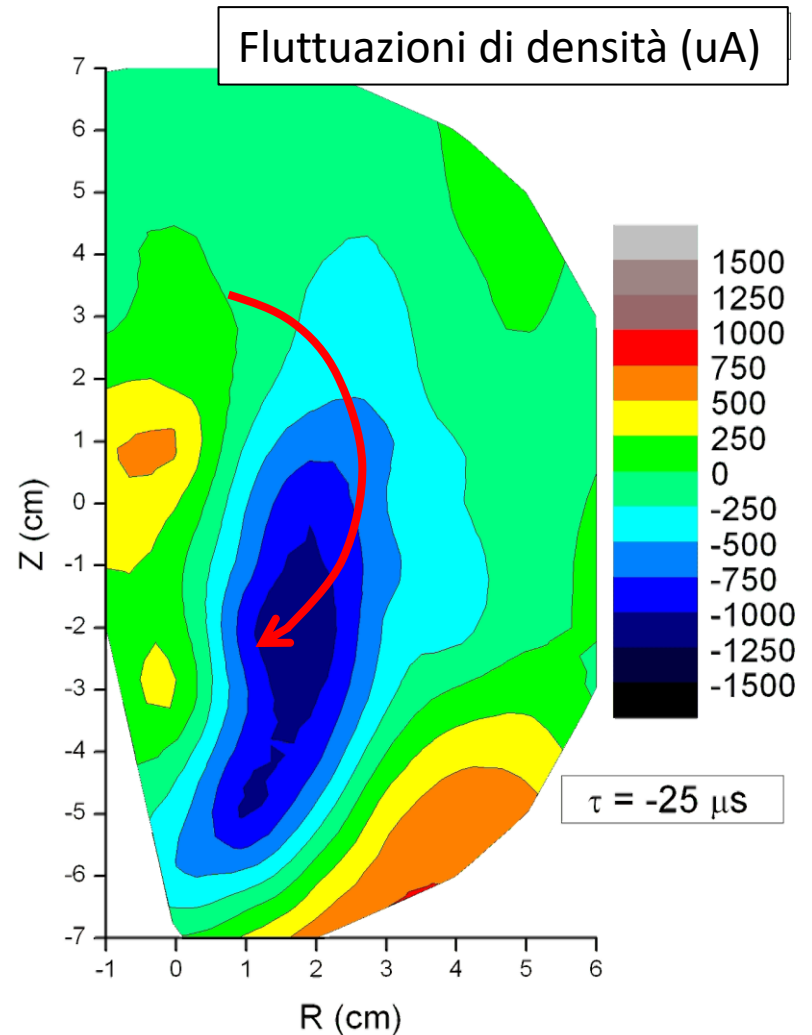
**Un campo elettrico  $E$  in un plasma magnetizzato a confinamento toroidale**

Gli elettroni primari vengono emessi da un filamento al centro della camera e accelerati verso le pareti da un campo elettrico radiale.

Esisterà quindi una rotazione macroscopica del plasma:



$$v_{\theta} = \frac{E_R \times B_{\phi}}{B^2}$$

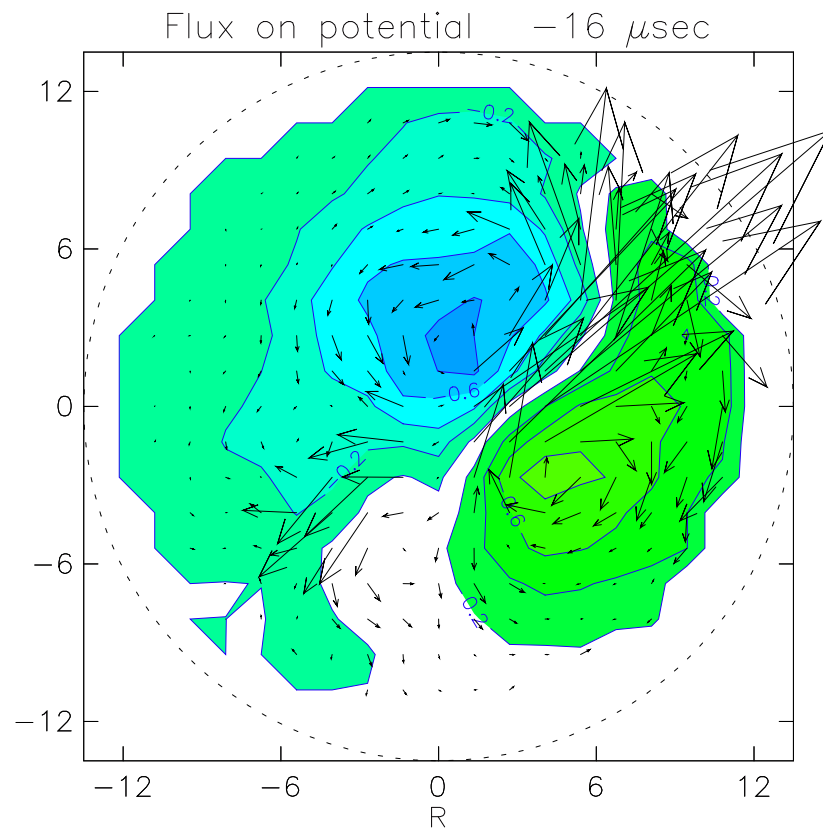
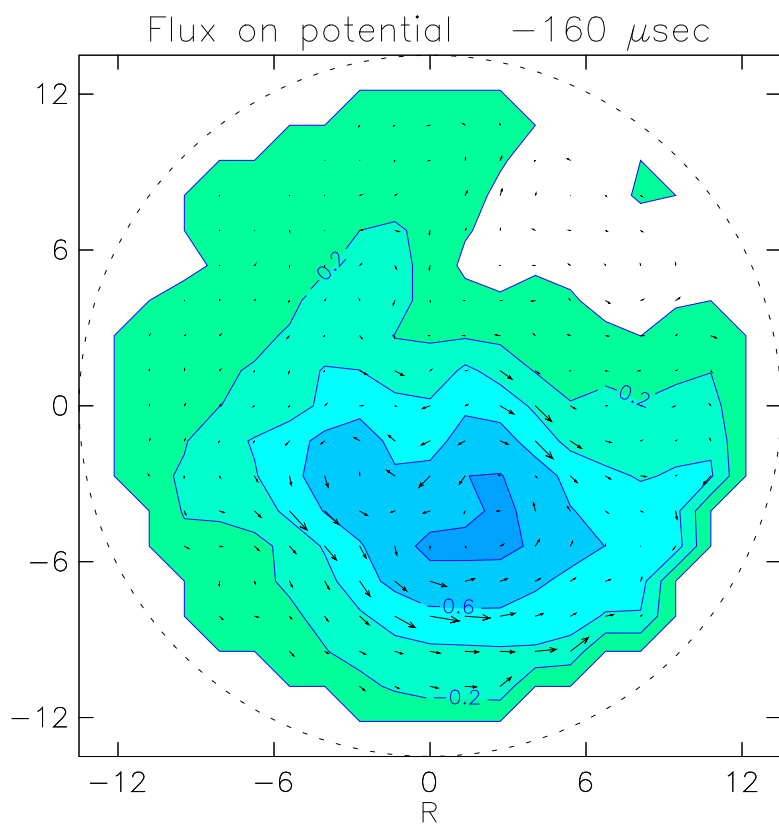




# Turbolenza

## Vortex structures

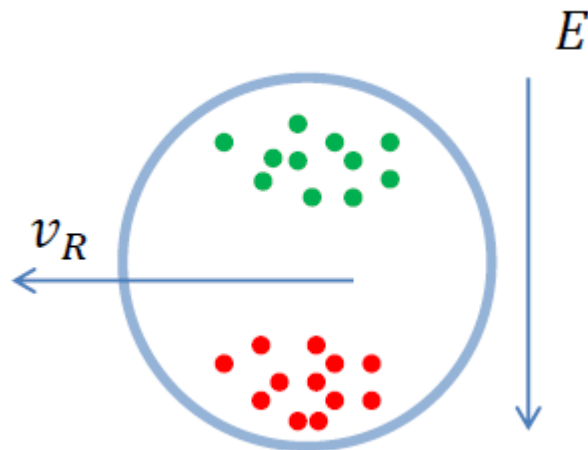
**Un campo elettrico E** fluttuante in un plasma magnetizzato a confinamento toroidale, produce un campo di velocità le cui linee di flusso coincidono con le linee equipotenziali del campo elettrico



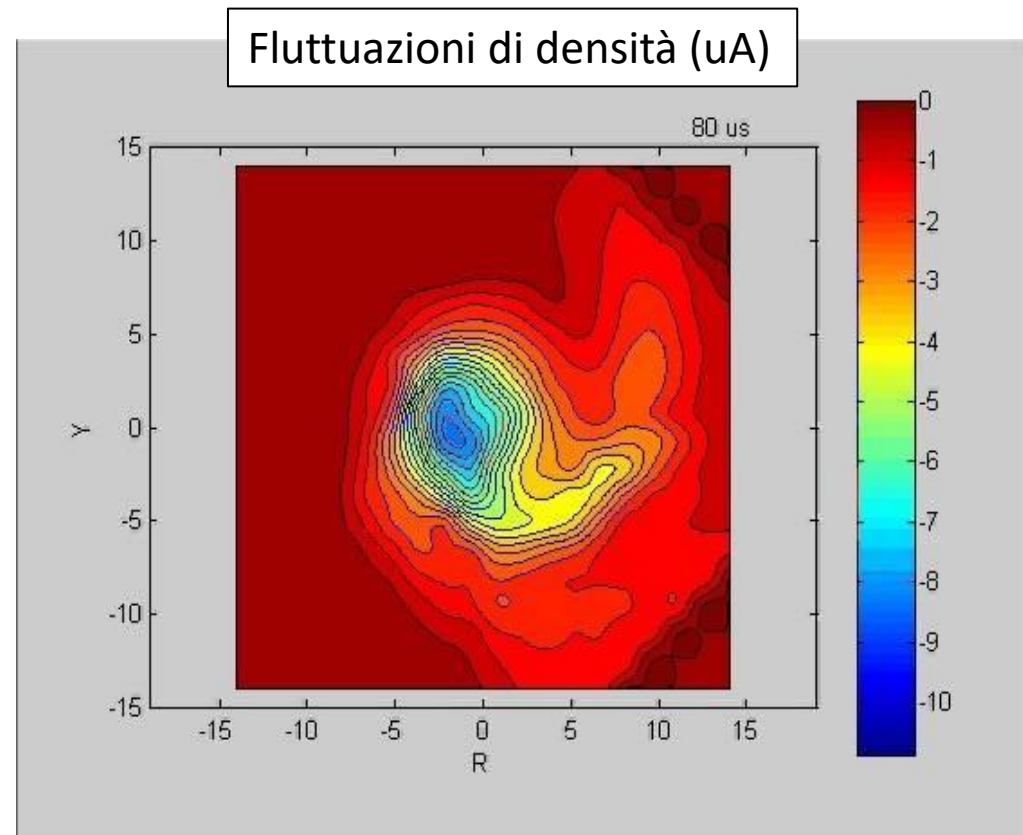
# Turbolenza

## Trasporto anomalo

**Una separazione di carica** in un plasma magnetizzato a confinamento toroidale produce una deriva globale  $E \times B$  verso l'esterno ( magnetic [grad(B)], centrifugal, diamagnetic [grad(P)], neutral drag)

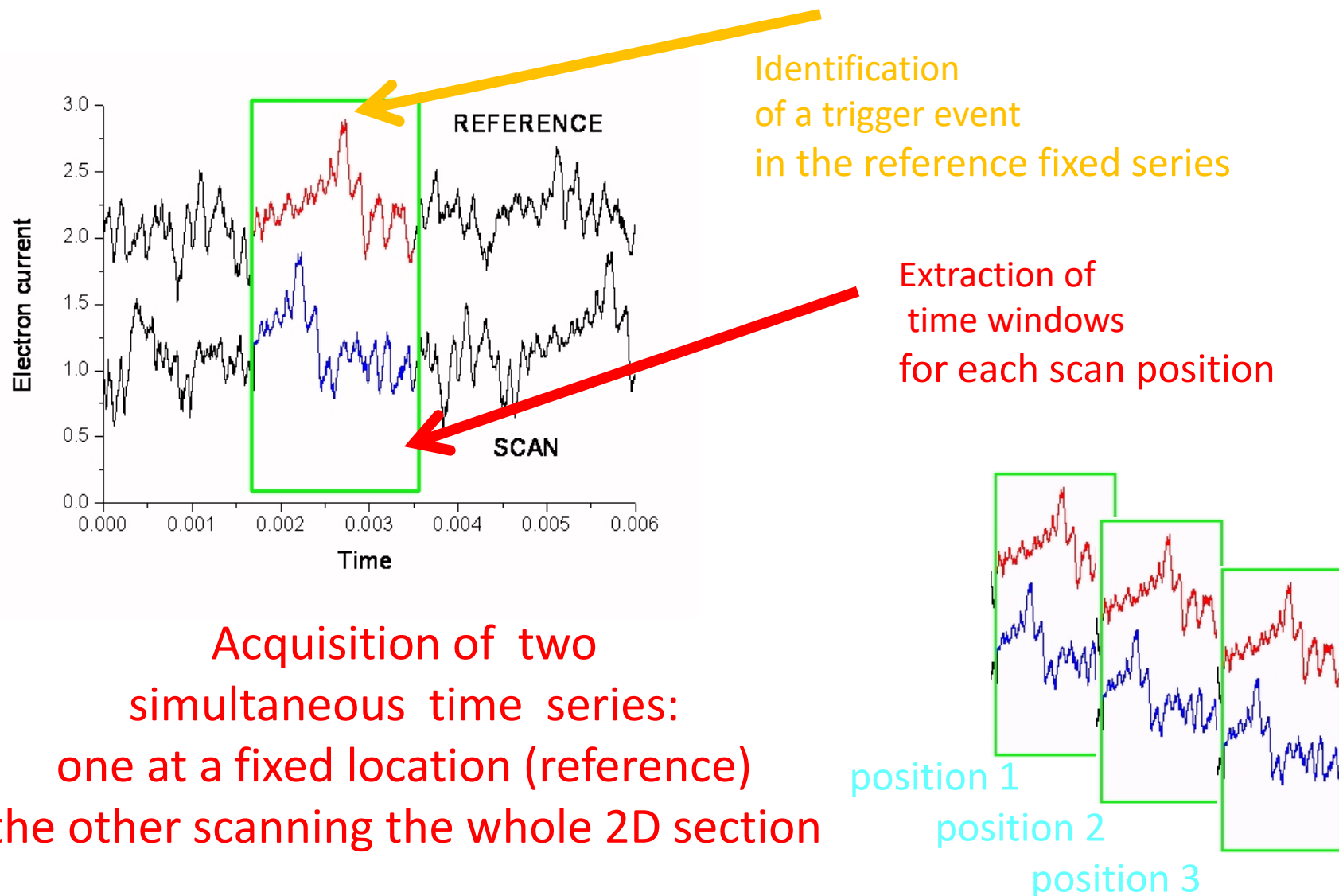


Exp Mistral - Marseille

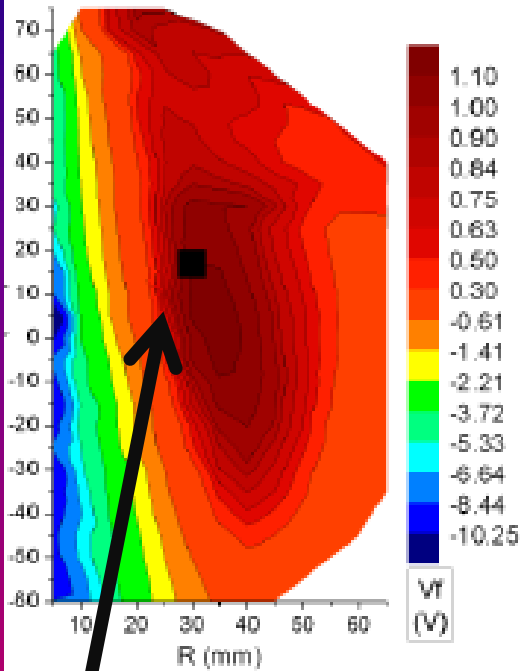


# Conditional sampling (analisi condizionale)

Reconstruction of the spatial and temporal correlations

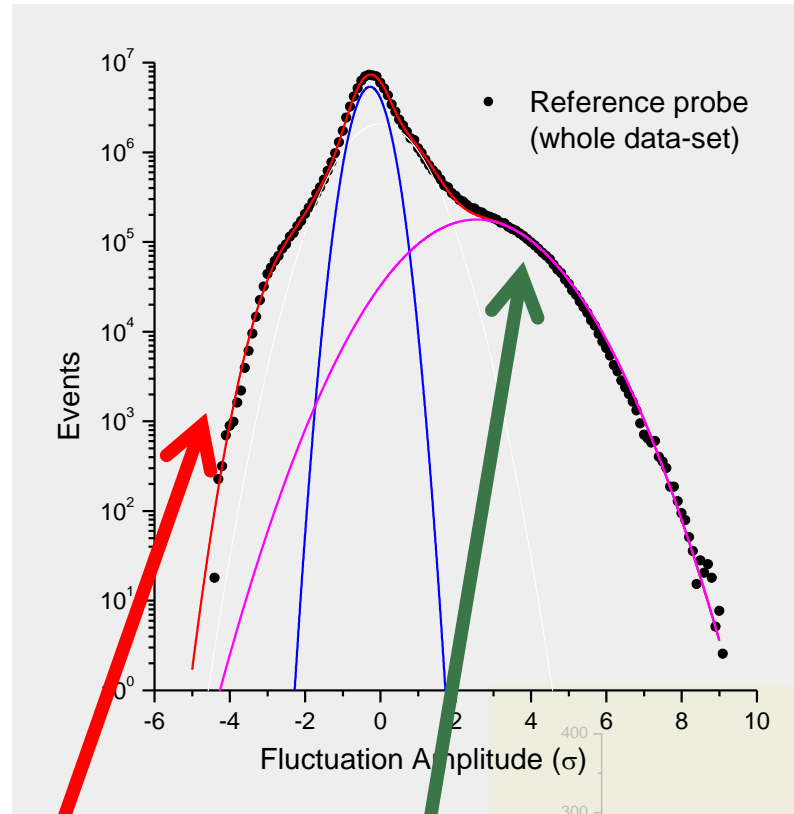


# Conditional sampling: trigger events



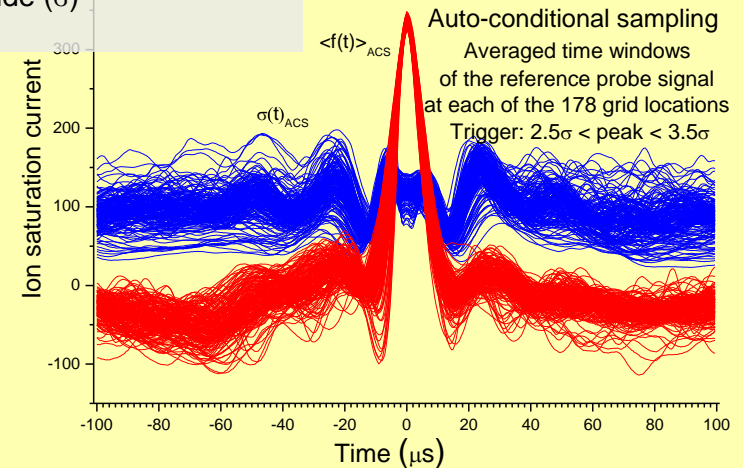
Reference probe

Negative density events:  
Voids



Density blobs

- Reference time windows:
- Selection of events
  - Cancellation of non-coherent fluctuations
  - Time Stability



# Esempio: eventi di flusso anomalo

Use a three-pin reference probe:  $I/V/V \Rightarrow (I_{sat}, E_{pol})$

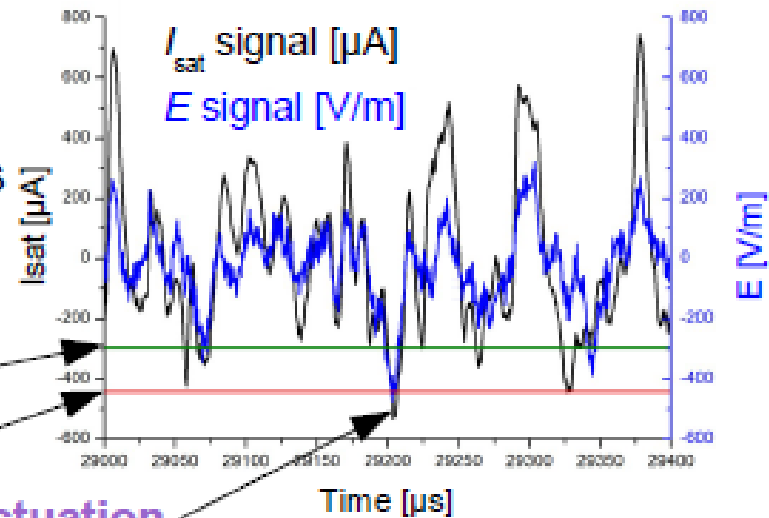
A certain condition is imposed to identify anomalous transport events within temporal series:

\* excess of a certain threshold

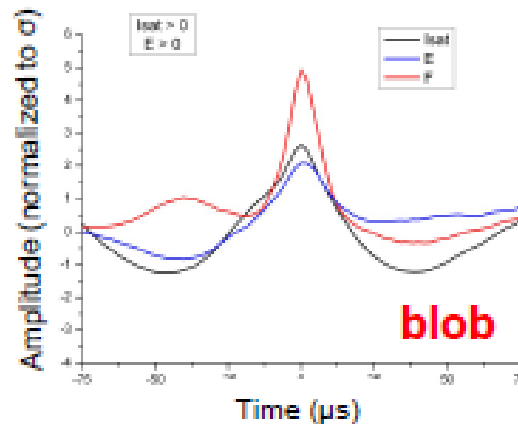
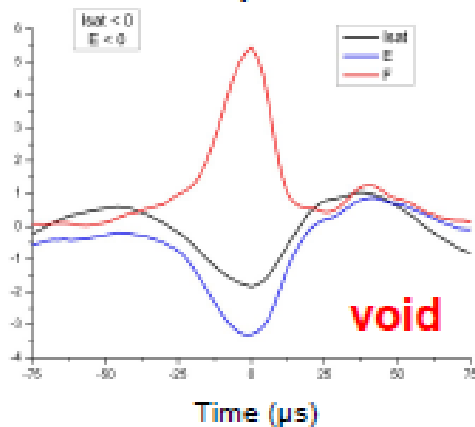
$E$  threshold

$I_{sat}$  threshold

simultaneous fluctuation



It correspond to a negative density fluctuation (void) associated with a radial inward  $E \times B$  velocity



Two kind of anomalous transport events