## DESCRIPTIVE STATISTICS

## Exercises

## EXERCISE 1

The following table shows the glycemia ( $\mathrm{mg} / \mathrm{dL}$ ) of 500 older adults grouped in 5 classes having the same width:

| CLASS <br> INTERVAL | MIDDLE <br> POINT | FREQUENCY |  | CUMULATIVE <br> FREQUENCY |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
|  |  | f | $\mathrm{p} \%$ |  | F |
| $\mathbf{n y y n n}-\mid 75$ | $\mathbf{7 0}$ | 75 | 15 | 75 | $\mathrm{P} \%$ |
| $75-\mid 85$ | 80 | 100 | 20 | 175 | 15 |
| $85-\mid 95$ | 90 | 150 | 30 | 225 | 35 |
| $95-\mid 105$ | 100 | 125 | 25 | 450 | 65 |
| $105-\mid 115$ | $\mathbf{1 1 0}$ | 50 | 10 | 500 | 90 |

a. Calculate mean and variance
b. Identify the modal class
c. Represent the data in a Galton Ogive and identify the glycemic value exceeded by only $5 \%$ of these older adults
d. Find the class containing the $50^{\text {th }}$ percentile

## SOLUTION 1

a.

To calculate the mean and the variance, it is necessary to consider the middle point as the representative value of each class.
$\begin{aligned} \bar{x}=\frac{\sum_{i=1}^{k} x_{i} \cdot f_{i}}{n} & =\frac{(70 \cdot 75)+(80 \cdot 100)+(90 \cdot 150)+(100 \cdot 125)+(110 \cdot 50)}{500}=\frac{44750}{500} \\ & =89.5 \mathrm{mg} / \mathrm{dL}\end{aligned}$
$s^{2}=\frac{\sum_{i=1}^{k}\left(x_{i}-\bar{x}\right)^{2} \cdot f_{i}}{(n-1)}$
$=\frac{(70-89.5)^{2} \cdot 75+(80-89.5)^{2} \cdot 100+(90-89.5)^{2} \cdot 150+(100-89.5)^{2} \cdot 125+(110-89.5)^{2} \cdot 50}{499}$
$=\frac{28518.75+9025+37.5+13781.25+21012.5}{499}=\frac{72375}{499}=145.04(\mathrm{mg} / \mathrm{dL})^{2}$
$s=\sqrt{s^{2}}=\sqrt{145.04}=12.04 \mathrm{mg} / \mathrm{dL}$
b.

The modal class is $85-\mid 95 \mathrm{mg} / \mathrm{dL}$
c.

$110 \mathrm{mg} / \mathrm{dL}$ is the glycemic value exceeded by only $5 \%$ of older adults
d.


The class containing the $50^{\text {th }}$ percentile is $85-\mid 95$. Consequently, the median is $90 \mathrm{mg} / \mathrm{dL}$

## EXERCISE 2

The following table shows the absolute frequencies of the hemoglobin blood concentration ( $\mathrm{g} / \mathrm{dL}$ ) categorized into 5 classes for 300 patients:

|  | Blood concentration of $\mathbf{~ H b}(\mathrm{g} / \mathrm{dL})$ |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | 12 | 13 | 14 | 15 | 16 |  |
|  | $(11.5,12.5]$ | $(12.5,13.5]$ | $(13.5,14.5]$ | $(14.5,15.5]$ | $(15.5,16.5]$ | Total |
| Females | 18 | 65 | 14 | 2 | 1 | $\mathbf{1 0 0}$ |
| Males | 2 | 40 | 71 | 58 | 29 | $\mathbf{2 0 0}$ |
| Total | $\mathbf{2 0}$ | $\mathbf{1 0 5}$ | $\mathbf{8 5}$ | $\mathbf{6 0}$ | $\mathbf{3 0}$ | $\mathbf{3 0 0}$ |

a. What is the proportion of patients with $\mathrm{Hb}>14.5 \mathrm{~g} / \mathrm{dL}$ ?
b. What is the proportion of females with $\mathrm{Hb}>14.5 \mathrm{~g} / \mathrm{dL}$ ?
c. What is the proportion of males with $\mathrm{Hb}>14.5 \mathrm{~g} / \mathrm{dL}$ ?
d. What is the proportion of females among patients with $\mathrm{Hb}<12.5 \mathrm{~g} / \mathrm{dL}$ ?

## SOLUTION 2

a.
$p=\frac{60+30}{300}=\frac{90}{300}=0.3$
b.
$p=\frac{2+1}{100}=\frac{3}{100}=0.03$
c.
$p=\frac{58+29}{200}=\frac{87}{200}=0.435$
d.
$p=\frac{18}{20}=0.9$

## EXERCISE 3

Five men with obesity have been visited in the same day. The following table shows their weights (kg):

| Patient ID | Weight $(\mathrm{kg})$ |
| :---: | :---: |
| 1 | 120 |
| 2 | 147 |
| 3 | 132 |
| 4 | 128 |
| 5 | 138 |

a. Calculate mean and standard deviation

The scale was later discovered to have been calibrated badly and that all measurements were wrong overestimated by 5 kg .
b. Calculate mean and standard deviation
c. Calculate mean and standard deviation in hg
d. Calculate the coefficient of variation of the weight both in kg and hg

## SOLUTION 3

a.
$\bar{x}=\frac{120+147+132+128+138}{5}=\frac{665}{5}=133 \mathrm{~kg}$
$s=\sqrt{\frac{(120-133)^{2}+(147-133)^{2}+(132-133)^{2}+(128-133)^{2}+(138-133)^{2}}{4}}$
$=\sqrt{\frac{169+196+1+25+25}{4}}=\sqrt{\frac{416}{4}}=\sqrt{104}=10.2 \mathrm{~kg}$
b.
$\bar{x}=133-5=128 \mathrm{~kg}$
$s=10.2 \mathrm{~kg} \rightarrow$ remain unchanged
c.
$1 \mathrm{~kg}=10 \mathrm{hg}$. So,
$\bar{x}=128 \cdot 10=1280 \mathrm{hg}$
$s=10.2 \cdot 10=102 \mathrm{hg}$
d.
$C V=\frac{s}{\bar{x}}=\frac{128}{10.2}=\frac{12.8}{1.02}=12.55$

## E

## EXERCISE 4

A sample is composed by 120 males and 80 females. The following table shows their age in years with the percentage distribution by gender:

| Age (years) | Males (\%) | Females (\%) |
| :--- | :--- | :--- |
| $0-19$ | 10 | 20 |
| $20-29$ | 10 | 20 |
| $30-49$ | 30 | 30 |
| $50-89$ | 50 | 30 |
| Total | 100 | 100 |

a. How many people are< 20 years old?
b. What is the percentage of individuals that are $\geq 50$ years old?
c. How many males are $\geq 30$ years old?
d. Find the modal classes for males and females separately and for the total sample
e. Identify the median of the total sample

## SOLUTION 4

|  | Males (years) |  | Females |  |  |
| :--- | :---: | :---: | :---: | :---: | :---: |
|  | $\mathbf{p \%}$ | $\mathbf{f}$ | $\mathbf{p} \%$ | $\mathbf{f}$ |  |
| $0-19$ | 10 | 12 | 20 | 16 |  |
| $20-29$ | 10 | 12 | 20 | 16 |  |
| $30-49$ | 30 | 36 | 30 | 24 |  |
| $50-89$ | 50 | 60 | 30 | 24 |  |
| Total | 100 | 120 | 100 | 80 |  |

a.

28 subjects are < 20 years old
b.

$$
\frac{60+24}{120+80}=0.42 \rightarrow 42 \%
$$

c.

96 males are $\geq 30$ years old
d.

Modal class for males: 50-89 years
Modal class for females: 30-49 and 50-89 years $\rightarrow$ bimodal distribution
Modal class overall: 50-89 years
e.


The median age of the total sample is 35 years.

## EXERCISE 5

The following table shows the distribution of frequencies of the attitude towards smoking observed in a group of young people.

|  | Age |  |  |  |
| :--- | :---: | :---: | :---: | :---: |
|  | $[16,18]$ | $\mathbf{1 1 8}, \mathbf{2 2}]$ | ]22, 25] | ]25, 30] |
| Smoking habit | 7 | 8 | 21 | 30 |
|  | 16 | 18 | 9 | 10 |
| No |  |  |  |  |

a. Calculate the mean age of the smokers and non-smokers
b. Identify the median age class of the smokers and non-smokers
c. Identify the modal age class of the smokers and non-smokers

## SOLUTION 6

Age
$[16,18] \quad] 18,22] \quad$ ]22, 25] $] 25,30]$

## Smoking habit

| (class middle point) | 17 | 20.5 | 24 | 28 |
| :--- | :---: | :---: | :---: | :---: |
| Yes | 7 | 8 | 21 | 30 |
| No | 16 | 18 | 9 | 10 |

a.
$\bar{x}_{S}=\frac{(17 \cdot 7)+(20.5 \cdot 8)+(24 \cdot 21)+(28 \cdot 30)}{66}=\frac{119+164+504+840}{66}=\frac{1627}{66}=24.65$
$\bar{x}_{N S}=\frac{(17 \cdot 16)+(20.5 \cdot 18)+(24 \cdot 9)+(28 \cdot 10)}{53}=\frac{272+369+216+280}{53}=\frac{1137}{53}=21.45$
b.

Adding the cumulative frequencies into the table:

|  | Age |  |  |  |  |
| :--- | :---: | :---: | :---: | :---: | :---: |
| Smoking habit | $[16, \mathbf{1 8}]$ | $\mathbf{1 1 8 , 2 2 ]}$ | ]22, 25] | ]25, 30] | Total |
| (class middle point) | 17 | 20.5 | 24 | 28 |  |
| Yes | $7(11 \%)$ | $8(23 \%)$ | $21(55 \%)$ | $30(100 \%)$ | 66 |
| No | $16(30 \%)$ | $18(64 \%)$ | $9(81 \%)$ | $10(100 \%)$ | 53 |

Median age class for smokers: ]22, 25]
Median age class for non-smokers: ]18, 22]
c.

Modal class for smokers: ]25, 30] years
Modal class for non-smokers: ]18, 22] years

