## **DESCRIPTIVE STATISTICS**

# Exercises

## EXERCISE 1

The following table shows the glycemia (mg/dL) of 500 older adults grouped in 5 classes having the same width:

| CLASS<br>INTERVAL | MIDDLE<br>POINT | FREQUENCY | CUMULATIVE<br>FREQUENCY |     |     |
|-------------------|-----------------|-----------|-------------------------|-----|-----|
|                   |                 | f         | р%                      | F   | P%  |
| 65- 75            | 70              | 75        | 15                      | 75  | 15  |
| 75- 85            | 80              | 100       | 20                      | 175 | 35  |
| 85- 95            | 90              | 150       | 30                      | 225 | 65  |
| 95- 105           | 100             | 125       | 25                      | 450 | 90  |
| 105- 115          | 110             | 50        | 10                      | 500 | 100 |

a. Calculate mean and variance

- b. Identify the modal class
- c. Represent the data in a Galton Ogive and identify the glycemic value exceeded by only 5% of these older adults
- d. Find the class containing the 50<sup>th</sup> percentile

### **SOLUTION 1**

a.

To calculate the mean and the variance, it is necessary to consider the middle point as the representative value of each class.

$$\begin{split} \bar{x} &= \frac{\sum_{i=1}^{k} x_i \cdot f_i}{n} = \frac{(70 \cdot 75) + (80 \cdot 100) + (90 \cdot 150) + (100 \cdot 125) + (110 \cdot 50)}{500} = \frac{44750}{500} \\ &= 89.5 \ mg/dL \\ s^2 &= \frac{\sum_{i=1}^{k} (x_i - \bar{x})^2 \cdot f_i}{(n-1)} \\ &= \frac{(70 - 89.5)^2 \cdot 75 + (80 - 89.5)^2 \cdot 100 + (90 - 89.5)^2 \cdot 150 + (100 - 89.5)^2 \cdot 125 + (110 - 89.5)^2 \cdot 50}{499} \\ &= \frac{28518.75 + 9025 + 37.5 + 13781.25 + 21012.5}{499} = \frac{72375}{499} = 145.04(mg/dL)^2 \\ s &= \sqrt{s^2} = \sqrt{145.04} = 12.04 \ mg/dL \end{split}$$

The modal class is 85-|95 mg/dL

с.



110 mg/dL is the glycemic value exceeded by only 5% of older adults



The class containing the 50<sup>th</sup> percentile is 85-|95. Consequently, the median is 90 mg/dL

### EXERCISE 2

The following table shows the absolute frequencies of the hemoglobin blood concentration (g/dL) categorized into 5 classes for 300 patients:

|         | Blood concentration of Hb (g/dL) |              |                      |                      |              |       |
|---------|----------------------------------|--------------|----------------------|----------------------|--------------|-------|
|         | 12                               | 13           | 14                   | 15                   | 16           | Total |
|         | (11.5, 12.5]                     | (12.5, 13.5] | (13.5 <i>,</i> 14.5] | (14.5 <i>,</i> 15.5] | (15.5, 16.5] | Iotai |
| Females | 18                               | 65           | 14                   | 2                    | 1            | 100   |
| Males   | 2                                | 40           | 71                   | 58                   | 29           | 200   |
| Total   | 20                               | 105          | 85                   | 60                   | 30           | 300   |

a. What is the proportion of patients with Hb> 14.5 g/dL?

b. What is the proportion of females with Hb> 14.5 g/dL?

- c. What is the proportion of males with Hb> 14.5 g/dL?
- d. What is the proportion of females among patients with Hb< 12.5 g/dL?

### **SOLUTION 2**

а.

$$p = \frac{60 + 30}{300} = \frac{90}{300} = 0.3$$

b.

$$p = \frac{2+1}{100} = \frac{3}{100} = 0.03$$

с.

$$p = \frac{58 + 29}{200} = \frac{87}{200} = 0.435$$

d.

$$p = \frac{18}{20} = 0.9$$

### EXERCISE 3

Five men with obesity have been visited in the same day. The following table shows their weights (kg):

| Patient ID | Weight (kg) |  |  |
|------------|-------------|--|--|
| 1          | 120         |  |  |
| 2          | 147         |  |  |
| 3          | 132         |  |  |
| 4          | 128         |  |  |
| 5          | 138         |  |  |
|            |             |  |  |

a. Calculate mean and standard deviation

The scale was later discovered to have been calibrated badly and that all measurements were wrong overestimated by 5 kg.

- b. Calculate mean and standard deviation
- c. Calculate mean and standard deviation in hg
- d. Calculate the coefficient of variation of the weight both in kg and hg

### **SOLUTION 3**

a.

$$\bar{x} = \frac{120 + 147 + 132 + 128 + 138}{5} = \frac{665}{5} = 133 \, kg$$

$$s = \sqrt{\frac{(120 - 133)^2 + (147 - 133)^2 + (132 - 133)^2 + (128 - 133)^2 + (138 - 133)^2}{4}}$$

$$= \sqrt{\frac{169 + 196 + 1 + 25 + 25}{4}} = \sqrt{\frac{416}{4}} = \sqrt{104} = 10.2 \, kg$$

b.

 $\bar{x} = 133 - 5 = 128 \ kg$  $s = 10.2 \ kg \rightarrow$ remain unchanged

с.

1 kg= 10 hg. So,  $\bar{x} = 128 \cdot 10 = 1280 hg$  $s = 10.2 \cdot 10 = 102 hg$ 

d.

# $CV = \frac{s}{\bar{x}} = \frac{128}{10.2} = \frac{12.8}{1.02} = 12.55$

<u>E</u>

## EXERCISE 4

A sample is composed by 120 males and 80 females. The following table shows their age in years with the percentage distribution by gender:

| Age (years) | Males (%) | Females (%) |
|-------------|-----------|-------------|
| 0-19        | 10        | 20          |
| 20-29       | 10        | 20          |
| 30-49       | 30        | 30          |
| 50-89       | 50        | 30          |
| Total       | 100       | 100         |

- a. How many people are< 20 years old?
- b. What is the percentage of individuals that are≥ 50 years old?
- c. How many males are  $\geq$  30 years old?
- d. Find the modal classes for males and females separately and for the total sample
- e. Identify the median of the total sample

### **SOLUTION 4**

| Age (years) | Males |     | Females |    |  |
|-------------|-------|-----|---------|----|--|
|             | р%    | f   | р%      | f  |  |
| 0-19        | 10    | 12  | 20      | 16 |  |
| 20-29       | 10    | 12  | 20      | 16 |  |
| 30-49       | 30    | 36  | 30      | 24 |  |
| 50-89       | 50    | 60  | 30      | 24 |  |
| Total       | 100   | 120 | 100     | 80 |  |

a.

28 subjects are < 20 years old

$$\frac{60+24}{120+80} = 0.42 \rightarrow 42\%$$

96 males are  $\geq$  30 years old

### d.

Modal class for males: 50-89 years

Modal class for females: 30-49 and 50-89 years  $\rightarrow$  bimodal distribution

Modal class overall: 50-89 years





The median age of the total sample is 35 years.

## EXERCISE 5

The following table shows the distribution of frequencies of the attitude towards smoking observed in a group of young people.

|               | Age      |          |          |          |  |
|---------------|----------|----------|----------|----------|--|
| Smoking habit | [16, 18] | ]18, 22] | ]22, 25] | ]25, 30] |  |
| Yes           | 7        | 8        | 21       | 30       |  |
| No            | 16       | 18       | 9        | 10       |  |

a. Calculate the mean age of the smokers and non-smokers

b. Identify the median age class of the smokers and non-smokers

c. Identify the modal age class of the smokers and non-smokers

## **SOLUTION 6**

|          | Age<br>[16, 18] ]18, 22] ]22, 25] ]25, 30] |          |          |
|----------|--|----------|----------|
| [16, 18] | ]18, 22]                                   | ]22, 25] | ]25, 30] |

| Smoking habit        |    |      |    |    |
|----------------------|----|------|----|----|
| (class middle point) | 17 | 20.5 | 24 | 28 |
| Yes                  | 7  | 8    | 21 | 30 |
| No                   | 16 | 18   | 9  | 10 |

а.

$$\bar{x}_{S} = \frac{(17 \cdot 7) + (20.5 \cdot 8) + (24 \cdot 21) + (28 \cdot 30)}{66} = \frac{119 + 164 + 504 + 840}{66} = \frac{1627}{66} = 24.65$$
$$\bar{x}_{NS} = \frac{(17 \cdot 16) + (20.5 \cdot 18) + (24 \cdot 9) + (28 \cdot 10)}{53} = \frac{272 + 369 + 216 + 280}{53} = \frac{1137}{53} = 21.45$$

b.

## Adding the cumulative frequencies into the table:

| Age                  |                       |                       |          |                  |       |
|----------------------|-----------------------|-----------------------|----------|------------------|-------|
| Smoking habit        | [16, 18]              | ]18, 22]              | ]22, 25] | ]25, 30]         | Total |
| (class middle point) | 17                    | 20.5                  | 24       | 28               |       |
| Yes                  | 7 (11%)               | 8 (23%)               | 21 (55%) | 30 <b>(100%)</b> | 66    |
| No                   | 16 <mark>(30%)</mark> | 18 <mark>(64%)</mark> | 9 (81%)  | 10 (100%)        | 53    |

Median age class for smokers: ]22, 25]

Median age class for non-smokers: ]18, 22]

с.

Modal class for smokers: ]25, 30] years

Modal class for non-smokers: ]18, 22] years