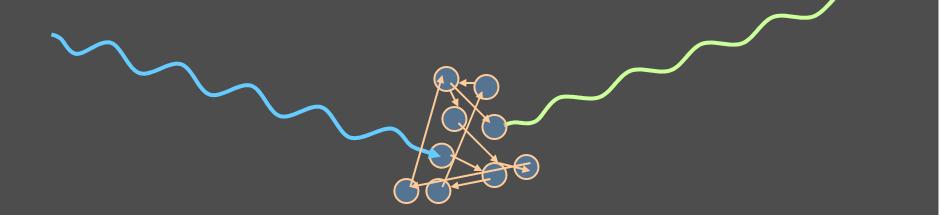
Förster (Fluorescence) Resonance Energy Transfer (FRET)

- Great method for the detection of:
  - Protein-protein interactions
  - Enzymatic activity
  - Small molecules interacting inside a cell

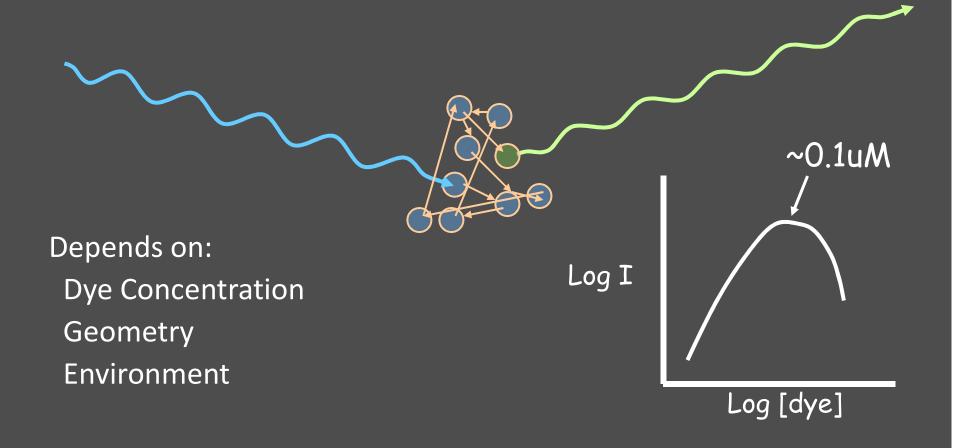
Resonance Energy Transfer (non-radiative) The Bad: Self-quenching



If dye at high concentration "hot-potato" the energy until lost Resonance Energy Transfer (non-radiative)

"Self-quenching" of dye

("hot-potato" the energy until lost)



# FRET: Resonance Energy Transfer (non-radiative) The Good: FRET as a molecular yardstick

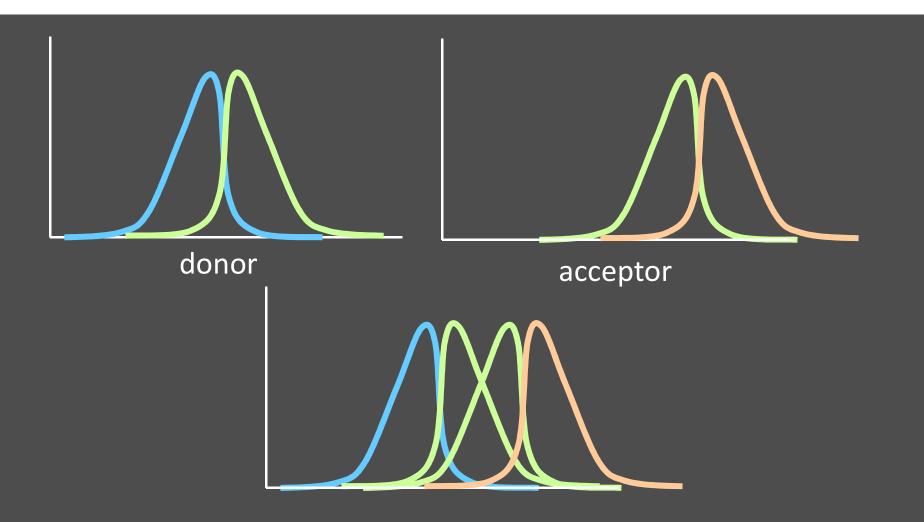
Transfer of energy from one dye to another

Depends on:

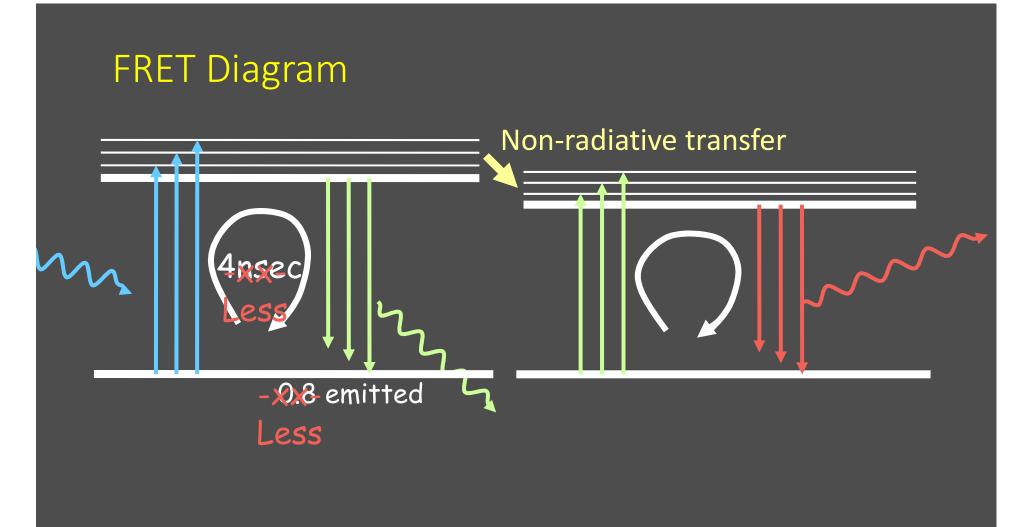
Spectral overlap

Distance

Alignment



FRET:
Optimize spectral overlap
Optimize κ<sup>2</sup> -- alignment of dipoles
Minimize direct excitement of the acceptor (extra challenge for filter design)



$$K_{\rm T} = (1/\tau_{\rm D}) \bullet [{\rm R}_0/{\rm r}]^6$$
$$E = \frac{1}{1 + (r/R_0)^6} = 1 - \frac{\tau'_D}{\tau_D}$$

The Förster Equations.

$$R_{0} = 2.11 \times 10^{-2} \bullet [\kappa^{2} \bullet J(\lambda) \bullet \eta^{-4} \bullet Q_{D}]^{1/6}$$
$$J(\lambda) = \int f_{D}(\lambda) \mathcal{E}_{A}(\lambda) \lambda^{4} d\lambda$$
$$E = 1 - \frac{F'_{D}}{F_{D}}$$

r is the center-to-center distance (in cm) between the donor and acceptor

 $\tau_{\text{D}}$  is the fluorescence lifetime of the donor in the absence of FRET

 $\kappa^2$  is the dipole-dipole orientation factor,

 $Q_D$  is the quantum yield of the donor in the absence of the acceptor  $\eta$  is the refractive index of the intervening medium,

 $F_D(\lambda)$  is the fluorescence emission intensity at a given wavelength  $\lambda$  (in cm)

 $\varepsilon_A$  ( $\lambda$ ) is the extinction coefficient of the acceptor (in cm <sup>-1</sup> M <sup>-1</sup>).

The orientation factor  $\kappa^2$  can vary between 0 and 4, but typically  $\kappa^2$  = 2/3 for randomly oriented molecules (Stryer, 1978).

```
When r = R_0, the efficiency of FRET is 50% (fluorescein-tetramethylrhodamine pair is 55 Å)
```

# FRET: Resonance Energy Transfer (non-radiative) The Good: FRET as a molecular yardstick

Transfer of energy from one dye to another

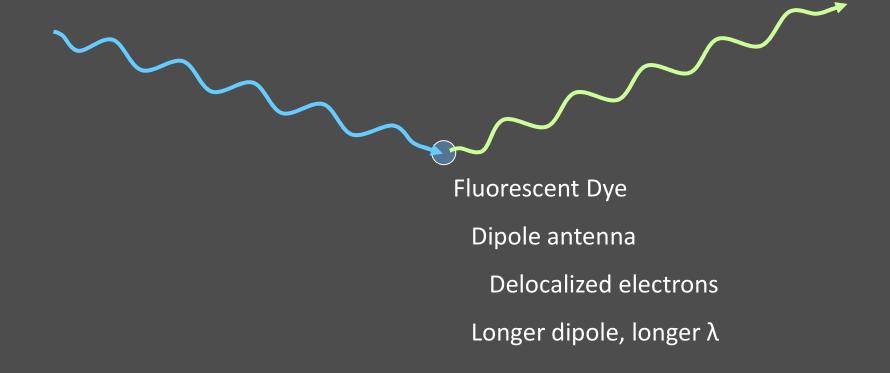
Depends on:

Spectral overlap

Distance

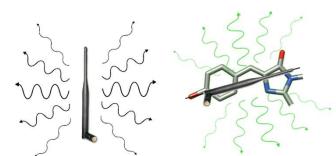
Alignment

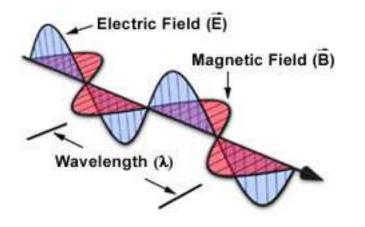
### How dipole affects FRET as a molecular yardstick

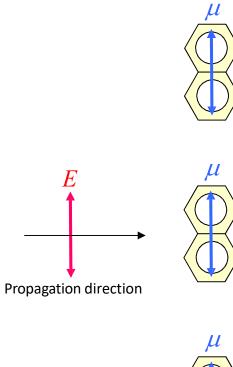


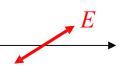
Fluorescent dye as dipole antenna

• Absorption depends on orientation









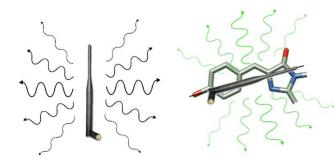


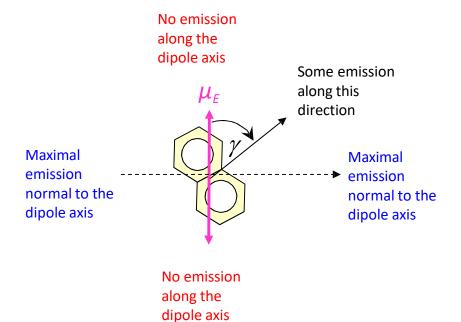
**Propagation direction** 

E

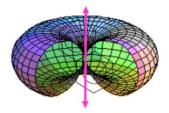
## Fluorescent dye as dipole antenna

• Orientation of fluorescence emission

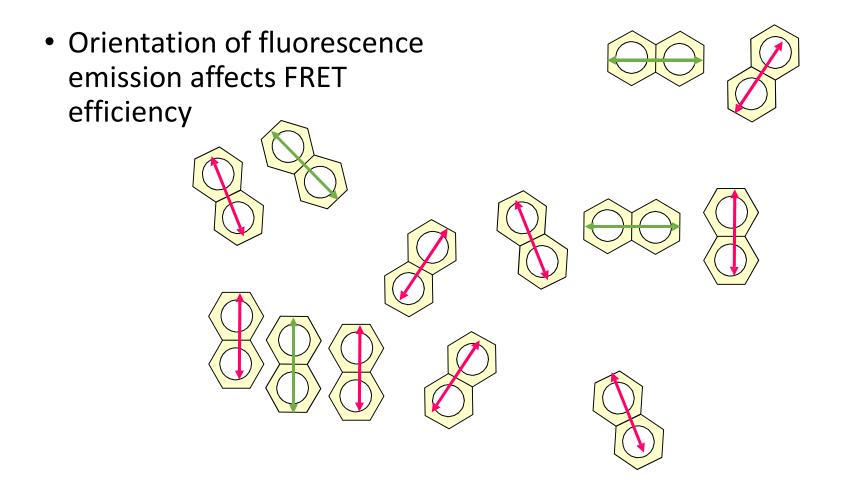




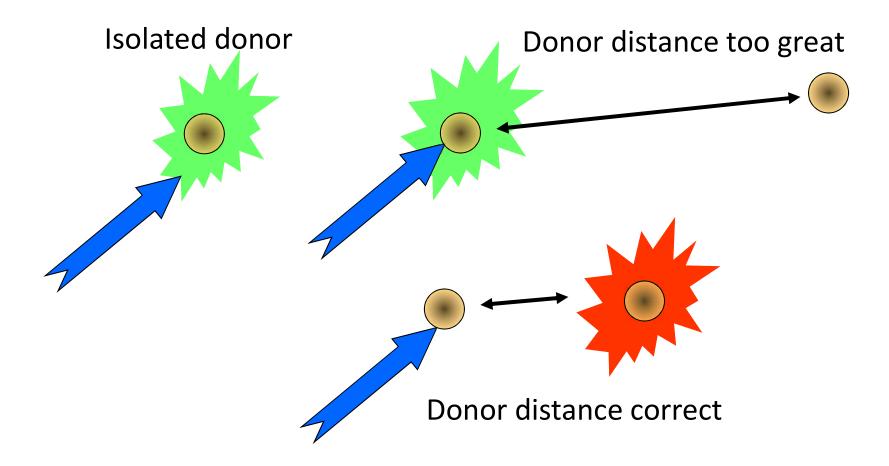
Dipole radiation pattern



Fluorescent dye as dipole antenna



### More about FRET (Förster Resonance Energy Transfer)



#### Effective between 10-100 Å only

Emission and excitation spectrum must significantly overlap

Note: donor transfers non-radiatively to the acceptor

From J. Paul Robinson, Purdue University

#### FRET efficiency and the Förster Equations

- Distance between donor and acceptor
- When r = R<sub>0</sub>, the efficiency of FRET is 50%
- When  $R < R_0$ ,  $E_{FRET} > 0.50$
- When  $R > R_0$ ,  $E_{FRET} < 0.50$

$$\begin{split} \mathsf{K}_{\mathsf{T}} &= (1/\tau_{\mathsf{D}}) \bullet [\mathsf{R}_{0}/\mathsf{r}]^{6} \\ E &= \frac{1}{1 + (r/R_{0})^{6}} = 1 - \frac{\tau'_{D}}{\tau_{D}} \\ \mathsf{R}_{0} &= 2.11 \times 10^{-2} \bullet [\kappa^{2} \bullet \mathsf{J}(\lambda) \bullet \mathsf{\eta}^{-4} \bullet \mathsf{Q}_{0}] \\ J(\lambda) &= \int f_{\mathsf{D}}(\lambda) \, \mathcal{E}_{\mathsf{A}}(\lambda) \, \lambda^{4} \, d\lambda \end{split}$$

