

$$J_{thi} < \omega_B < J_{the}$$

$$\bar{I}_B \sim 100 \text{ keV} \quad F_{\text{fusion}} \sim 10 \text{ keV}$$

$$T \sim \text{keV} \quad n = \frac{\omega}{J_{th}} \quad \left| \begin{array}{l} \text{products} \end{array} \right.$$

$$T_i \sim T_e \Rightarrow J_{the} \gg J_{thi}$$

$$\frac{du}{dt} = \frac{e^2 q^2 \ln \Lambda n_e}{4\pi \epsilon_0^2 m_T^2} \left[ \left(1 + \frac{m_T}{m_e}\right) \frac{m_e}{2T_e} \frac{d}{dx_e} \left( \frac{1}{x_e} \text{erf}(x_e) \right) \right. \\ \left. + Z \left(1 + \frac{m_T}{m_i}\right) \frac{m_i}{2T_i} \frac{d}{dx_i} \left( \frac{1}{x_i} \text{erf}(x_i) \right) \right]$$

$$x_i \gg 1$$

$$x_e \ll 1$$

$$\frac{d}{dx_i} \left( \frac{1}{x_i} \text{erf}(x_i) \right)$$

$$\frac{d}{dx_e} \left( \frac{1}{x_e} \text{erf}(x_e) \right) \approx \frac{-4}{3\sqrt{\pi}} x_e$$

$$12 \frac{1}{x_i}$$

$$\frac{du}{dt} \approx \frac{-e^2 q_T^2 \ln \Lambda n_e}{4\pi \epsilon_0^2 m_T^2} \left[ \left(1 + \frac{m_T}{m_e}\right) \frac{4}{3\sqrt{\pi}} u \left(\frac{m_e}{2Te}\right)^{3/2} + \right. \\ \left. + Z \left(1 + \frac{m_T}{m_i}\right) \frac{1}{u^2} \right]$$

Observe that:  $\left(1 + \frac{m_T}{m_e}\right) \frac{4}{3\sqrt{\pi}} u \left(\frac{m_e}{2Te}\right)^{3/2} = Z \left(1 + \frac{m_T}{m_i}\right) \frac{1}{u^2}$

$$u_{Cr} = \left[ \frac{Z \left(1 + \frac{m_T}{m_i}\right)}{1 + \frac{m_T}{m_e}} \frac{3\sqrt{\pi}}{4} \left(\frac{2Te}{m_e}\right)^{3/2} \right]^{1/3}$$

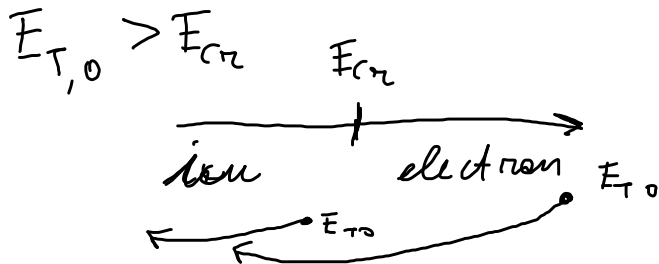
Critical energy:

$$\frac{1}{2} m_T u_{cr}^2 = K \cdot T_e$$

$$K \approx 20 \div 30$$

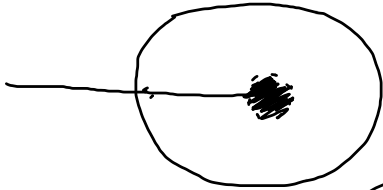
$\int E_T > E_{cr}$ : slowing down mostly due  
to el. collisions  
 $\Rightarrow$  el. heating

$\int E_T < E_{cr}$ : = = = due  
to ion collisions



$\Rightarrow$  ion heating

# Neutral beam injection



$F_{T0}$  is predominantly determined by the need to drive most of the 'ionization' in the core

Dependence:  $\begin{cases} \text{machine size} \\ \text{density} \end{cases}$

Joint European Torus  
(JET)

$$R_0 \approx 3 \text{ m} \quad a \approx 1 \text{ m}$$

$$n \sim 5 \cdot 10^{19} \text{ m}^{-3}$$

$$E_{T0} \sim 100 \text{ keV}$$

$$T \sim 5 \div 10 \text{ keV}$$

$$30 \cdot T \sim 150 \div 300 \text{ keV}$$

$$E_{T0} < E_{\text{critical}}$$

ITER

$$R_0 \approx 6 \text{ m} \quad a \approx 2 \text{ m}$$

$$n \sim 10^{20} \text{ m}^{-3}$$

$$T \sim 10 \div 20 \text{ keV}$$

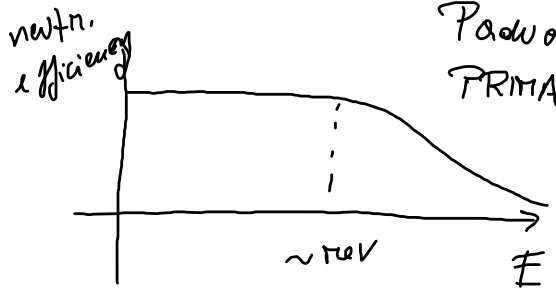
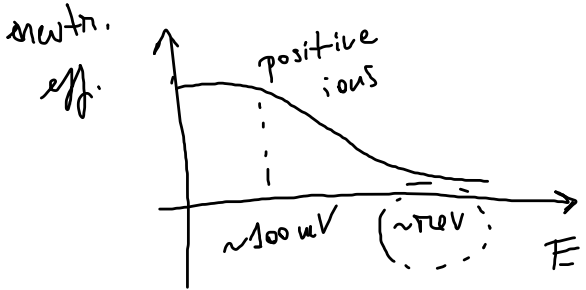
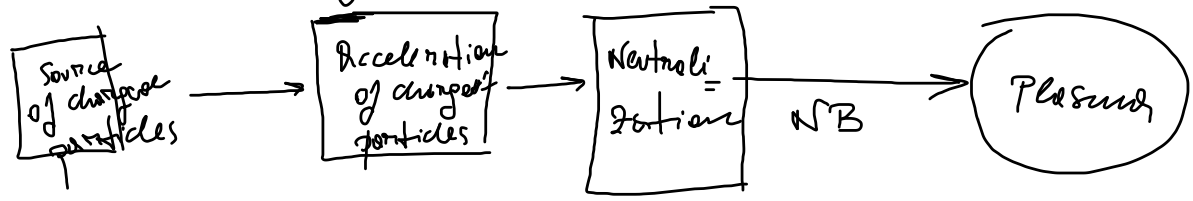
$$30 \cdot T \sim 300 \div 600 \text{ keV}$$

$$E_{T0} \rightarrow E_{\text{critical}}$$

$$E_{T0} \sim 1 \text{ MeV}$$

$$E \sim 10 \text{ MeV} \quad \bar{I}_{\text{fusion product}} > E_{\text{critical}}$$

# Neutral Beam System



Padua  
PRIMA



$$P = I \cdot V$$

$\sim \text{A} \cdot \text{MV}$